Name_____

Period _____ Date _____

UNIT 7 **STUDENT PACKET**



EQUATIONS AND INEQUALITIES

-			
		Monitor Your Progress	Page
	My Word Bank		0
7.0	Opening Problem: Lions and Tigers and Bears		1
7.1	 Solving Equations Using Substitution Use substitution as a strategy to solve equations. Solve number puzzle problems using equation-skills. 	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	2
7.2	 Solving Equations Using Algebra Use the concept of balance with a cups and counters model to solve equations. Solve equations algebraically. Solve problems using equations. 	3 2 1 0 3 2 1 0 3 2 1 0 3 2 1 0	8
7.3	Inequalities Solve and graph inequalities. 	3 2 1 0	16
7.4	 Equations and Inequalities with Rational Numbers Solve equations and inequalities that include rational numbers. Use equations and inequalities to solve problems. 	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	22
	Review		28
	Student Resources		35

Parent (or Guardian) signature _____

MY WORD BANK

Explain the mathematical meaning of each word or phrase, using pictures and examples when possible. See **Student Resources** for mathematical vocabulary.



OPENING PROBLEM: LIONS, TIGERS AND BEARS

[7.NS.3; SMP 1, 2, 3, 7, 8]

On this page, the same animals have the same value. Different animals have different values.

Find the value of each animal and the value of 💥 . Explain your reasoning. 2 =

SOLVING EQUATIONS USING SUBSTITUTION

We will use substitution as a strategy to solve equations. Then we will use these equation-solving skills to solve number puzzle problems, given visual and written clues.

[7.NS.3, 7.EE.3, 7.EE.4a; SMP1, 7]

GETTING STARTED

Solve for the unknown. Write MM if you use mental math. Otherwise, show work. Check each solution by substituting it into the original equation.



10. Record the meanings of <u>equation</u> and <u>solution to an equation</u> / <u>solve an equation</u> in **My Word Bank**.

THE COVER UP METHOD

Follow your teacher's directions for (1) - (7). Solve and check each equation using substitution.



MathLinks: Grade 7 (2nd ed.) ©CMAT Unit 7: Student Packet

Equations and Inequalities

PRACTICE 1

1. Record the meaning of <u>substitution</u> in **My Word Bank**.

Solve and check each equation using substitution.

2.	4 + 12 <i>b</i> = 100	3.	15 = 5 <i>y</i>	+ 20	4.	6 <i>n</i> – 5 = -65
5.	0 = 23(0.5 + x)	6.	$\frac{m}{4}$ + 6	= 7	7.	-4(p-10) = 100
			-4			
8.	$-6 = \frac{42}{2}$	9.	$-\frac{1}{4}(x+$	33) = -8	10.	-(0.5y + 1.5) = -3
	<i>n</i> + 1		4			
					r	

11. The weight of a small bag of apples, *a*, is unknown. The weight of a small bag of oranges is 5 pounds.

a. Write an expression for the weight of a large grocery bag filled with a small bag of oranges and a small bag of apples.	b.	Write an expression for the weight of 3 large grocery bags, each filled with a small bag of oranges and a small bag of apples.
c. Write an equation to show that the total weight of the 3 large grocery bags is 36 pounds. Then solve the equation.	d.	What does the solution to the equation represent?

INTRODUCTION TO THE HUNDRED CHART PUZZLE

To the right is a hundred chart.

1. State two patterns you notice on the chart.

1	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50
51	52	53	54	55	56	57	58	59	60
61	62	63	64	65	66	67	68	69	70
71	72	73	74	75	76	77	78	79	80
81	82	83	84	85	86	87	88	89	90
91	92	93	94	95	96	97	98	99	100

Suppose a hundred chart is cut into puzzle-type pieces. For problems 2 - 4, write in the missing numbers. For problems 5 - 7, write in the missing algebraic expressions.



THE HUNDRED CHART PUZZLE

Follow your teacher's directions.



PRACTICE 2

Here are some puzzle pieces from different hundred square puzzles. Write in variable expressions and use your equation-solving skills to find the numbers in the pieces.



