## Alge-Grid: What's the $\boldsymbol{a}$ ?

 Carole Greenes and Tanner Wolfram

## Prime Group@2021

# Alge-Grid: What's the $\boldsymbol{a}$ ? 

## Carole Greenes <br> Tanner Wolfram

Alge-Grid puzzles are designed to enhance solvers' algebraic reasoning talents. In each puzzle, a 3-by-3 grid with nine cells is presented. Each cell contains an algebraic expression containing one unknown, the $a$. In each puzzle, the value of $a$ is the same. To solve each puzzle and fill in the values of the nine expressions in the grid, the value of that $a$ must be determined first. To assist solvers, a Clue is presented for each grid. The Clue provides information about the numbers in three of the cells. Those three cell clues are connected along a side or corner, relating to their position (not always obvious!) in the grid. Clue information may be mathematical (e.g., a perfect number; number of sides on a heptagon); or relate to sports (e.g., number of members on a soccer team); the sciences (e.g., number of eyes on a cyclops); history (e.g., number of world wars); geography (e.g., number of great lakes); or the arts (e.g., number of sharps in a specific musical scale). The goal for solvers is to determine the value of the $a$ and complete the grid to include the given numbers.

Set 1 , problems $1-18$, $a$ can be any number $1-9$, and all cells contain the numbers $1-9$.
Set 2, problems $19-36$, $a$ can be any number $10-18$, and all cells contain the numbers $10-18$.
Set 3, problems $37-54$, $a$ can be any number $19-27$, and all cells contain the numbers $19-27$.
Solutions are presented after the last problem.
Note: The use of calculators for obtaining information, as well as computing, is recommended. The focus of the problems is on reasoning, not on the memorization of facts.

Have fun!!
Carole and Tanner


Carole Greenes, Ed.D. is Professor Emerita, Mathematics Education at Arizona State University. While at ASU, she served as Associate Vice President for STEM Education, Dean of the School of Educational Innovation and Teacher Preparation, Director of the Practice Research and Innovation in Mathematics Education (PRIME) Center, Director of the Vertically Integrated Projects program that provides research experiences for undergraduate students, and Professor of Mathematics Education in the Ira A. Fulton Schools of Engineering and the College of Liberal Arts and Sciences. Currently, she directs the PRIME Group that develops books of challenge problems for students, grades $\mathrm{K}-12$. Carole is author of more than 350 books for students, PreK-12 and college, and teachers; 81 articles; six mathematical musicals; and two histories of mathematics in story and song. She served as editor of the Arizona Association of Teachers of Mathematics journal, OnCore, and author of the online monthly free MATHgazine Senior (grades 8-12), MATHgazine Junior (grades 5-8), MATHgazine Elementary (grades 3-5) and MATHgazine Primary (grades K-2). In 2003, Greenes was inducted into the Massachusetts Mathematics Educators' Hall of Fame. In 2011, she received the NCSM Ross Taylor/Glenn Gilbert National Leadership Award in Mathematics Education. In 2016, she received the Copper Apple Award for Leadership in Mathematics in Arizona, and in 2018 she received the National Council of Teachers of Mathematics Lifetime Achievement Award.

Tanner Wolfram is a Fall 2019 graduate, Summa cum Laude, of Barrett, The Honors College at Arizona State University. He holds a major in Physics and minors in both Spanish and Chinese. Tanner is the co-author of Alge-Grid: What's the a? puzzle book, and senior author of the Facasumi Puzzle Book. From Spring 2016 to Fall 2020, Tanner served as a Senior Project Assistant in the Practice, Research, and Innovation in Mathematics Education (PRIME) Center/Group at ASU. During his time with the PRIME Group/Center, Tanner assisted with the NSF-funded Project App Maker Pro (AMP), edited and contributed to eight MATHadazzle Puzzle Books, co-authored six articles in Math Education, co-edited two free monthly AATM MATHgazines, and additionally co-edited the AATM Journal for two semesters.

Set 1
Possible $a$ values: 1 - 9

## Alge-Grid 1

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $(\sqrt{a})^{2}$ | $(a+1)^{2}-6$ | $a \div a$ |
| :---: | :---: | :---: |
| $a^{3}-2$ | $5 a \div 2$ | $(a \div 2)^{3}+6$ |
| $a^{2}-a+2$ | $a+6$ | $a^{3}+1$ |

## Clue



## Alge-Grid 2

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $(a+1) \div 4$ | $a+1$ | $a-1$ |
| :---: | :---: | :---: |
| $(a+3) \div 2$ | $(a+1) \div 2$ | $(a-1) \div 2$ |
| $(4 a)^{0}$ | $a+2$ | $2 a-7$ |

Clue

|  | Number of <br> planets in the <br> solar system |
| :--- | :--- |
|  | Even square <br> number |
| Number of <br> wheels on a <br> unicycle |  |

## Alge-Grid 3

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a^{8}+a^{7}$ | $2 a^{6}+a^{5}+a^{4}+2$ | $a+3$ |
| :---: | :---: | :---: |
| $3 \sqrt{a}$ | $8 a$ | $a \div 4+6.75$ |
| $(a+9) \div 2$ | $a \div a \times 1$ | $a \div a^{2}+8$ |

## Clue

| Number of <br> cups in a pint |  |
| :--- | :--- |
|  | Number of <br> arms on an <br> octopus |
| Number of <br> toes on each <br> foot |  |

