Period

Date \_\_\_\_\_







#### MATHLINKS: GRADE 7 STUDENT PACKET 15 SCALE DRAWINGS AND CIRCLE MEASUREMENTS

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## WORD BANK

Word or Phrase	Definition or Descripti	on	Example or Picture
center of a circle			
chord			
circle			
circumference			
diamotor			
ulameter			
рі			
radius			
scale			
scale drawing			
scale factor			

# SCALE DRAWINGS

#### Summary

Goals

We will make scale drawings with different scale factors. We will use ratio strips and rulers to construct and read drawings made to scale.

- Explore the effect of different scale factors on scale drawings.
- Read and analyze drawings made to scale.

- 1. Whose face is:
  - a. twice as long as Buddy's?
  - b. twice as wide as Buddy's?
  - c. both twice as long and twice as wide as Buddy's?
- 2. Whose face is:
  - a. half as long as Dabney's?
  - b. half as wide as Dabney's?
  - c. both half as long and half as wide as Dabney's?
  - d. twice as wide as Buddy's.
  - e. both twice as long and twice as wide as Buddy's.
- 3. A scale factor is a positive number which multiplies some quantity. Whose face:
  - a. represents Buddy's face multiplied by a scale factor of 2?
  - b. represents Dabney's face multiplied by a scale factor of  $\frac{1}{2}$ ?
- 4. Which two faces look the most alike? \_\_\_\_\_ and \_\_\_\_\_





## **SCALE FACTORS: ARROWS**

Each arrow is made by combining a rectangle with a triangle as shown below. Draw each arrow on the grid paper based on arrow #1, and complete the table.

Arrow #	Scale factor	Rewrite the scale factor as a fraction or decimal	Enlargement or Reduction?	Height of the rectangle	Base of the triangle	Area of the arrow
1	100%		neither	4 units	4 units	
2	200%					
3	50%					
4	150%					
5	25%					
6	125%					



## **SCALE FACTORS: SQUARES**

Draw each square on the grid paper based on square #1 below and complete the table.

Square #	Scale factor	Rewrite the scale factor as a percent value	Enlargement or Reduction?	Length of a side	Area of the square
1	1	100%			
2	2				
3	0.5				
4	$1\frac{1}{2}$				
5	$\frac{1}{4}$				
6	1.25				



## **PATTERNS** IN RATIOS

Use the pages 3 and 4 to complete the table. Write		Ratio of scale factors	Ratio of side lengths	Ratio of areas
eac	h ratio and its value.	Value of ratio	Value of ratio	Value of ratio
1	Square 2: Square 1	2 : 1		
1.	Square 2. Square 1	2		
2.	Square 3: Square 4			
3.	Square 6: Square 5			
4.	Arrow 1: Arrow 2		4:8 1 2	
5.	Arrow 4: Arrow 3			
6.	Arrow 6: Arrow 5			

7. What do you notice about values of the ratios of the scale factors and the corresponding values of ratios of the side lengths?

8. What do you notice about the values of the ratios of side lengths and the values of the ratios of areas?

## USING A RATIO STRIP

In a <u>scale drawing</u>, all lengths are multiplied by the same scale factor. If the scale factor is greater than 1, the figure is expanded, and if the scale factor is between 0 and 1, the figure is reduced in size.

Sometimes the scale in a drawing is described using a ratio. A <u>ratio strip</u> is a double number line where equivalent ratios can be easily identified. You will use Ratio Strip 1 to interpret drawings using a scale of 2 cm : 9 ft.

1. Complete the sequence of numbers on each edge of the strip. Then measure each line segment below with the ratio strip to the nearest whole cm. Finally write how many feet each line segment would represent on a scale drawing.

2. Here is a drawing of a garden that was created using the scale 2 cm : 9 ft. Use Ratio Strip 1 to determine the actual dimensions and area of the garden.



width

	Drawing dimensions	Drawing area	Garden dimensions	Garden area
Length				
Width				

Use the data from the table above to complete the table below.

		Ratios of measurements drawing : garden	Value of the ratio
3.	Length		
4.	Width		
5.	Area		

6. Consider the ratio used to create the scale drawing (2 cm : 9 ft), and the ratios found in problems 3 and 4 above. How do the values of these ratios compare?

7. Consider the ratio used to create the scale drawing and the ratio of the areas found in problem 5 above. How do the values of these ratios compare?