Shah and Jacy built square tile patterns and kept track of the steps in the tables below.

- 5. Fill in the number of tiles in step 5 for each, and then write input-output rules (equations).
- 6. Find the number of tiles in step 100 for each.
- 7. Find the step number for the given number of tiles in the last row for each.

Shah's tile pattern						
Step # (x)	# of tiles (y)					
1	9					
2	17					
3	25					
4	33					
5						
100						
	401					
Rule:						

Jacy's tile pattern						
Step # (<i>x</i>)	# of tiles (y)					
1	7					
2	15					
3	23					
4	31					
5						
100						
	159					
Rule:						

- 8. How are these patterns the same?
- 9. How are they different?

SOLVING EQUATIONS USING ALGEBRA

We will use the concept of balance with a cups and counters model to solve equations. Then we will use properties of arithmetic and equality to solve equations algebraically, and apply these skills to solving problems.

[7.NS.3, 7.EE.1, 7.EE.3, 7.EE.4a, 7.RP.2ac; SMP1, 2, 3, 4, 5, 6, 7, 8]

GETTING STARTED In each problem below, all the shapes have some weight, the same shapes have the same weight, and different shapes have different weights. All problems are independent of one another. Use what you know about balance to answer each question. 1. 2. What weighs the same as \land ? What weighs the same as ? 4. 3. This scale shows balance. Why is this What weighs the same as \land ? incorrect?

BALANCED AND UNBALANCED SCALES

We can picture equalities with balanced scales and inequalities with unbalanced scales. Imagine that each 1 represents one unit of weight and each 2 represents an unknown weight (not equal to zero). To represent unknowns, a popular variable is x.

		Equation		Inequality	<u>_</u>
ba (This is a lanced scale (equation).	3x = 3x		1 < 3	This is an unbalanced scale (inequality)
For Dra Wri	each proble w a sketch to te the resulti	m, start with this original o illustrate the action descri ng equation or inequality.	balance bed.	ed scale, 4 = 4.	
1.	Three units sides of the equation of inequality:	(1's) are removed from bot original balanced scale.	n 2.	One unknown (<i>x</i>) is of the original balance equation or inequality:	added to both sides need scale.
3.	Two units a	re removed from the right s	ide 4.	Two x's are added to	to the right side, and
	equation of inequality:			equation or inequality:	
5.	The numbe original sca equation of inequality:	r of units on both sides of th le is doubled.	e 6.	One-half the units an side of the original s equation or inequality:	are removed from each scale.

- 7. Iggy built the balanced scale to the right.
 - a. Write the equation it represents.



- b. Why can Iggy remove 3 units from both sides?
- c. Draw the new balanced scale and write the equation it represents.
- d. Does the equation in part c represent the solution to the equation in part a?

SOLVING EQUATIONS WITH BALANCE

Follow your teacher's directions.

(1)			
Positive Counter	Negative Counter	Cup	Upside-down Cup
		(2)	
(4)		(5)	

PRACTICE 3

For each equation, first build it with cups and counters. Continue the building process until it is solved. Record the process with drawings. Write the solution and check it using substitution.



SOLVING EQUATIONS ALGEBRAICALLY







Circle the part of each equation-solving process that contains a mistake. Correct it and continue the solution process underneath the problem.

5.	-12 = -3x + 15 - 6x	6. $0 = 10 - 2(x + 5) + 30 + 12x$	7. $7x - 3(2x - 1) - 2x = -2$
	-12 = 3x + 15	0 = 10 - 2x + 5 - 30 + 12x	7x - 6x + 3 - 2x = -2
	-27 = 3x	0 = 45 + 10 <i>x</i>	- <i>x</i> + 3 = -2
	-9 = x	-45 = 10 <i>x</i>	- <i>x</i> = -5
		-4.5 = x	
Co	rrection(s):	Correction(s):	Correction(s):

8. Circle all of the following equations that are equivalent to 4 + 6x = 22.

$$6x = 18$$
 $4 + x = 16$ $22 = 4 + 6x$ $\frac{4 + 6x}{2} = \frac{22}{2}$ $3(4 + 6x) = 66$

PRACTICE 5

Frida and Tommy discussed how they might solve the equation 20d + 78 = 12.