## Alge-Grid 4

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $\frac{3}{4} a+0.5$ | $a^{2}$ | $(a+1)^{2}$ |
| :---: | :---: | :---: |
| $3 a$ | $a^{0}$ | $a^{2}-1$ |
| $a^{2}+1$ | $a^{2}+2 a-1$ | $a^{3}$ |

Clue

| Perfect <br> number | Factor of all <br> numbers |  |
| :--- | :--- | :--- |
|  |  |  |

## Alge-Grid 5

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a+3$ | $[9(a-1)]^{1 / 3}$ | $\sqrt{a}-1$ |
| :---: | :---: | :---: |
| $a \times a^{0}$ | $(a-1)^{2}$ | $a^{2}-2 a-2$ |
| $\frac{1}{2} a$ | $(a-2)^{3}$ | $a+1$ |

Clue

|  | Number of <br> primary <br> colors |
| :--- | :--- |
|  | Greatest <br> single-digit <br> number |
| Number of <br> brain <br> hemispheres |  |

## Alge-Grid 6

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a^{2}-8 a-2$ | $\sqrt{a}+(a \div 3)$ | $a \times(a \div 9)$ |
| :---: | :---: | :---: |
| $a^{0}+(a \div 3)-3$ | $a-5$ | $(a-8)^{2}+4$ |
| $8 a \div 9$ | $(a+1) \div 2-3$ | $a \div 3$ |

## Clue

| Number of red <br> stripes on U.S. <br> flag |  |
| :--- | :--- |
|  | Smallest <br> composite <br> number |
|  | Even prime |
|  |  |

## Alge-Grid 7

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $6 a$ | $(a+1)^{3}$ | $(a+2)^{2}$ |
| :---: | :---: | :---: |
| $a \times a^{2} \times a^{3}$ | $10 a \div 2$ | $2 a$ |
| $(a+1)^{2}$ | $2 a+1$ | $(a+2)^{2}-2$ |

## Clue

| Product of two <br> different <br> prime <br> numbers | Number of <br> faces on an <br> octahedron |
| :--- | :--- |
|  | Third prime <br> number |
|  |  |

## Alge-Grid 8

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a^{3}-\mathrm{a}^{2}-5 a+2$ | $a^{2}$ | $2 a$ |
| :---: | :---: | :---: |
| $a-2$ | $a^{0}+1$ | $(a+3)^{2}-32$ |
| $2 a+2$ | $a^{2}-2$ | $3 a \div 3$ |

Clue

| Third square <br> number |  |
| :--- | :--- |
| Odd number |  |

## Alge-Grid 9

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a+2$ | $\sqrt{a+3}-1$ | $a \div 2$ |
| :---: | :---: | :---: |
| $a-1$ | $a+1$ | $a^{2}-27$ |
| $(a-4)^{2}$ | $a^{2}-30$ | $a^{0} \times \frac{1}{6} a$ |

Clue

| Number of <br> musicians in <br> an octet | Number of <br> feet in a yard |  |
| :--- | :--- | :--- |
|  | Number of <br> Ancient <br> Wonders of <br> the World |  |
|  |  |  |

## Alge-Grid 10

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a \div a+(3 a \div a)$ | $2 a-a \div 5$ | $a+3$ |
| :---: | :---: | :---: |
| $a+2$ | $\sqrt{a+4}-1$ | $2 a-4$ |
| $a-4$ | $(a-2)^{2}-4$ | $a^{2}-4 a-2$ |
|  |  |  |

Clue

|  | Number of <br> letters in the <br> word <br> "kindness" |
| :--- | :--- |
| Number of <br> continents | Number of <br> wheels on a <br> bicycle |

## Alge-Grid 11

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $\sqrt{a+8}-1$ | $(a \div 4)^{3}$ | $a \div 2$ |
| :---: | :---: | :---: |
| $(a-5)^{2}$ | $a^{2}-7 a-1$ | $a-2$ |
| $\sqrt[3]{a}$ | $a \div a+4$ | $a^{0}$ |

## Clue

| Sixth <br> Fibonacci <br> number | Number of <br> points on a <br> compass |
| :--- | :--- |
|  | Half dozen |
|  |  |
|  |  |

## Alge-Grid 12

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $\sqrt{a}-1$ | $a \div 2+6$ | $a+5$ |
| :---: | :---: | :---: |
| $\left(a^{3}-a^{2}\right) \div 12+2$ | $a^{2} \div 4-1$ | $a^{2}-3 a$ |
| $2 a-1$ | $\sqrt{a}$ | $a+1$ |

## Clue

| Fourth prime <br> number | Factor of all <br> even numbers | Roman <br> numeral is V |
| :--- | :--- | :--- |

## Alge-Grid 13

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $\left(\frac{1}{3} a\right)^{3}$ | $a \div a$ | $2(a+1)-a-1$ |
| :---: | :---: | :---: |
| $\frac{1}{3} a$ | $\frac{1}{2} a$ | $a+\frac{1}{2} a$ |
| $2 \times \frac{1}{3} a$ | $2 a-7$ | $a \times a^{0}$ |

## Clue

| Base of <br> Binary <br> System | Number of <br> sharps in A <br> Major |
| :--- | :--- |
|  | Sum of two <br> different <br> prime <br> numbers |
|  |  |

## Alge-Grid 14

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a^{1 / 3}$ | $2 a-(a+1)$ | $3 a \div 4$ |
| :---: | :---: | :---: |
| $(a-2) \div 2$ | $a^{3} \div a^{2}$ | $(5 a)^{0}$ |
| $\frac{1}{2} a$ | $2 a-(a-1)$ | $40 \div a$ |