## A FLOOR PLAN

Architects often use scale drawings to represent actual building floor plans. Use Ratio Strip 1 to measure some scale drawings of rooms and determine their actual dimensions.

BEDROOM 1		LIVING ROOM		DINING ROOM	   ⊢ width – ⊣ 	
	BATH	BEDROOM 2	JNDRY	KITCHEN	₹ ↓	
CLOSET			IAL		Scale: 2 cm : 9 ft	

	Room	Drawing length	Drawing width	Actual length	Actual width
1.	Bath	cm	cm	ft	ft
2.	Bedroom 2				
3.	Laundry				
4.	Dining Room	3 cm			
5.	Bedroom 1			18 ft	
6.	Living Room				

7. If length and width of the dining room in the scale drawing were increased by 2 cm each, what would be the new actual dimensions of the dining room?

### THE MUSEUM

Here is a scale drawing of a museum floor plan. The floor of the photography room is a square with actual side lengths equal to 22.5 feet.

1. Find the scale of this drawing using a customary ruler in inches, rounding all measurements to the nearest  $\frac{1}{4}$  inch (0.25"). Then write the scale in these three different equivalent ways.

\_\_\_\_\_ in : 22.5 ft 3 in : \_\_\_\_\_ ft 1 in : \_\_\_\_\_ ft

2. Create Ratio Strip 2 below based on your scale.



Use your ratio strip as needed and complete the table.

	Room	Drawing length	Drawing width	Drawing area	Actual length	Actual width	Actual area
3.	Cafe						
4.	Video						
5.	Painting						
6.	Sculpture						
7.	Gift shop						

## **SPORTS PLAYING SURFACES**

You will make scale drawings of sports playing surfaces.

1. Draw a ratio strip or double number line that shows a scale of 3 cm : 20 ft.

#### Determine the dimensions of each sports surface if the scale is 3 cm : 20 ft.

	Sport Surface	Actual Length	Actual Width	Drawing length	Drawing width
2.	Soccer Field	400 ft	300 ft	cm	
3.	Volleyball Court	60 ft	30 ft		
4.	Football Field	360 ft	160 ft		
5.	Roller Rink	70 ft	150 ft		
6.	Bowling Lane	60 ft	3 ft 4 in		

7. Use centimeter graph paper. Choose two of the sports surfaces above and create scale drawings. You may need to tape sheets of graph paper together. You may want to research other features on the internet to include on your scale drawings. Cut them out and label completely.

I made scale drawings for a \_\_\_\_\_\_ and a \_\_\_\_\_.

8. Use your drawings and explain approximately how many copies of your smaller sports surface will fit inside your larger sports surface.

## CIRCUMFERENCE OF CIRCLES

Summary	Goals
We will explore the relationship between a circle's diameter and its circumference. We will learn about historical approximations to $\pi$ . We will use the formula for the circumference of a circle to solve problems.	<ul> <li>Use multiple representations to explore the relationship between the diameter and the circumference of a circle.</li> <li>Understand the formula relating circumference and diameter of a circle.</li> <li>Understand that π is not a rational number, and explore several approximations to π.</li> <li>Solve problems that involve circumferences of circles.</li> </ul>

#### Warmup

1. Explain why each of the following pairs of figures appear to be scaled copies of one another.





2. Explain why each of the following pairs of figures appear **not** to be scaled copies of one another.





- 3. Make up a reasonable scale for the pair of squares in problem 1.
- 4. Make up a reasonable scale for the pair of circles in problem 1.

## **IMPORTANT VOCABULARY**

1. Your teacher will give you directions for drawing several points in relation to the given point. Do not draw line segments.

Use the diagram to the right and the word list below for the following statements.

2.	Points on a circle a	re all equidistant from its	·	A
	In the figure, this po	pint is represented by	·	
3.	A line segment from the circle is called a In the figure, this se	n the center of a circle to a egment is represented by	any point on	
4.	A line segment with In the figure, this se	າ both endpoints on the ci egment is represented by	rcle is called a	
5.	A chord that goes t In the figure, this cl	hrough the center of the one of t	circle is called a	·
		Word	I List	
	center	chord	diameter	radius

## **MEASURIN**G CIRCLES

1. Use the table to record the diameter and circumference of objects measured in class.

Object	Diame <mark>ter</mark> ( <i>d</i> )	Circumference ( <i>C</i> )	C d
Α.			
В.			
C.			
D.			
E.			