- 1. Frida said, "First I'm going to divide the expressions on both sides of the equation by 20." Even though Frida's strategy is permissible, why might it be difficult to execute?
- 2. Tommy said, "First I'm going to subtract 78." Even though Tommy has the right idea, explain why this language is not precise.
- 3. Solve the equation above. Show your work.

- 4. D.D. has \$240 in a savings account. D.D. deposits \$20 per month for several months.
 - a. Write a numerical expression for the amount of money in D.D.'s account after 6 months.
 - c. Write an equation to represent that D.D. has \$580 in the account after *n* months. Then solve the equation for *n*.
- b. Write a variable expression for the amount of money in D.D.'s account after *n* months.
- d. D.D. decides to be more ambitious about saving. With the same initial amount of money in the account and with deposits of \$25 per month, how long will it take for D.D. to save \$580? Show all work by writing and solving an equation.
- 5. Circle all the equations below that are equivalent to 0 = 3(x 2) + 5.
 - -5 = 3(x 2)

3(x-2) + 5 = 0

3x - 2 + 5 = 0

RAMON'S PHONES

Ramon's Phones sells cheap calling plans. There is a set-up cost of \$20, and then there is an annual charge of \$144. If you wish, you may be billed semi-annually or quarterly.



11. Ric thinks that the point (1, 144) should lie on the graph since the cost is \$144 per every 1 year of service. Explain to Ric why this isn't true.

INEQUALITIES

We will explore the conditions under which the sign of an inequality is preserved or reversed, and solve and graph inequalities.

[7.NS.3, 7.EE.1, 7.EE.4ab; SMP1, 3, 6, 7, 8]

GETTING STARTED

1. Circle all of the true inequalities below. Then use these inequalities for problems 2 – 3

a.	(-1)(7) > (-1)(8)	b.	$\frac{5}{12} < \frac{5}{9}$	c. $3(4-8) < 3(4) - 8$
d.	21 + 9 < 9 + 21	e.	$\frac{3}{5} < \frac{6}{13}$	f4(3) + 6(3) < -(4 + 6)

- 2. Choose one false inequality above with a fraction or decimal and explain why it is false.
- 3. Choose one false inequality above with mathematical operations and explain why it's false.

Under each inequality below are four potential solutions. Circle all the solutions that make each inequality true. Then write a description of ALL of the numbers that could be solutions to the inequality.

4. v + 5 > -2	5. w-4<-4	6. $2x > -20$	7. $\frac{y}{3} < -6$
v = -8	<i>w</i> = 0	<i>x</i> = 10	<i>y</i> = 18
V=-7	<i>w</i> = -1	<i>x</i> = -10	<i>y</i> = -18
v = -6	<i>w</i> = 0.5	<i>x</i> = -9	<i>y</i> = -24
<i>v</i> = -6.9	<i>w</i> = -0.5	<i>x</i> = -10.5	<i>y</i> = -21
Description:	Description:	Description:	Description:

8. Record the meaning of <u>inequality</u> in **My Word Bank**.

GRAPHING INEQUALITIES

Follow your teacher's directions.



PRACTICE 6

1. Record the meaning of <u>boundary point of a solution set</u> in **My Word Bank**.

Fill in	the table for	each inequality below.						
In	equality	Written description of all	solutions	Graph of all solutions				
2.	v > -3							
3.	<i>w</i> ≤ 1							
4. Cii	rcle all numb	ers below that are solutions to	o the inequ	ality $x + 1 \ge -5$.				
-7	· -6	-5.9999 -6.00	00001	$-\frac{30}{5}$ 0 $\frac{3}{17}$				
5. List four integers that are less than or equal to -2.								
6. List four non-integers that are less than or equal to -2.								
7. Hc	7. How many numbers exist that are less than or equal to -2?							