Clue

| Number of <br> miles in a <br> League | Number of <br> musical notes <br> in an octave |
| :--- | :--- |
|  | Sum of digits <br> of any <br> multiple of <br> this number is <br> this number |

## Alge-Grid 15

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a^{2} \div 5 a$ | $2 a-3$ | $(a-2)^{2}$ |
| :---: | :---: | :---: |
| $a^{4} \div a^{3}$ | $(a+1) \div 3$ | $a+1$ |
| $a-2$ | $2 a-2$ | $[2(a+1)] \div 3$ |

Clue

|  | Square of an <br> odd prime <br> number |
| :--- | :--- |
|  | Number faces <br> on a cube |
| Number of <br> pints in a <br> gallon |  |

## Alge-Grid 16

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a^{2} \div 7$ | $a-4$ | $6 a^{0}$ |
| :---: | :---: | :---: |
| $a^{2} \div a+2$ | $9 a-7 a-13$ | $(a-5)^{2}+a-3$ |
| $\sqrt[3]{a+1}$ | $(a+1) \div 2+1$ | $a-3$ |

## Clue

| Sum of the <br> first two <br> counting <br> numbers |
| :--- |
| $a \times 0+1$ |
|  |
| Number of <br> players on the <br> court for each <br> team in <br> basketball |

## Alge-Grid 17

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $3 a-4$ | $a^{2} \div 3$ | $2 a$ |
| :---: | :---: | :---: |
| $2^{a}$ | $a^{2}-2$ | $a^{2}-(a+2)$ |
| $a \div a$ | $a^{2}$ | $2 a-4$ |

Clue

|  | Smallest <br> perfect <br> number |  |
| :--- | :--- | :--- |
| Second cubic <br> number | $2^{3}-1$ |  |

## Alge-Grid 18

Use the clue and the grid to fill in numbers, 1-9. The letter $a$ represents the same number.

| $a^{1 / 2}$ | $(a+1) \div 2$ | $\left(\frac{1}{3} a\right)^{2}$ |
| :---: | :---: | :---: |
| $a-2$ | $(a+1) \div 5$ | $2 a-10$ |
| $\sqrt{a}-2$ | $\frac{2}{3} a$ | $(a-1) \div 2$ |

Clue

|  | Number of <br> Beethoven <br> symphonies |
| :--- | :--- |
| Number of <br> sides on a <br> heptagon | Number of <br> moons on <br> Mars |

# Alge-Grid: What's the $a$ ? 

## Set 2

Possible $a$ values: 10 - 18

## Alge-Grid 19

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $\sqrt{a+8}+5$ | $3 a-2 a-4$ | $(a-8)^{2}-70$ |
| :---: | :---: | :---: |
| $2(a-9)$ | $a-5$ | $(a-15)^{3}+9$ |
| $a-2$ | $(a+3) \div 2+4$ | $a+1$ |

## Clue

| Even number |  |  |
| :--- | :--- | :--- |
|  | Number of <br> inches in a <br> foot |  |
|  |  | Twice the <br> greatest <br> single-digit <br> square <br> number |

## Alge-Grid 20

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $2 a-19$ | $a-2$ | $2 a-14$ |
| :---: | :---: | :---: |
| $2(a+1)-15$ | $\frac{4}{5} a$ | $\frac{2}{3} a$ |
| $a^{2} \div 5 \div 3$ | $\frac{1}{3} a+9$ | $\frac{1}{5} a \times 6$ |

## Clue

| Triangular <br> number | Sum of first <br> three square <br> numbers | Number of <br> holes on a golf <br> course |
| :--- | :--- | :--- |

## Alge-Grid 21

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $\frac{1}{3} a+9$ | $\sqrt{a+4}+a+1$ | $\frac{1}{3} a+(a-10)^{3}$ |
| :---: | :---: | :---: |
| $\frac{1}{4} a+a$ | $(a-8)^{2}-2$ | $\frac{5}{6} a$ |
| $a+4$ | $a-a^{0}$ | $\frac{3}{2} a$ |

Clue


## Alge-Grid 22

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $a^{3} \div a^{2}$ | $a+1$ | $(a+7) \div 2$ |
| :---: | :---: | :---: |
| $(2 a-2) \div 2$ | $2(a-4)$ | $a-2$ |
| $\frac{3}{2}(a-3)$ | $a+4$ | $2 a-10$ |

Clue

| Greatest <br> number with a <br> one-syllable <br> name | Reverse its <br> digits and get <br> the same <br> number |  |
| :--- | :--- | :--- |
|  | XVII in <br> Roman <br> numerals |  |

## Alge-Grid 23

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $3(a-4)$ | $a+\frac{1}{10} a$ | $2 a-3$ |
| :---: | :---: | :---: |
| $2 a-7$ | $a^{2} \div a$ | $a+0.4 a$ |
| $1.2 a$ | $a^{2}-(10-1)^{2}-3$ | $3 a \div 2$ |

Clue

|  | Smallest two- <br> digit prime <br> number |
| :--- | :--- |
| Smallest <br> Emirp <br> number | Sum of first <br> three prime <br> numbers |

## Alge-Grid 24

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $4 a-2 a-6$ | $a^{4} \div a^{2}-10 a$ | $(a-8)^{3}-(a-2)$ |
| :---: | :---: | :---: |
| $10 a^{0}$ | $3(\sqrt{a+5}+1)$ | $a+3$ |
| $\sqrt{a-7}+a$ | $a^{2}-9 a-5$ | $a+1$ |