- 2. The circumference of a circle is *about* equal to \_\_\_\_\_\_ times the length of the diameter.
- 3. Write an equation to describe the relationship between the circumference (*C*) and the diameter (*d*). Use the symbol "≈" to represent "is about equal to."

Use the relationship from above to estimate the circumference of the following circles.

4. d = 4 cm 5.  $C \approx$  6.  $C \approx$  \_\_\_\_  $C \approx$  \_\_\_\_  $\int 50 \text{ mm}$   $\int 6 \text{ in}$ 

Use the relationship from above to estimate the radius and diameter of the following circles.

7. C = 24 cm  $d \approx \_$   $r \approx \_$   $r \approx \_$   $r \approx \_$  $r \approx \_$ 

## **CIRCUMFERENCE REPRESENTATIONS**

- 1. Your teacher will help you determine which data to transfer into the table to the right.
- 2. Draw horizontal and vertical axes on the graph below. Label and scale the axes. Title the graph.
- 3. Graph the data points and draw a line that best fits the data.
- 4. What does the point (0, 0) represent on this graph?

Diameter (x)	Circumference ( <i>v</i> )

- 5. Estimate the *y*-value when *x* = 1 on your graph. In other words, what is (1, *y*)?
- 6. What does the point (1, *y*) represent on this graph?
- 7. Write an equation that best represents this graph.
- 8. Explain in words what this equation means.
- 9. Explain why each of the following represents a proportional relationship.
  - a. The values in your data table.
  - b. The graph.
  - c. The equation.

<u> </u>					
<u> </u>		 		 	
<u> </u>		 		 	 
<u> </u>					
<u> </u>					
<u> </u>	 				
<u> </u>					

## A LITTLE HISTORY

Many civilizations over the centuries have observed that the ratio of the circumference to the diameter of a circle has a constant value. For example, the Romans observed that the number of paces around the outer portion of their circular temples was about three times the number of paces through the center. In mathematics, the Greek letter pi (written  $\pi$ ) is used to represent this constant. The number  $\pi$  is not rational, that is,  $\pi$  cannot be expressed as a quotient of integers. Here are some approximations to  $\pi$  used by different civilizations over the ages.

Fraction use	d as approximation to $\pi$	Decimal approximation for $\pi$ (to the nearest ten-thousandth)
1. Egyptian:	256 81	
2. Greek:	between $\frac{22}{7}$ and $\frac{223}{71}$	
3. Hindu:	3,927 1,250	
4. Roman:	377 120	
5. Chinese:	355 113	
6. Babylonian:	<u>25</u> 8	

- 7. The decimal approximation to  $\pi$ , correct to five decimal places, is 3.14159.
  - a. Which civilization named above had the best decimal approximation to  $\pi$ ?
  - b. Round this decimal approximation to the nearest hundredth.

If you want to write the exact value of pi, you should use the symbol  $\pi$ . Numerical approximations to  $\pi$ , such as 3.14 or  $\frac{22}{7}$ , are not exact.

- 8. Starting with your equations from the previous pages, now write exact equations for the **circumference of a circle**:
  - a. In terms of d:



C =	

b. In terms of r:

## USING APPROXIMATE VALUES FOR $\pi$

There is no fraction that represents the exact value of  $\pi$ . If an exact solution to a problem is required, leave the symbol  $\pi$  in the solution. However, if the solution is needed for a task for which an approximation will serve, such as for making a measurement with a ruler, you may approximate  $\pi$  to the accuracy required for the application.

Compute the numerical approximations for each measurement that represents the circumference of a circle

	Exact Circumference of a Circle	Approximate <i>C</i> using 3 for π	Approximate C using 3.14 for $\pi$	Approximate C using $\frac{22}{7}$ for $\pi$
1.	$C = 7 \bullet \pi$ $(d = \)$			
2.	C = 28 π (d =)			
3.	C = 1.4 π (d =)			
4.	C = 100 π (d =)			
5.	C = 10 π (d =)			

- 6. The value of 3 for  $\pi$  may be the simplest approximation to  $\pi$ . Why may it not be the "best?"
- 7. Which approximations above were easier to calculate using 3.14 for  $\pi$ ? Explain.
- 8. Which approximations above were easier to calculate using  $\frac{22}{7}$  for  $\pi$ ? Explain.