8. Why is -1 not a solution to the inequality $x \le -2$?

Write an inequality for each situation below. Label and scale each graph appropriately.

4	Situation	Inequality	Graph
9.	You must be at least 48 inches tall to ride the rollercoaster.	(let <i>h</i> = height)	
10.	To ride the rollercoaster, wait time is more than 16 minutes.	(let <i>t</i> = time)	

Write situations of your choice for the graphs below.



EXPLORING INEQUALITIES

Complete the tables below. For the last column, write a new inequality that reflects the change in values after operating on the original inequality each time. Be sure that your new inequality is in fact a true statement.

1. Begin each operation	then do this to both		Ste	eps	True inequality with the resulting values
inequality:	sides	Left		Right	
4 < 10	Add 5	4 +	-	10 +	9 < 15
	Add -5				
	Subtract 3				
	Subtract -3	4 – (_)		
	Multiply by 8				
	Multiply by -8	4()			
	Divide by 2				
	Divide by -2	4 _ ()		
and the second					
2. Begin each operation	then do this to both		Ste	eps	True inequality with the resulting values
2. Begin each operation with this inequality:	then do this to both sides	Left	Ste	eps Right	True inequality with the resulting values
2. Begin each operation with this inequality:	then do this to both sides Add 5	Left -3 +	Ste	eps Right -6 +	True inequality with the resulting values
 Begin each operation with this inequality: -3 > -6 	then do this to both sides Add 5 Add -5	Left -3 +	Ste	eps Right -6 +	True inequality with the resulting values
 2. Begin each operation with this inequality: -3 > -6 	then do this to both sides Add 5 Add -5 Subtract 7	Left	Ste	eps Right -6 +	True inequality with the resulting values
 2. Begin each operation with this inequality: -3 > -6 	then do this to both sides Add 5 Add -5 Subtract 7 Subtract -7	Left -3.+	Ste	eps Right -6 +	True inequality with the resulting values
 2. Begin each operation with this inequality: -3 > -6 	then do this to both sides Add 5 Add -5 Subtract 7 Subtract -7 Multiply by 2	Left 3.+	Ste	eps Right -6 +	True inequality with the resulting values
 2. Begin each operation with this inequality: -3 > -6 	then do this to both sides Add 5 Add -5 Subtract 7 Subtract -7 Multiply by 2 Multiply by -2	Left -3.+	Ste	eps	True inequality with the resulting values
 2. Begin each operation with this inequality: -3 > -6 	then do this to both sides Add 5 Add -5 Subtract 7 Subtract 7 Multiply by 2 Multiply by -2 Divide by 3	Left -3.+	Ste	eps Right -6 +	True inequality with the resulting values

- 3. In the table above, look closely at the last column and circle every result where the inequality changed direction compared to the original inequality.
- 4. Under what circumstances did the direction of the inequality symbol change?

SOLVING INEQUALITIES

Follow your teacher's directions.



PRACTICE 7

Rewrite each inequality below so that the variable is on the left side and graph it.



EQUATIONS AND INEQUALITIES WITH RATIONAL NUMBERS

We will solve equations and inequalities that include rational numbers. We will use equations and inequalities to solve problems.

[7.NS.3, 7.EE.1, 7.EE.3, 7.EE.4a, 7.EE.4b; SMP1, 3, 4, 6, 8]

GETTING STARTED

For each verbal statement below, choose an appropriate symbolic representation from the given choices. Some choices may not be used at all, and some may be used more than once.



- 8. Why must the inequality n > n always be false?
- 9. Why must the inequality n + 1 > n always be true?

Describe a situation that could be represented by each graph.



EQUATIONS WITH RATIONAL NUMBERS

Follow your teacher's directions.



PRACTICE 8

Solve each equation below and check.

1.
$$-1.4 = 2.2 - 4(y - 1.1)$$

2. $-\frac{1}{6} = \frac{2}{3}(h - 1)$
3. $4p + 1\frac{1}{2} - 6p = -\frac{3}{4}$
4. $\frac{-k - 2 - 3k}{-10} = -1$

Identify your variable(s), write an equation, solve the equation, and answer the question.