Clue

|  |  | Number of months in 1 1/2 years |
| :---: | :---: | :---: |
|  | Number of players on a rugby team |  |
| Sum of its digits is the second square number |  |  |

## Alge-Grid 25

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $(a+6) \div 2$ | $\frac{5}{6} a$ | $2 \sqrt{a+7}$ |
| :---: | :---: | :---: |
| $18 a^{0}$ | $a-5$ | $a-7$ |
| $\frac{8}{9} a$ | $\frac{1}{9} a+15$ | $\frac{21}{27} a$ |

## Clue

| Number of <br> pairs of ribs in <br> a human | Triangular <br> number |
| :--- | :--- |
|  | Multiples of <br> this number <br> produce two <br> like numbers |

## Alge-Grid 26

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $2 a-17$ | $a+\frac{1}{8} a$ | $a+1$ |
| :---: | :---: | :---: |
| $\frac{7}{8} a$ | $3 \sqrt{a}-1$ | $(a+4) \div 2$ |
| $\frac{1}{2} a+5$ | $16^{1 / 4} \times \frac{1}{2} a$ | $0.75 a$ |

Clue

|  | Seventh prime <br> number |
| :---: | :--- |
| $1 / 2$ dozen +5 | Sum of first <br> four counting <br> numbers |

## Alge-Grid 27

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $a+4$ | $\frac{1}{2} a+\frac{1}{7} a+2$ | $2 a-12$ |
| :---: | :---: | :---: |
| $a+3$ | $a^{2}-12 a-18 a^{0}$ | $6 \times \frac{1}{7} a$ |
| $(a-13)^{2}+a-1$ | $\frac{1}{2} a+6$ | $a+1$ |

Clue

| Least two- <br> digit number |  |
| :--- | :--- |
| Sixth prime <br> number | Number of <br> minutes in $1 / 4$ <br> hour |

## Alge-Grid 28

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $a-5$ | $(a+13) \div 2$ | $2(a-10)$ |
| :---: | :---: | :---: |
| $a \times(2 a)^{0}$ | $a-4$ | $(a+3) \div 2$ |
| $a+1$ | $3 a-40$ | $a-1$ |

## Clue

| Number of <br> weeks in each <br> season of the <br> year | Deficient <br> number |
| :--- | :--- |
|  | Square <br> number |

## Alge-Grid 29

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $a+\frac{1}{7} a$ | $2 a-10$ | $a+a^{0}$ |
| :---: | :---: | :---: |
| $a-a^{0}$ | $3 a-5^{2}-3$ | $a-3$ |
| $a \div 2+10$ | $3 a-30$ | $2 a-18$ |

Clue

|  | Reverse its <br> digits and get <br> a multiple of 9 |
| :--- | :--- |
| Sum of two <br> square <br> numbers |  |

## Alge-Grid 30

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $(3 a-1) \div 2$ | $3 a-20$ | $a+4$ |
| :---: | :---: | :---: |
| $a \times\left(a^{2}\right)^{0}$ | $(2 a+2) \div 2$ | $2 a-5$ |
| $3 a-19$ | $a+[(a+3) \div 2]$ | $a-a^{0}$ |

## Clue

| Number of <br> hearts in a <br> deck of cards | Product of two <br> odd prime <br> numbers |
| :--- | :--- |
|  | Sum of first <br> four prime <br> numbers |

## Alge-Grid 31

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $\frac{5}{6} a+\frac{1}{6} a$ | $\frac{1}{3} a+11$ | $\sqrt{a+1}+6$ |
| :---: | :---: | :---: |
| $a-2$ | $3 \sqrt{a+10}-1$ | $\frac{2}{3} a+a^{0}$ |
| $\frac{3}{5} a+8$ | $2(a-12)^{2}$ | $4 a \div 3-8$ |

## Clue

| Smallest <br> number with <br> exactly five <br> factors |  |
| :--- | :--- |
|  | Reversing its <br> digits <br> produces the <br> same number |
| Abundant <br> number |  |

## Alge-Grid 32

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $(a-14)^{2}+12$ | $3(a+4) \div 4$ | $a-5$ |
| :---: | :---: | :---: |
| $1.125 a$ | $3 \sqrt{a}$ | $\frac{1}{8} a+a-4$ |
| $a+1$ | $4 \sqrt{a}-3$ | $2(a-6)-10$ |

Clue

| Roman <br> numeral is XII |  |
| :--- | :--- |
| Fibonacci <br> number | Triangular <br> number |

## Alge-Grid 33

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $2 a-10$ | $a+a^{0}$ | $a^{2} \div a^{1} \div a^{0}$ |
| :---: | :---: | :---: |
| $a+\frac{1}{4} a$ | $(2 a+10) \div 2$ | $a+\frac{1}{2} a$ |
| $2 a-14$ | $a-a^{0}$ | $a+\frac{1}{3} a$ |

## Clue

| Smallest <br> number with <br> exactly six <br> factors |
| :--- |
| Each of its <br> digits is a <br> cubic number |
| Double a cubic <br> number |

## Alge-Grid 34

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $3 a-40$ | $a-1$ | $2(a-15)^{2}$ |
| :---: | :---: | :---: |
| $\frac{1}{2} a+6$ | $\frac{2}{3} a$ | $(a+2) \div 2$ |
| $a-\frac{1}{9} a$ | $a^{0} \times \sqrt{169}$ | $a+3-10$ |

Clue

| Product of its <br> digits is a <br> prime number |
| :--- |
| Smallest <br> abundant <br> number |
| Fibonacci <br> number |