## **CIRCUMFEREN**CE PROBLEMS

1.	The symbol for pi is				
2.	Common approximations for pi are		 _, and _	·	
3.	Explain what pi means.				
4.	Formulas for the circumference of a circle a	ire	 _ and _	 	_·

Draw a picture, write a formula, and substitute to solve each problem. Use either 3.14 or  $\frac{22}{7}$  for  $\pi$ .

5. <b>The plate problem:</b> Calculate the circumference of a plate with a radius of 14 cm.	6. <b>The can problem:</b> Calculate the diameter of the top of a soup can with a circumference of 32 cm.
a. Sketch	a. Sketch
b. Appropriate formula	b. Appropriate formula
c. Substitute and solve	c. Substitute and solve
d. Solution	d. Solution

7. Explain why neither of the answers you wrote for problems 5 or 6 are exact measurements.

## **CIRCUMFERENCE PROBLEMS** (Continued)

#### Solve.

8.	The earth's orbit problem: The earth is about 93,000,000 miles from the sun, and the earth revolves around the sun one time per year. If the earth's orbit is approximately a circle, how far does the earth travel in one year?	9.	<b>The school track problem:</b> A field at a local school is surrounded by a track. The straightaways are each 425 feet long. The distance across the field (top to bottom in the diagram) is 150 feet. Find the distance around the track.
	a. Sketch		a. Label the figure
			straightaway
			Hint: Think of this field as a combination of two familiar shapes.
	b. Appropriate formula(s)		b. Appropriate formula(s)
	c. Substitute and solve		c. Substitute and solve
	d. Solution		d. Solution

10. Explain why in problems like these it may be preferable to use an approximation to  $\pi$  rather than to leave the answer in terms of  $\pi$ .

# **AREA OF CIRCLES**

Summary	Goals
We will use our knowledge of the area of rectangles and circumference of circles to give an informal derivation of the area formula for a circle. We will use the formula to solve problems.	<ul> <li>Derive the area formula for circles.</li> <li>Solve problems that involve areas of circles.</li> </ul>

#### **War**mup

Suppose the vertical and horizontal length between adjacent dots represents 4 feet.

<ol> <li>Find the area of a 16 foot by 20 foot rectangle. Make a scale drawing of the rectangle.</li> </ol>	2. Find the circumference of a circle with a radius of 8 feet. (Your answer should be exact, with $\pi$ in it.) Make a scale drawing of the circle.

## **DERIVING THE AREA OF A CIRCLE**

- 1. What is the formula for the circumference of a circle in terms of its radius r?
- 2. Your teacher will give you a paper circle and some directions for folding it, cutting it into wedges, and then arranging the wedges into a shape. Space is provided below to tape, glue stick, or sketch the shape.

Use your knowledge of the area of a parallelogram / rectangle, and the circumference of a circle to find the area of this shape.

3. This figure, before folding and cutting, was a \_\_\_\_\_\_, now looks much like a \_\_\_\_\_\_, and the more wedges

you make, the closer it gets to becoming a \_\_\_\_\_

- 4. The "base" of the figure is approximately \_\_\_\_\_\_ of the circle.
- 5. The height of the figure is approximately \_\_\_\_\_\_ of the circle.
- 6. Write an equation for the approximate area of the figure.
- 7. Substitute the expression for the circumference of the circle from problem 1 above into your formula and simplify.
- 8. What is the formula for the area of a circle, in terms of the radius?

#### Area of a Circle

A = \_\_\_\_\_

## **AREA REPRE**SENTATIONS

- 1. Use the formula for the area of a circle to complete the table to the right.
- 2. Draw horizontal and vertical axes on the graph below. Label and scale the axes. Title the graph.
- 3. Graph the data points. How can you tell that a line does not fit the data very well?
- 4. What does the point (0,0) represent on this graph?
- RadiusArea<br/>(y)0 units1 units2 units3 units4 units
- 5. What does the point (1, *y*) represent on this graph?
- 6. Write an equation that best represents this graph.
- 7. Explain in words what this equation means.
- 8. Explain why each of the following does NOT represent a proportional relationship.
  - a. The values in your data table.
  - b. The graph.
  - c. The equation.



## AREA PROBLEMS

Draw a picture, write an appropriate formula, and substitute to solve each problem.

