

RATIONAL NUMBER ADDITION AND SUBTRACTION

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MY WORD BANK

Explain the mathematical meaning of each word or phrase, using pictures and examples when possible. See **Student Resources** for mathematical vocabulary.



OPENING PROBLEM: MR. MORTIMER'S MAGIC CUBES

[SMP 1, 2]

As a child, Merrimack Mortimer loved chemistry, and he grew to become an inventor. He called one of his great inventions Magic Hot them in greater detail.



COUNTERS AND ADDING INTEGERS

We will use counters to develop concepts about integers and use this model to generalize rules for integer addition. We will add integers using these rules.

[7.NS.1ab; SMP1, 2, 3, 5, 6, 7, 8]



c. Choose one number above that is NOT rational. Explain why it is not a rational number.

A COUNTER MODEL



12. Record the meanings of <u>zero pair</u> and <u>opposite of a number</u> in **My Word Bank**. *MathLinks*: Grade 7 (2nd ed.) ©CMAT Unit 4: Student Packet

- 1. The combination of one positive and one negative counter is called a _______.
- 2. Describe a zero pair using Mortimer's magic cubes.

	Build the	given values	using the	given numbers	of counters.	Then record drawings.
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Build	the given value	des using the given numbers of counter	s. Then record drawings.
	Value	# of counters	Drawing
3.	5	the least possible	
4.	-6	the least possible	
5.	0	2	
6.	0	10	
7.	5	7	
8.	5	more than 7, but less than 11	
9.	-2	8	
10.	-2	more than 2, but less than 6.	
11.	6	at least7	
12.	-1	more than 7	

Build and draw the following situations.

13. Start with a value of 4.What can you place on your work space to change this into a value of zero?	14. Start with a value of -4.What can you place on your work space to change this into a value of zero?
Draw the result.	Draw the result.

15. Try to represent any odd value with an even number of counters. What do you notice?

ADDING INTEGERS WITH COUNTERS

Use these sentence frames to help think through integer addition. Do not write in these.



5. (7) + (-)	2)	6. $(5) + (-5)$	7.	(2) + (6)
8. (-8) + (3	3)	9. (-2) + (-6)	10.	(-4) + (6)

For problems 11 – 13, use **positive**, **negative**, and **zero** as choices to finish each sentence below. Use all that apply for each.

11. When adding two positive integers, the result will be ______.

12. When adding two negative integers, the result will be ______.

13. When adding a positive integer and a negative integer, the result will be _____,

_____, or _____.

INTEGER ADDITION RULES

Description of counters on your workspace		Drawing	Numerical example	Summarizing Shorthand (positive → pos) (negative → neg)
1.	Positive Only			
	Place some positives. Then place more positives.		+	pos + pos is
2.	Negative Only			
	Place some negatives. Then place more negatives.		+	pos + pos is
3.	Positive and Negative			
	a. Place some of each so that the result is positive.	2	+	pos + neg is pos when:
	b. Place some of each so that the result is negative.		+	pos + neg is neg when:
	c. Place some of each so that the result is zero.		+	pos + neg is 0 when:

Without computing, determine whether each sum is positive (pos), negative (neg), or zero (0).

	Positive Example 6 + (-4)		Negative -6 +	Example (-4)		Zero Example -6 + 6
1.	-2 + (-11)	2.	7 + (-3)		3.	-2 + (-6)
4.	9 + 4	5.	-6 + 4		6.	11 + (-4)
7.	-6 + (-1)	8.	-5 + 1		9.	1 + (-1)

Compute each sum. Use drawings if desired.

10.	7 + (-2)	11.	-9 + 9		121 + (-3)
13.	11 + 12	14.	3 + (-8		155 + 6
16.	2 + (-2)	17.	-3 + (-(6)	1813 + 3

Make each equation true using the given directions.

Directions	Equation
19. Both numbers are positive.	10 = +
20. One positive number and one negative number.	10 = +
21. Both numbers are negative.	-10 = +
22. One positive number and one negative number.	-10 = +

Write a number sentence and describe the change resulting from each action.