## Alge-Grid 35

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $a+4$ | $9 a-8 a+3$ | $3(a-8)$ |
| :---: | :---: | :---: |
| $3(a-9)$ | $(a-15)^{2}+a+1$ | $0.5(a+1)+3$ |
| $a-2$ | $(a-12)^{22}+12$ | $a+1$ |

## Clue

| Haiku has this <br> number of <br> syllables |  |
| :--- | :--- |
| Composite <br> number | Number of <br> inches in $1 / 2$ <br> yard |

## Alge-Grid 36

Use the clue and the grid to fill in numbers, 10-18. The letter $a$ represents the same number.

| $(a-7)^{2}+3$ | $a+a^{0}$ | $2 a-3 a^{0}$ |
| :---: | :---: | :---: |
| $a^{2} / a+\frac{1}{5} a-2$ | $\frac{3}{2} a$ | $2 a-2$ |
| $\frac{1}{5} a+14$ | $a+4$ | $\frac{1}{5} a+11$ |

Clue

| $10^{1}$ |  |
| :--- | :--- |
| Double a cubic <br> number | Multiple of 7 |

# Alge-Grid: What's the $\boldsymbol{a}$ ? 

 Set 3Possible $a$ values: 19-27

## Alge-Grid 37

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $\frac{8}{9} a-3 a^{0}$ | $(a-22)^{2}-3$ | $a-a / a$ |
| :---: | :---: | :---: |
| $4 \sqrt{a-2}+4$ | $\frac{1}{3} a+\frac{2}{9} a+5$ | $a-8$ |
| $(a-23)^{2}+11$ | $a-4$ | $25 \sqrt{a-26}$ |

## Clue



## Alge-Grid 38

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $\frac{2}{3} a+6$ | $\frac{1}{2} a+11$ | $\sqrt{a+25}+20$ |
| :---: | :---: | :---: |
| $\frac{1}{3} a+13$ | $(a-19)^{2}-6$ | $\frac{3}{4} a+\frac{3}{12} a+1$ |
| $a+2$ | $\frac{4}{6} a+8$ | $(a-20)^{2}+4$ |

Clue

|  | XXVII in <br> Roman <br> numerals |
| :--- | :--- |
|  | Prime number |

## Alge-Grid 39

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $\frac{4}{5} a$ | $3 \sqrt{a}+4$ | $a^{1 / 2} \times 4+1$ |
| :---: | :---: | :---: |
| $3(a \div 5+4)$ | $3(\sqrt{a}+3)$ | $5(a \div 5)$ |
| $4 \sqrt{a}+3$ | $a-\frac{1}{5} a+6$ | $a \div 5+17$ |

## Clue

| Sum of its <br> digits is a <br> square <br> number | Sum of two <br> consecutive |
| :--- | :--- | :--- |
| square |  |
| numbers |  |$|$| Only number |
| :--- | :--- |
| between a |
| square |
| number and a |
| cubic number |$\quad$.

## Alge-Grid 40

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $\frac{12}{3}(a-15)$ | $\frac{3}{7} a+4^{2}+1$ | $20(a-20)^{2}+2$ |
| :---: | :---: | :---: |
| $(a-19)^{2}+19$ | $\frac{3}{7} a+12$ | $a+6$ |
| $a-2$ | $\frac{1}{7} a+3^{3}-5$ | $4 \sqrt{a+4}$ |

Clue
2/3 yard in inches

Digits differ by 1

Product of its
digits is a
multiple of 3

## Alge-Grid 41

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $(a-17)^{4}+9$ | $(a+1) \div 4+15$ | $a+7$ |
| :---: | :---: | :---: |
| $12 \times(a-3) \div 8$ | $(a-17)^{5}-9$ | $\sqrt{a+17}+15$ |
| $27 a^{0}$ | $19(a-18)$ | $a+3$ |

Clue

|  | Product of two <br> primes |
| :--- | :--- |
| XIX in Roman <br> numerals | $3^{3}$ minus <br> number of <br> fingers on one <br> hand |

## Alge-Grid 42

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $\frac{1}{13} a+\sqrt{441}$ | $a-1$ | $(a-24)^{4}+3$ |
| :---: | :---: | :---: |
| $\frac{7}{13} a+\sqrt{64}$ | $(a-20)^{2}-12$ | $a-5$ |
| $a+1$ | $(a-24)^{4}+\frac{2}{13} a$ | $(a-24)^{3}+\frac{9}{13} a$ |

## Clue

| 3/4 yard in <br> inches | Product of a <br> square <br> number and a <br> prime number | Number of <br> letters in the <br> alphabet |
| :--- | :--- | :--- |

## Alge-Grid 43

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $a \div 2+10$ | $a \div 4+20$ | $a-4+\sqrt{a+1}$ |
| :---: | :---: | :---: |
| $2 a \div 6 \times 3$ | $(a+14) \div 2$ | $\frac{5}{6} a$ |
| $\frac{3}{4} a+3 \times a^{0}$ | $a-1$ | $a \div 8 \times 9$ |

Clue

| Eighth prime <br> number |  |
| :--- | :--- |
| Sum of its <br> digits is a <br> prime number |  |

## Alge-Grid 44

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $\frac{1}{2} a+6$ | $(a+2) \div 2+\frac{1}{2} a$ | $a-3$ |
| :---: | :---: | :---: |
| $\frac{10}{13} a$ | $2 a-26$ | $a-24 \div 2+10$ |
| $\frac{1}{2} a+12$ | $\frac{14}{13} a$ | $\frac{7}{9}(a+1)$ |