<ol> <li>The dish problem: Find the area of a plate whose diameter is 12 inches.</li> </ol>	2. The water sprinkler problem: A revolving water sprinkler sprays water in a circular fashion to a distance of 20 feet in all directions. What area of grass does it cover?
a. Sketch	a. Sketch
b. Appropriate formula	b. Appropriate formula
c. Substitute and solve	c. Substitute and solve
d. Solution	d. Solution

## **MORE CIRCLE PROBLEMS**

Label the diagrams, write the appropriate formulas, and substitute to solve each problem.

1. The shaded area problem: The largest 2. The school track problem (revisited): A possible circle is to be cut from a square field at a local school is surrounded by a board that is 56 inches on each side. track. Each straightaway is 425 feet. The distance across the field (top to bottom in What is the approximate area, in square the diagram) is 150 feet. Find the area of inches, of the remaining board (shaded the entire field. area)? a. Label the figure. a. Label the figure. \_\_\_\_\_ straightaway \_ b. Appropriate formulas b. Appropriate formulas c. Substitute and solve c. Substitute and solve d. Solution d. Solution

## **MORE CIRCLE PRO**BLEMS (Continued)

- 3. The exact circumference of a circle is  $8\pi$  cm. Find the exact area.
- 4. The exact area of a circle is  $25 \pi$  cm<sup>2</sup>. Find the exact circumference.

7. Find the shaded area of the basketball key to the right.

8. A dartboard is a representation of <u>concentric</u> circles, which are circles that have the same center. The smallest circle (the bullseye) has diameter d = 4 in. Each successive circle has a radius 2 inches greater than the previous one. What fraction of the whole dartboard is the smaller gray ring?





## SKILL BUILDERS, VOCABULARY, AND REVIEW

### SKILL BUILDER 1

- 1. A rectangle has an area of 40.5 square units. One side is half the length of the other side. What is the length of each side?
- 2. The sum of three consecutive even integers is 240. What is each integer?

Compute.			
34(7 – 3) + (-17)	4. 19 – 9(4	– 8) – 21	5. $\frac{-8+3(-4)}{9-11}$

State whether each angle appears to be acute, right, obtuse, or straight. Then use a protractor to find the measure.



8. Daniel bought a shirt for \$10 and sold the shirt for \$18. What was his percent markup?

Solve the equations.

1.	3 <i>x</i> – 8 = -19	2.	$\frac{x}{12}$ + 15	= 13	3.	4(x-9) = 26
4.	3.8 – 5 <i>y</i> = 12.2	5.	$1\frac{3}{4} + 3\frac{3}{2}$	$\frac{1}{2}x = 4\frac{1}{4}$	6.	$5\frac{4}{5} = 3w - 3\frac{1}{10}$

State whether each measure represents an acute, right, straight, or obtuse angle. Then use a protractor to draw the angle. One ray of the angle and the vertex are given.



9. Explain the difference between the diameter and the radius of a circle.

#### Simplify the expressions.

10. 
$$5x - 6(x - y)$$
  
11.  $2(w + 6y) - 4 + 12w - y$ 

 Make a tree diagram or outcome grid to the right to show all possible outcomes of flipping a penny and a nickel. (Use H for heads and T for tails.)

Use the sample space above to find the following probabilities.

2. P(TT)	3. <i>P</i> (TH or HT)	4. <i>P</i> (getting at least one head)

- 5. If you flipped a penny and a nickel 20 times, how many times would you expect both to be tails (TT)?
- 6. Flip a penny and a nickel 20 times and record your results. How many times did get TT? What is your experimental probability for flipping two tails?

By what percent does your estimate in problem 5 deviate from your theoretical expectation?

7. Sameeha surveyed 20 seventh graders in her math class about their favorite sport, and 13 of them said it was football. She concluded that 65% of the seventh graders at her school like football the best. Is her conclusion valid?

Solve the inequalities.

8. 
$$3x - 9 > 15$$
  
9.  $\frac{1}{2} - 2\frac{3}{4}w \le -5$   
10.  $5.6 > 2.4y - 7$ 

Simplify each complex fraction.



5. At a seventh grade dance, the ratio of boys to girls is 5 : 4. There are 65 boys at the dance. How many girls are at the dance?