GRAPH MATCH

The solutions to problems 1 - 4 on **Practice 8** are the boundary points for problems 1 – 8 below. Use what you know about inequalities to write the solutions and match the them to their correct graphs.



PRACTICE 9: EXTEND YOUR THINKING

Solve each equation or inequality and graph it.



Solve each problem using algebra (an equation or inequality). Define variables, answer the question and check the solution(s).



IESHA'S SUMMER

For each problem below, write an inequality, solve it, and graph the solutions. Then explain each answer in the context of the problem.

1. lesha has \$460 in a checking account at the beginning of summer. She wants to leave at least \$200 in her account by the end of summer. She withdraws \$25 each week for her expenses. How many weeks can lesha withdraw this amount of money from this account?

2. A taxi service charges a \$2.25 flat rate in addition to \$0.64 per mile. lesha wants to spend no more than \$10 on a ride. How many miles can lesha travel without exceeding her limit?

3. lesha goes to the Fun Golf Arcade with her friends. They play golf, have lunch, and then play some video games. A round of golf is \$6.20. Lunch is \$5.60. Video games are \$0.50 each. If lesha wants to spend no more than \$20.00, how many video games can she play?

REVIEW

BIG SQUARE PUZZLE: EQUATIONS AND INEQUALITIES

Your teacher will give you a puzzle to assemble. Below is one of the equations in the puzzle. Explain or show two different ways to solve it.



WHY DOESN'T IT BELONG?: EQUATIONS AND INEQUALITIES

Solve and graph each of the algebraic sentences below. Choose one and explain why its solutions don't belong with the others. Then choose at least one more and explain why its solutions don't belong.



OPEN MIDDLE PROBLEMS: EQUATIONS AND INEQUALITIES

Use exactly three of the digits 1 through 9 one time each.

1. Structure:	2. Structure:
$\Box x + \Box = \Box$	x - x = x
a. Write an equation and find its solution.	a. Write an equation and find its solution.
b. Write an equation so that it has the greatest possible solution.	 b. Write an equation so that it has the greatest possible solution.
c. Write an equation so that it has the least possible solution.	c. Write an equation so that it has the least possible solution.

POSTER PROBLEMS: EQUATIONS AND INEQUALITIES

Part 1: Your teacher will divide you into groups.

- Identify members of your group as A, B, C, or D.
- Each group will start at a numbered poster. Our group start poster is _____.
- Each group will have a different colored marker. Our group marker is _____

Part 2: Do the problems on the posters by following your teacher's directions

Poster 1 (or 5)	Poster 2 (or 6)	Poster 3 (or 7)	Poster 4 (or 8)
$\frac{1}{2}\left(v+\frac{1}{3}\right)-\frac{1}{4}v \ge -1$	$1\frac{1}{2} - 1\frac{1}{2}(w-1) > 2\frac{1}{4}$	$\frac{5}{3} < \frac{1}{5}x - 2\left(x - \frac{1}{3}\right)$	$-\frac{3}{4} \leq -\frac{4}{5} - \left(y - \frac{1}{2}\right)$

- A. Copy the inequality and apply the distributive property (one step).
- B. Collect like terms (one more step).
- C. Solve for the values of the variable (two more steps).
- D. Check the boundary point and at least one other point. Graph the solutions.

Part 3:

- 1. Copy the problem from your start poster.
- 2. Solve your start poster problem in a different way.

VOCABULARY REVIEW



SPIRAL REVIEW

1. Follow the math path to computational fluency.



SPIRAL REVIEW

3. Linus is choosing from two different restaurants, Patty On Burgers and Oh What a Burger. Linus created tables and graphs to show how much he would have to pay for different amounts of burgers. Unfortunately, water spilled on parts of his tables and the graph for Patty On Burger and some information was erased.