Clue
Product of its digits is a perfect number

Number of ribs in the human body

Multiple of 3

## Alge-Grid 45

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $(a-22)^{2}+13$ | $\frac{1}{5} a+\sqrt{20^{2}}$ | $\frac{1}{5} a+4^{2}$ |
| :---: | :---: | :---: |
| $\sqrt{a+75}+9$ | $a-1$ | $\frac{4}{5} a+6$ |
| $\frac{3}{5} a+12$ | $\frac{2}{5} a+\frac{1}{5} a+5$ | $\sqrt{a+144}+10$ |

## Clue

| Product of its <br> digits is a <br> square <br> number | 2 dozen + 1 |
| :--- | :--- |
| $\sqrt{144}+\sqrt{49}$ |  |
|  |  |
|  |  |

## Alge-Grid 46

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $(a+3) \div 10 \times 9$ | $0.9 a-1.3$ | $a-1$ |
| :---: | :---: | :---: |
| $a+1-6$ | $(a+3) \div 2+5$ | $a-\frac{1}{9} a$ |
| $\frac{5}{6}(a+3)$ | $a \div 3+10$ | $\frac{7}{9} a$ |

## Clue

| Palindromic <br> number | Number of <br> faces on an <br> icosahedron |
| :--- | :--- |
|  | Sum of its <br> digits is a <br> multiple of 10 |
|  |  |

## Alge-Grid 47

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $a^{0} \times \sqrt{484}$ | $a-2$ | $\frac{1}{7} a \times 9$ |
| :---: | :---: | :---: |
| $a+2^{2}$ | $a+2$ | $2 a-(a-3)$ |
| $6 a-100$ | $\frac{1}{7} a+18$ | $\sqrt{a+4}+15$ |

## Clue

| Double an <br> Emirp <br> number | Triangular <br> number | Sum of its <br> digits is a <br> factor of it |
| :--- | :--- | :--- |

## Alge-Grid 48

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $2 \times(3 a \div 5)$ | $a+6$ | $\frac{1}{4} a+16$ |
| :---: | :---: | :---: |
| $\frac{1}{4} a+18$ | $\sqrt{30 a+25}-3$ | $\frac{5}{4} a$ |
| $(a-15)^{2}+2$ | $5 \sqrt{a-4}$ | $(a-16)^{2}+3$ |

## Clue

| Sum of its <br> digits is a <br> square <br> number |  |
| :--- | :--- |
| Sum of its <br> digits is a <br> prime number | Reverse its <br> digits and get <br> a multiple of 7 |

## Alge-Grid 49

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $a^{2}-(a-1)^{2}-18$ | $a+8$ | $44 \div(a-17)$ |
| :---: | :---: | :---: |
| $a+125^{1 / 3}$ | $2 a-18$ | $(a+6)+9^{0}$ |
| $(a+1) \div 2+13$ | $\left[(a+6)^{2}\right]^{1 / 2}$ | $a+2$ |

## Clue

| Number of <br> carats in <br> $100 \%$ gold | Product of a <br> prime number <br> and the square <br> of a prime <br> number |
| :--- | :--- |
| Reverse its <br> digits and get <br> a power of 2 |  |

## Alge-Grid 50

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $3 \sqrt{a+42}-2$ | $a+5$ | $6 a \div 11+7$ |
| :---: | :---: | :---: |
| $3 \times(a \div 11)^{3}$ | $(a-16)^{2}-11$ | $5 a \div 11+16$ |
| $24 \times(a-21)^{10}-1$ | $a-2$ | $3 a \div 11+15$ |

## Clue

| Width of a <br> tennis court in <br> feet | Product of its <br> digits equals <br> the number of <br> months in a <br> year |
| :--- | :--- |
|  | Multiple of 7 |

## Alge-Grid 51

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $a-3$ | $(a-20)^{3}-1$ | $a+1$ |
| :---: | :---: | :---: |
| $(a-19)^{2}+6$ | $a-2$ | $a+4$ |
| $\sqrt{602+a}$ | $[5(a+1)] \div 6-1$ | $6 \sqrt{a-7}-1$ |

Clue

| Fibonacci <br> number |  |
| :--- | :--- |
| XXV in <br> Roman <br> numerals |  |

## Alge-Grid 52

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $\frac{1}{2} a+11$ | $\frac{1}{4} a+a$ | $\frac{3}{4} a+8$ |
| :---: | :---: | :---: |
| $a+a^{0}+a^{0}$ | $2 a-13$ | $a-\frac{2}{40} a$ |
| $1.3 a$ | $\frac{4}{5} a+4$ | $\frac{1}{5} a+20$ |

Clue

|  | Cubic number |
| :--- | :--- |
| Sum of its <br> digits is a <br> cubic number | Product of a <br> prime number <br> and a square <br> number |

## Alge-Grid 53

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $18+\sqrt{a+2}$ | $5 \sqrt{a+2}$ | $a+[(a+1) \div 6]$ |
| :---: | :---: | :---: |
| $a^{2}-(a-1)^{2}-23$ | $2 a-20$ | $a-2$ |
| $4[(a+2) \div 5]$ | $a+1$ | $25-[(a+1) \div 4]$ |

Clue

|  | Difference <br> between digits <br> is a square <br> number |
| :--- | :--- |
| Multiple of 1, <br> $2,4,5$ <br> and 10 |  |

## Alge-Grid 54

Use the clue and the grid to fill in numbers, 19-27. The letter $a$ represents the same number.