23. Jenelle earns \$20, then loses \$20.	24. Andres loses 5 yards, then gains 5 yards.
25. Minh's kite drops 10 ft, then climbs 10 feet.	26. Avani gets 15 new cards for her collection, then gives away 15 cards.

- Compute the following: 100 + 100 = _____ and -100 + (-100) = _____.
 How is adding two negative numbers the same as adding two positive numbers?
- How is it different? 2. Compute the following: 100 + (-10) = ______ -100 + 10 = _____ How are these computations related to subtraction?
- 3. Complete the puzzle below using the given expression. Then find total sums for rows and for columns (exclude the gray numbers). Make sure the sums are equal for the very bottom row and far right column.

					b	
_		a + b		40	-60	TOTAL SUMS (ROWS)
		20	0			
		-50				
	a				-90	
		TOTAL SUMS (COLUMNS)				

4. Devin is a running back on her high school football team. On first down (the first play), she loses 3 yards. On second down (the next play), she gains 17 yards. Where is Devin's team in relation to where they started before first down?

COUNTERS AND SUBTRACTING INTEGERS

We will use a counter model to generalize the rule for integer subtraction. We will subtract integers using the rule.

[7.NS.1abcd, 7.SP.7b, 7.SP.8a; SMP1, 2, 3, 4, 5, 6, 7, 8]

GETTING STARTED

- 1. Using at least 6, but no more than 12 counters, draw a value of -2 in two different ways.
- 2. How many ways are there to build any given integer with counters?

Compute each sum. Use positive symbols (+) and negative symbols (-) if desired.

3.	-6 + (-6)	4.	-5 + 3
5.	5 + (-3)	6.	6 + (-6)

Compute each sum without using counters or drawings. Show work if not done mentally.

9600 + (-300)	7.	60 + (-30)	8. 27 + (-59)
	9.	-600 + (-300)	

- 10. Think about Mortimer's magic cubes. Regardless of the temperature of the liquid,
 - a. what happens to it if we remove some cold cubes?

b. what happens if instead we remove some hot cubes?

11. Marlowe thinks that -6 is greater than -3. What mistake is Marlowe making?

SUBTRACTING INTEGERS WITH COUNTERS 1

Use these sentence frames to help think through integer subtraction. Do not write in these.



Compute each difference. Draw using positive symbols (+) and negative symbols (-).

4. 6-3	56 - (-3)	6.	-7 – (-1)
71-(-1)	8. 4-4	9.	-4 – (-4)

10. Mateo thinks that "when you subtract, the result is **less than** what you started with." Look at problems 1 - 9. Put stars by examples that illustrate Mateo is not correct.

SUBTRACTING INTEGERS WITH COUNTERS 2



Compute each difference. Draw using positive symbols (+) and negative symbols (-).

5.	1 – 3	6.	-4 - (-5)
7.	2 – (-4)	8.	-6 – (3)
9.	8 – (-4)	10.	3 – (-3)
11.	-5 – (5)	12.	-2 – (-2)

13. Put a star next to all the problems above where the result (difference) is greater than number you started with (minuend). Then look at all the problems where you put stars in this lesson. What do you notice about the number that is being subtracted (subtrahend) EVERY time?

THE SUBTRACTION RULE

Compute. Show ACTIONS using positive symbols (+) and negative symbols (-).



Compare parts (a) and (b) for problems 1 - 5.

- 6. How are the actions for (a) different than the actions for (b)?
- 7. These examples show that subtracting a number gives the same result as ...

8. Generalize the **subtraction rule** for any numbers *m* and *n*.

Symbols	:	<i>m</i> – <i>n</i> = <i>m</i> +	<i>m</i> – (- <i>n</i>) = <i>m</i> +
Words:		<i>m</i> minus <i>n</i> is equal to	<i>m</i> minus the opposite of <i>n</i> is equal to
Example	•		

Complete each statement.

9.	3 – 2 = 3 +	10.	-3 - 2 = -3 +	11.	3 – (-2) = 3 +
12.	5 – (-7) = 5 +	13.	5 + 7 = 5	14.	6 + 8 = 6

- 1. Rewrite 7 (-3) as an equivalent addition expression using the subtraction rule. Which is easier for you to compute, the addition or subtraction expression?
- 2. Circle all expressions that are equivalent to 5 (-7).