- a. Complete Linus' tables
- b. Complete the graph with labels, title, and graph Patty On Burgers.
- c. Do both graphs represent proportional relationships? Explain.
- d. What is the unit rate for Patty On Burgers?
- e. What is the unit rate for Oh What a Burger?
- f. Which burger place is the better buy? Explain.

REFLECTION

1. **Big Ideas**. Shade all circles that describe big ideas in this unit. Draw lines to show connections that you noticed.



- 2. Unit Progress. Go back to Monitor Your Progress on the cover and complete or update your responses. Explain something you understand better now than before.
- 3. **Mathematical Practices.** Which properties of equality hold for inequalities? Which do not? Give a counter example to prove a property that does not hold [SMP3, 7]. Then circle one more SMP on the back of this packet that you think was addressed in this unit and be prepared to share an example.
- 4. **Making Connections.** What strategies that you used for solving simple equations helped you when the equations became more complex?

STUDENT RESOURCES

[Word or Phrase	Definition
	boundary point of a solution set	A <u>boundary point of a solution set</u> is a point for which any interval surrounding the point on the number line contains both solutions and non-solutions. If the solution set is an interval, the boundary points of the solution set are the endpoints of the interval.
		The boundary point for BOTH $x < -1$ AND $x \stackrel{f}{=} -1$ is $x = -1$. In the first case the boundary point IS NOT part of the solution set (open circle). In the second case it IS (closed circle).
	equation	An <u>equation</u> is a mathematical statement that asserts the equality of two expressions.
	expression	A mathematical <u>expression</u> is a combination of numbers, variables, and operation symbols. When values are assigned to the variables, an expression represents a number.
		Some mathematical expressions are $7x$, $a + b$, $4v - w$, $\frac{8 + x}{10}$, and 19.
	inequality	An <u>inequality</u> is a mathematical statement that asserts the relative size or order of two objects. When the expressions involve variables, a <u>solution to the inequality</u> consists of values for the variables which, when substituted, make the inequality true.
		5 > 3 is an inequality.
		x + 3 > 4 is an inequality. All values for x that are greater than 1 are solutions to this inequality.
	solution to an equation	A <u>solution to an equation involving</u> variables consists of values for the variables which, when substituted, make the equation true.
		The value $x = 8$ is a solution to the equation $10 + x = 18$. If we substitute 8 for x in the equation, the equation becomes true: $10 + 8 = 18$.
	solve an equation	To <u>solve an equation</u> refers to finding all values for the variables in the equation that, when substituted, make the equation true. Values that make an equation true are called solutions to the equation.
		To solve the equation $2x = 6$, one might think "two times what number is equal to 6?" Since $2(3) = 6$, the only value for x that satisfies this condition is 3. Therefore 3 is the solution.
	substitution	Substitution refers to replacing a value or quantity with an equivalent value or quantity.
		If $x + y = 10$, and $y = 8$, then we may substitute this value for y in the equation to get $x + 8 = 10$.

Properties of Arithmetic Properties of arithmetic govern the manipulation of expressions (mathematical phrases). For any three numbers *a*, *b*, and *c*: ✓ Associative property of addition Associative property of multiplication a + (b + c) = (a + b) + c $a \bullet (b \bullet c) = (a \bullet b) \bullet c$ Commutative property of addition Commutative property of multiplication $a \bullet b = b \bullet a$ a + b = b + a✓ Additive identity property ✓ Multiplicative identity property (addition property of 0) (multiplication property of 1) a + 0 = 0 + a = a $a \bullet 1 = 1 \bullet a = a$ Additive inverse property ✓ Multiplicative inverse property a + (-a) = -a + a = 0 $a \bullet \frac{1}{2} = \frac{1}{2} \bullet a = 1$ Distributive property relating addition and multiplication. a(b + c) = ab + ac and (b + c)a = ba + ca for any three numbers a, b, and c. **Properties of Equality** Properties of equality govern the manipulation of equations (mathematical sentences). For any three numbers *a*, *b*, and *c*: ✓ Addition property of equality Reflexive property of equality: a = a(Subtraction property of equality) If a = b and c = d, then a + c = b + d. Symmetric property of equality: If a = b, then b = aMultiplication property of equality \checkmark (Division property of equality) Transitive property of equality: If a = b and c = d, then ac = bdIf a = b, and b = c, then a = c