<ol> <li>Draw an isosceles triangle with two sides of length 2 cm, and a third side that is longer than 3 cm.</li> </ol>	7. Draw a triangle for which one side has length 3 cm, another side has length 4 cm, and the included angle is 110°. What is the length of the third side to the nearest mm?
--	--

Complete the table. Square A is the original drawing, and Squares B, C, and D are reductions or enlargements of A. Use the grid paper below to draw the squares if needed.

	Square	Scale factor	Rewrite the scale factor as a percent value	Enlargement or Reduction?	Length of a side	Area of the square
1.	А	1				
2.	В	2	200%	Enlargement	8 cm	64 sq. cm
3.	С	0.5				
4.	D	$1\frac{1}{2}$				



On a map,  $\frac{1}{4}$  inch represents one mile. Fox, Tiger, and Lion are three cities on the map.

5. If the distance between Fox and Lion is 9 miles, how far apart are Fox and Lion on the map?	<ol> <li>If Tiger and Lion are 3<sup>1</sup>/<sub>2</sub> inches apart on the map, what is the actual distance between Tiger and Lion in miles?</li> </ol>

7. Harper has an 80 in : 1 in scale drawing of the floor plan of her house. On the floor plan, the dimensions of her rectangular living room are  $1\frac{7}{8}$  inches by  $2\frac{1}{4}$  inches. What is the area of her real living room in square feet?

Solve. Use either 3.14 or $\frac{22}{7}$ for $\pi$ below.	
<ol> <li>Approximate the circumference of a plate with a radius of 12 cm.</li> </ol>	<ol> <li>Approximate the diameter of a trash can lid with a circumference of 42 in.</li> </ol>
a. Sketch	a. Sketch
b. Appropriate formula	b. Appropriate formula
c. Substitute and solve	c. Substitute and solve
d. Solution	d. Solution

The city of Atlantic Beach is building a new park. It includes a circular pond that has a circumference of 628 feet.

3. About what is the radius of the pond?	4. The city wants to build a short wall around the pond. The wall must be 1 foot away from the edge of the pond the entire way around. About how long will the wall be? Use 3.14 for $\pi$ .

Use either 3.14 or  $\frac{22}{7}$  for  $\pi$ .

<ol> <li>Find the area of a circle with a radius of 5 cm.</li> </ol>	<ol> <li>Find the area of a circle with a diameter of 22 in.</li> </ol>
3. Find the radius of a circle with an area of 200.96 square feet.	<ol> <li>Find the diameter of a circle with an area of 19.625 square cm.</li> </ol>

5. Frank's Pizza uses 13 inch by 13 inch pizza boxes for medium pizzas. Their medium pizza has a 12 inch diameter. What percent of the bottom of the box will a medium pizza cover?

6. An apple pie has a diameter of 8 inches, and a cherry pie has a radius of 5 inches. Which pie has a greater area and by how much?

7. Maya is building a pool whose shape combines a rectangle and semicircle (shown to the right). Find the area of the pool.

	5 yds	
3 yds		

## FOCUS ON VOCABULARY

Select the word from the word list below that best completes the sentence.

1. The \_\_\_\_\_\_ of a circle is the distance around it.

2. A line segment with both endpoints on the circle is called a \_\_\_\_\_\_.

3. Points on a circle are equidistant from its \_\_\_\_\_.

- 4. A \_\_\_\_\_\_ drawing is a kind of enlargement or reduction of an actual figure.
- 5. To enlarge a figure proportionally, multiply its dimensions by the \_\_\_\_\_\_.
- 6. A line segment from the center of a circle to any point on the circle is called a
- 7. A \_\_\_\_\_\_ is the set of all points in a plane that are a given distance (radius) from a given point (center).
- 8. A chord that goes through the center of a circle is called a \_\_\_\_\_\_.
- 9.  $\frac{22}{7}$  and 3.14 are approximations for \_\_\_\_\_.