| $\frac{1}{2} a+3 \times 5$ | $a^{1}+a^{0}$ | $\left(a^{2}+3 \times 47\right)^{1 / 2}$ |
| :---: | :---: | :---: |
| $\left(a^{2}-84\right)^{1 / 2}$ | $2 a-20$ | $\frac{1}{2} a \times a^{0} \times 2$ |
| $\frac{1}{2} a+[(a+2) \div 3]$ | $a-1$ | $\frac{1}{2} a+a-6$ |

## Clue

$1 / 4$ number of years in a century

When divided by 7 , gives $\pi$

Number of small cubes in a Rubik's cube

## Alge-Grid Solutions

Alge-Grid 1 Solution
$a=2$

| 2 | 3 | 1 |
| :--- | :--- | :--- |
| 6 | 5 | 7 |
| 4 | 8 | 9 |

Alge-Grid 3 Solution
$a=1$

| 2 | 6 | 4 |
| :--- | :--- | :--- |
| 3 | 8 | 7 |
| 5 | 1 | 9 |

Alge-Grid 5 Solution
$a=4$

| 7 | 3 | 1 |
| :--- | :--- | :--- |
| 4 | 9 | 6 |
| 2 | 8 | 5 |

Alge-Grid 2 Solution
$a=7$

| 2 | 8 | 6 |
| :---: | :---: | :---: |
| 5 | 4 | 3 |
| 1 | 9 | 7 |

Alge-Grid 4 Solution
$a=2$

| 2 | 4 | 9 |
| :--- | :--- | :--- |
| 6 | 1 | 3 |
| 5 | 7 | 8 |

Alge-Grid 6 Solution
$a=9$

| 7 | 6 | 9 |
| :---: | :---: | :---: |
| 1 | 4 | 5 |
| 8 | 2 | 3 |

## Alge-Grid Solutions

Alge-Grid 7 Solution
$a=1$

| 6 | 8 | 9 |
| :--- | :--- | :--- |
| 1 | 5 | 2 |
| 4 | 3 | 7 |

Alge-Grid 9 Solution
$a=6$

| 8 | 2 | 3 |
| :---: | :---: | :---: |
| 5 | 7 | 9 |
| 4 | 6 | 1 |

Alge-Grid 11 Solution
$a=8$

| 3 | 8 | 4 |
| :---: | :---: | :---: |
| 9 | 7 | 6 |
| 2 | 5 | 1 |

Alge-Grid 8 Solution
$a=3$

| 5 | 9 | 6 |
| :---: | :---: | :---: |
| 1 | 2 | 4 |
| 8 | 7 | 3 |

Alge-Grid 10 Solution $a=5$

| 4 | 9 | 8 |
| :--- | :--- | :--- |
| 7 | 2 | 6 |
| 1 | 5 | 3 |

Alge-Grid 12 Solution
$a=4$

| 1 | 8 | 9 |
| :---: | :---: | :---: |
| 6 | 3 | 4 |
| 7 | 2 | 5 |

## Alge-Grid Solutions

Alge-Grid 13 Solution
$a=6$

| 8 | 1 | 7 |
| :--- | :--- | :--- |
| 2 | 3 | 9 |
| 4 | 5 | 6 |

Alge-Grid 15 Solution
$a=5$

| 1 | 7 | 9 |
| :---: | :---: | :---: |
| 5 | 2 | 6 |
| 3 | 8 | 4 |

Alge-Grid 17 Solution
$a=3$

| 5 | 3 | 6 |
| :---: | :---: | :---: |
| 8 | 7 | 4 |
| 1 | 9 | 2 |

Alge-Grid 14 Solution
$a=8$

| 2 | 7 | 6 |
| :--- | :--- | :--- |
| 3 | 8 | 1 |
| 4 | 9 | 5 |

Alge-Grid 16 Solution $a=7$

| 7 | 3 | 6 |
| :--- | :--- | :--- |
| 9 | 1 | 8 |
| 2 | 5 | 4 |

Alge-Grid 18 Solution
$a=9$

| 3 | 5 | 9 |
| :---: | :---: | :---: |
| 7 | 2 | 8 |
| 1 | 6 | 4 |

## Alge-Grid Solutions

Alge-Grid 19 Solution
$a=17$

| 10 | 13 | 11 |
| :---: | :---: | :---: |
| 16 | 12 | 17 |
| 15 | 14 | 18 |

Alge-Grid 21 Solution
$a=12$

| 13 | 17 | 12 |
| :---: | :---: | :---: |
| 15 | 14 | 10 |
| 16 | 11 | 18 |

Alge-Grid 23 Solution
$a=10$

| 18 | 11 | 17 |
| :---: | :---: | :---: |
| 13 | 10 | 14 |
| 12 | 16 | 15 |

Alge-Grid 20 Solution
$a=15$

| 11 | 13 | 16 |
| :---: | :---: | :---: |
| 17 | 12 | 10 |
| 15 | 14 | 18 |

Alge-Grid 22 Solution $a=13$

| 13 | 14 | 10 |
| :---: | :---: | :---: |
| 12 | 18 | 11 |
| 15 | 17 | 16 |

Alge-Grid 24 Solution
$a=11$

| 16 | 11 | 18 |
| :---: | :---: | :---: |
| 10 | 15 | 14 |
| 13 | 17 | 12 |

## Alge-Grid Solutions

Alge-Grid 25 Solution
$a=18$

| 12 | 15 | 10 |
| :---: | :---: | :---: |
| 18 | 13 | 11 |
| 16 | 17 | 14 |

Alge-Grid 27 Solution
$a=14$

| 18 | 11 | 16 |
| :---: | :---: | :---: |
| 17 | 10 | 12 |
| 14 | 13 | 15 |

Alge-Grid 29 Solution