String of Words	Example	Symbols	Classification
is less than	4 is less than 10	4 < 10	inequality
less than	4 less than 10	10 – 4	expression
is greater than	7 is greater than 2 + 3	7 > 2 + 3	inequality
greater than	7 greater than 2 + 3	(2 + 3) + 7	expression

"Is greater than" includes the word "is." Therefore, it behaves like a mathematical verb. This string of words is used to make a mathematical sentence (an inequality in this case).

"Greater than" is a string of words without a verb. It translates into an expression. In English, we connect phrases with verbs to make sentences. The same is true in mathematics.

Equations and Inequalities





Solving Equations Using a Model					
Let + represent 1	Let ${f V}$ represent the unkn	nown (like <i>x</i>)			
Let – represent -1	Let $oldsymbol{\Lambda}$ represent the oppo	osite of the unknown (like - <i>x</i>)			
 As you solve equations, think: Can I simplify one or both sides? That is, focus on what can be done to each expression alone. What can I do to both sides? That is, focus on what can be done to the equation. The following examples illustrate one solution path. Others paths are possible to arrive at the same solutions. 					
Example 1: Solve $-3 = 3(x + 2)$. Check (after solving): $3(-3) + 6 \rightarrow -5$	$9 + 6 \rightarrow -3 = -3$				
Picture	Equation	Comments			
V V V +++ +++	-3 = 3x + 6	build the equation (think: 3 groups of x + 2) and rewrite			
 +++ +++ 	$ \begin{array}{rcl} -3 &=& 3x + 6 \\ \underline{+(-6)} &=& \underline{+(-6)} \\ -9 &=& 3x \end{array} $	add -6 to both sides and remove zero pairs			
$\begin{array}{cccc} - & - & - & \leftarrow & \vee & \vee \\ - & - & - & \leftarrow & \rightarrow & \vee & \vee \\ - & - & - & \leftarrow & \rightarrow & \vee & \vee \end{array}$	$\frac{-9}{3} = \frac{3x}{3}$ $-3 = x$	divide both sides by 3 to put counters equally into cups			
Example 2: Solve: $-2x - 5 - x = 4$ Check (after solving): $-2(-3) - 5 - (-3)$	$0) \rightarrow 6-5+3 \rightarrow 1+3=-3+7-2$	$\rightarrow 4 = 4$			
Picture	Equation	Comments			
$ \begin{array}{c c} \wedge \wedge \wedge \\ \end{array} + + + + \end{array} $	-3x-5=4	build the equation and rewrite (collect like terms)			
$ \begin{array}{c c} & & & & \\ & & & \\ \hline & & & \\ - & - & - \\ + & + & + & + \\ + & + & + & + & + \\ \end{array} $	$-3x-5 = 4$ $\frac{+5}{-3x} = \frac{+5}{9}$	add 5 to both sides and remove zero pairs			
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	(-1)(-3x) = (-1)(9) → 3x = -9 $\frac{3x}{3} = \frac{-9}{3}$ x = -3	take the opposite of both sides (accomplished by multiplying both sides by -1), and then divide both sides by 3			
$\begin{array}{ccc} V & \longleftrightarrow & - & - & - \\ V & \longleftrightarrow & - & - & - \\ V & \longleftrightarrow & - & - & - \end{array}$	$\frac{-3x}{-3} = \frac{9}{-3}$ $x = -3$	The above actions have the same effect as diving by -3 in a single step			



V

re

4

······································	
/hen multiplying or dividing both sides of an inequality	by a negative number, the direction of the inequality
everses.	