	Word List	
circle	radius	diameter
chord	circumference	center
scale factor	рі	scale drawing

### **SELECTED** RESPONSE

Show your work on a separate sheet of paper and select the best answer(s). 1. Each floor of an office building measures 50 ft by 120 ft. On a blueprint, the same floor measures 25 in by 60 in. What is the blueprint scale? A. 2 in : 10 ft B. 1 in : 2 ft C. 10 in : 2 ft D. 1 ft : 2 in 2. A scale drawing of a school was created using a 1.5 cm : 10 ft scale. What actual length is represented by 6 cm on the drawing? A. 0.15 feet B. 15 feet C. 9 feet D. 40 feet 3. Choose all the statements that are true for a circle with a radius of 5 units. The circumference is  $5\pi$  units. Β. The circumference is  $10 \pi$  units. Α. C. The area is  $10\pi$  square units. D. The area is  $25\pi$  square units. Use the circle below to answer problems 4 and 5. d = 5.4 cm 4. What is the area of the circle to the nearest tenth? 8.5 cm<sup>2</sup> 17 cm<sup>2</sup> 22.9 cm<sup>2</sup> 91.7 cm<sup>2</sup> B. C. D. A. 5. What is the circumference of the circle to the nearest tenth? 8.5 cm Β. 17 cm C. 22.9 cm 91.7 cm Α. D. 6. Choose all the statements that are true for all circles. Α. The circumference divided by the Β. If the diameter triples, then the diameter equals  $\pi$ . circumference triples. If the diameter is divided by 2, the D. If the diameter is divided by 2, the C. area is divided by 2. area is divided by 4.

#### KNOWLEDGE CHECK

Show your work on a separate sheet of paper and write your answers on this page.

#### 15.1 Scale Drawings

1. A blueprint of a room is drawn with a scale of  $\frac{1}{2}$  in : 1 ft. The actual length of the room is 16 ft. Find the room's length on the blueprint.

A map is created with a scale of 2 cm : 15 km. Find the actual distance for each map distance.

2. 6 cm

3. 10 mm

#### 15.2 Circumference of Circles

4. Find the circumference of a circle whose radius is 14 meters.

Approximate the measurement using 3 for $\pi$	Approxi measuren 3.14	mate the nent using for $\pi$	Approximate the measurement using $\frac{22}{7}$ for $\pi$

- 5. What is the circumference of a circle with a radius of 3 meters?
- 6. The circumference of a DVD is 28.26 centimeters. What is the diameter?

#### 15.3 Area of Circles

- 7. Find the area of a circle with a radius of 12 km.
- 8. The area of a circle is 50.24 sq. cm. What is the radius of the circle?
- 9. Explain which has a greater area, a circle with radius of 3 meters or a square with a side length of 3 meters.

## **HOME-SCHOOL** CONNECTION

Here are some problems to review with your young mathematician.

- 1. To make a scale drawing of your bedroom on an  $8\frac{1}{2}$  in  $\times$  11 in sheet of paper, what might be an appropriate scale? Be sure to include units of measure.
- 2. Explain what pi means (do not simply write a number for it). Draw a diagram that helps support your explanation.

- 3. Each of Diana's dinner plates has a diameter of 14 inches.
  - a. Find the circumference and the area of her plates.

b. Diana wants to order salad plates that are half the area of the dinner plate. She orders salad plates that have a diameter of 7 inches. Did she order the right size? Explain.

## **COMMON CORE STATE STANDARDS – MATHEMATICS**

#### STANDARDS FOR MATHEMATICAL CONTENT

- 7.NS.A Apply and extend previous understandings of multiply, and divide rational numbers.
- 7.NS.3 Solve real-world and mathematical problems involving the four operations with rational numbers.
- 7.EE.A Use properties of operations to generate equivalent expressions.
- 7.EE.2 Understand that rewriting an expression in different forms in a problem context can shed light on the problem and how the quantities in it are related. For example, a + 0.05a = 1.05a means that "increase by 5%" is the same as "multiply by 1.05."
- 7.G.A Draw, construct and describe geometrical figures and describe the relationships between them.
- 7.G.1 Solve problems involving scale drawings of geometric figures, including computing actual lengths and areas from a scale drawing and reproducing a scale drawing at a different scale.
- 7.G.B Solve real-life and mathematical problems involving angle measure, area, surface area, and volume.
- 7.G.4 Know the formulas for the area and circumference of a circle and use them to solve problems; give an informal derivation of the relationship between the circumference and area of a circle.
- 7.G.6 Solve real-world and mathematical problems involving area, volume and surface area of two- and three-dimensional objects composed of triangles, quadrilaterals, polygons, cubes, and right prisms.

#### STANDARDS FOR MATHEMATICAL PRACTICE

- MP2 Reason abstractly and quantitatively.
- MP5 Use appropriate tools strategically.

MP6 Attend to precision.



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