$a=14$

| 16 | 18 | 15 |
| :---: | :---: | :---: |
| 13 | 14 | 11 |
| 17 | 12 | 10 |

Alge-Grid 26 Solution
$a=16$

| 15 | 18 | 17 |
| :---: | :---: | :---: |
| 14 | 11 | 10 |
| 13 | 16 | 12 |

Alge-Grid 28 Solution $a=17$

| 12 | 15 | 14 |
| :---: | :---: | :---: |
| 17 | 13 | 10 |
| 18 | 11 | 16 |

Alge-Grid 30 Solution
$a=11$

| 16 | 13 | 15 |
| :---: | :---: | :---: |
| 11 | 12 | 17 |
| 14 | 18 | 10 |

## Alge-Grid Solutions

Alge-Grid 31 Solution
$a=15$

| 15 | 16 | 10 |
| :---: | :---: | :---: |
| 13 | 14 | 11 |
| 17 | 18 | 12 |

Alge-Grid 33 Solution
$a=12$

| 14 | 13 | 12 |
| :---: | :---: | :---: |
| 15 | 17 | 18 |
| 10 | 11 | 16 |

Alge-Grid 35 Solution $a=13$

| 17 | 16 | 15 |
| :---: | :---: | :---: |
| 12 | 18 | 10 |
| 11 | 13 | 14 |

Alge-Grid 32 Solution
$a=16$

| 16 | 15 | 11 |
| :---: | :---: | :---: |
| 18 | 12 | 14 |
| 17 | 13 | 10 |

Alge-Grid 34 Solution $a=18$

| 14 | 17 | 18 |
| :---: | :---: | :---: |
| 15 | 12 | 10 |
| 16 | 13 | 11 |

Alge-Grid 36 Solution
$a=10$

| 12 | 11 | 17 |
| :---: | :---: | :---: |
| 10 | 15 | 18 |
| 16 | 14 | 13 |

## Alge-Grid Solutions

Alge-Grid 37 Solution
$a=27$

| 21 | 22 | 26 |
| :---: | :---: | :---: |
| 24 | 20 | 19 |
| 27 | 23 | 25 |

Alge-Grid 39 Solution
$a=25$

| 20 | 19 | 21 |
| :---: | :---: | :---: |
| 27 | 24 | 25 |
| 23 | 26 | 22 |

Alge-Grid 41 Solution $a=19$

| 25 | 20 | 26 |
| :---: | :---: | :---: |
| 24 | 23 | 21 |
| 27 | 19 | 22 |

Alge-Grid 38 Solution
$a=24$

| 22 | 23 | 27 |
| :---: | :---: | :---: |
| 21 | 19 | 25 |
| 26 | 24 | 20 |

Alge-Grid 40 Solution $a=21$

| 24 | 26 | 22 |
| :--- | :--- | :--- |
| 23 | 21 | 27 |
| 19 | 25 | 20 |

Alge-Grid 42 Solution
$a=26$

| 23 | 25 | 19 |
| :---: | :---: | :---: |
| 22 | 24 | 21 |
| 27 | 20 | 26 |

## Alge-Grid Solutions

Alge-Grid 43 Solution
$a=24$

| 22 | 26 | 25 |
| :--- | :--- | :--- |
| 24 | 19 | 20 |
| 21 | 23 | 27 |

Alge-Grid 45 Solution
$a=25$

| 22 | 25 | 21 |
| :---: | :---: | :---: |
| 19 | 24 | 26 |
| 27 | 20 | 23 |

Alge-Grid 47 Solution $a=21$

| 22 | 19 | 27 |
| :---: | :---: | :---: |
| 25 | 23 | 24 |
| 26 | 21 | 20 |

Alge-Grid 44 Solution
$a=26$

| 19 | 27 | 23 |
| :---: | :---: | :---: |
| 20 | 26 | 24 |
| 25 | 28 | 21 |

Alge-Grid 46 Solution $a=27$

| 27 | 23 | 26 |
| :---: | :---: | :---: |
| 22 | 20 | 24 |
| 25 | 19 | 21 |

Alge-Grid 48 Solution
$a=20$

| 24 | 26 | 21 |
| :---: | :---: | :---: |
| 23 | 22 | 25 |
| 27 | 20 | 19 |

## Alge-Grid Solutions

Alge-Grid 49 Solution
$a=19$

| 19 | 27 | 22 |
| :---: | :---: | :---: |
| 24 | 20 | 26 |
| 23 | 25 | 21 |

Alge-Grid 51 Solution
$a=23$

| 20 | 26 | 24 |
| :---: | :---: | :---: |
| 22 | 21 | 27 |
| 25 | 19 | 23 |

Alge-Grid 53 Solution $a=23$

| 23 | 25 | 27 |
| :---: | :---: | :---: |
| 22 | 26 | 21 |
| 20 | 24 | 19 |

Alge-Grid 50 Solution
$a=22$

| 22 | 27 | 19 |
| :--- | :--- | :--- |
| 24 | 25 | 26 |
| 23 | 20 | 21 |

Alge-Grid 52 Solution $a=20$

| 21 | 25 | 23 |
| :--- | :--- | :--- |
| 22 | 27 | 19 |
| 26 | 20 | 24 |

Alge-Grid 54 Solution
$a=22$

| 26 | 23 | 25 |
| :---: | :---: | :---: |
| 20 | 24 | 22 |
| 19 | 21 | 27 |

## Prime Group©2021