Reversing the Direction of an Inequality

Original inequality	Do to both sides	Resulting inequality	Direction reverses?
	Add 2	12 > -2	No
40 4	Subtract 2	8 > -6	No
10 > -4	Multiply by 2	20 > -8	No
	Divide by 2	5 > -2	No
	Add -2	-12 < 2	No
10 - 1	Subtract -2	-8 < 6	No
-10 < 4	Multiply by -2	20 > -8	Yes
	Divide by -2	5 > -2	Yes

The direction of an inequality reverses **ONLY** when multiplying or dividing both sides of an inequality by a negative number.

Note that it does not matter if there are negative numbers in the original inequality or not.

Solving Inequalities in One Variable

When solving a linear inequality, treat the inequality as if it were an equation. When multiplying or dividing both sides of the inequality by a negative number, reverse the direction of the inequality.

	Example 1	Comments		Example 2	Comments
	-4 <i>x</i> + 1 ≤ 13	(Subtraction)		2 <i>x</i> – 9 ≤ -13	(Addition)
	-1 -1	inequality.		+9 +9	inequality.
	-4 <i>x</i> ≤ 12	(Division by a negative number)		2 <i>x</i> ≤ -4	(Division by a positive number)
	$\frac{-4x}{-4} \ge \frac{12}{-4}$	Reverse the inequality symbol.		$\frac{2x}{2} \le \frac{-4}{2}$	Do not reverse the inequality symbol.
	x≥-3	Solutions		x ≤ -2	Solutions
E	Fror alert. The inequa Example 2	lity does not always reverse v illustrates this.	whe	en solving an inequality	that includes negatives.

COMMON CORE STATE STANDARDS

	STANDARDS FOR MATHEMATICAL CONTENT				
7.RP.A	Analyze proportional relationships and use them to solve real-world and mathematical problems.				
7.RP.2	Recognize and represent proportional relationships between quantities:				
a.	Decide whether two quantities are in a proportional relationship, e.g., by testing for equivalent ratios in a table or graphing on a coordinate plane and observing whether the graph is a straight line through the origin.				
c.	Represent proportional relationships by equations. For example, if total cost t is proportional to the number n of items purchased at a constant price p , the relationship between the total cost and the number of items can be expressed as $t = pn$.				
7.NS.A	Apply and extend previous understandings of operations with fractions to add, subtract, multiply, and divide rational numbers.				
7.NS.3	Solve real-world and mathematical problems involving the four operations with rational numbers.				
7.EE.A	Use properties of operations to generate equivalent expressions.				
7.EE.1	Apply properties of operations as strategies to a dd, subtract, factor, and expand linear expressions with rational coefficients.				
7.EE.B	Solve real-life and mathematical problems using numerical and algebraic expressions and equations.				
7.EE.3	Solve multi-step real-life and mathematical problems posed with positive and negative rational numbers in				
	operations to calculate with numbers in any form; convert between forms as appropriate; and assess the reasonableness of answers using mental computation and estimation strategies.				
7.EE.4	Use variables to represent quantities in a real-world or mathematical problem, and construct simple equations and inequalities to solve problems by reasoning about the quantities: Solve word problems leading to equations of the form $px + q = r$ and $p(x + q) = r$, where p , q , and r are specific rational numbers.				
a.	Solve equations of these forms fluently. Compare an algebraic solution to an arithmetic solution, identifying the sequence of the operations used in each approach. For example, the perimeter of a rectangle is 54 cm. Its length is 6 cm. What is its width?				
b.	Graph the solution set of the inequality and interpret it in the context of the problem. For example: As a salesperson, you are paid \$50 per week plus \$3 per sale. This week you want your pay to be at least \$100. Write an inequality for the number of sales you need to make, and describe the solutions.				
SMP1	Make sense of problems and persevere in solving them				
SMR2	Reason abstractly and quantitatively.				
SMP3	Construct viable arguments and critique the reasoning of others.				
SMP4	Model with mathematics.				
SMP5	Use appropriate tools strategically.				
SMP6	Attend to precision.				
SMP7	Look for and make use of structure.				
SMP8	Look for and express regularity in repeated reasoning. 9 ¹¹ 781614 ¹¹ 454458 ¹¹				

MathLinks: Grade 7 (2nd ed.) ©CMAT Unit 7: Student Packet