-5 - 7 5 - 7 5 + 7

Rewrite each subtraction expression as an equivalent addition expression. Then compute

3.	17 – 24	4.	-56 – 18	5. 23 – (-9)
6.	-19 – (-44)	7.	-11 – 37	841 – (-15)

- 9. On a cold winter afternoon in Minnesota, the temperature was 4° Fahrenheit. By evening the temperature had dropped 11°. What was the evening temperature? Write as a subtraction expression and its equivalent addition expression before answering the question.
- 10. Complete the puzzle below using the given expression. Then find total sums for rows and for columns (exclude the gray numbers). Make sure the sums are equal for the very bottom row and far right column.

				b	
	a-b		30	-60	TOTAL SUMS (ROWS)
	-80	-70			
	-100				
a				85	
	TOTAL SUMS (COLUMNS)				

Rational Number Addition and Subtraction

4.2 Counters and Subtracting Integers

A ZERO-SUM GAME

- 1. Choose three numbers (two positive and one negative) whose sum is 0. Record them in Spinner 1 in any way you like.
- 2. Choose three numbers (two negative and one positive) whose sum is 0. Record them in Spinner 2 in any way you like.



3. In this game, one turn is spinning both spinners once and finding the sum. If the sum is greater than 0, you win. If the sum is less than zero, you lose. For your chosen numbers, explain whether or not this is a fair game where $P(\text{winning}) = P(\text{losing}) = \frac{1}{2}$.

- 4. Using a paperclip as a spinner, find the sum for 20 trials and record. Did the results turn out as you expected? Explain.
- 5. Change the positions of the numbers you placed in Spinner 1 and/or Spinner 2. Is the probability of winning still the same? Do you have a better chance of winning?





ADDING AND SUBTRACTING RATIONAL NUMBERS

We will use number lines to extend the addition and subtraction rules for integers to the set of rational numbers.

[7.NS.1abcd; SMP1, 2, 5, 6, 7, 8]



How do the two numbers added to 3 compare?



NUMBER LINE ADDITION

13. Look at problems 1 – 12 above. Do the addition rules we learned in a previous lesson hold for these problems? Do you think that these rules hold for all rational number addition?



Compute each sum using rules. Show work as needed.

716 + (-31)	8. 57 + 44	9.	-39 + 93
105.5 + 8.6	110.21 + (-0.245)	12.	6.81 + (-0.44)
13. $-6\frac{1}{3} + \left(-2\frac{1}{4}\right)$	14. $10\frac{2}{3} + \left(-8\frac{1}{5}\right)$	15.	$7\frac{1}{2} + \left(-12\frac{9}{16}\right)$



NUMBER LINE SUBTRACTION

13. Look at problems 1 – 12 above. Does the subtraction rule we learned in a previous lesson hold for these problems? Do you think that this rule holds for all rational number subtraction?



Compute each difference using rules. Show work as needed.

$7. -1\frac{1}{4} - \left(-2\frac{1}{4}\right)$	$8. 5\frac{3}{4} - \left(-3\frac{1}{4}\right)$	9.	$-2\frac{1}{4} - \left(-6\frac{3}{4}\right)$
1016 (-31)	1157 – 44	12.	39 – (-93)

Compute using any method. If mental math is used, write MM. Otherwise show all work.



Compute using any method. If mental math is used, write MM. Otherwise show all work.



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EXPLORING DIFFERENCE AND DISTANCE ON THE NUMBER LINE

Use the number line below as needed for problems 1 – 6 to count the distance between the given points. Recall that distances are always represented by nonnegative numbers.

	-10 -8	-2		
	Points on a line	Distance counted between points	Difference between points	Absolute value of the differences
1.	5 and 8		8-5=	
	0 and 4		5-6=	
2.	0 and 4			
3.	-7 and -5			
4.	-4 and 0			
5.	2 and -9			
6.	3 and 3			

7. The distance between two points on a number line is the ______ of their difference.

For the given pairs of points on a line below, find the distance between them without counting.

8. 25 and 105	930 and -70	10. 50 and -50

11. A bird is flying 50 meters above sea level. A dolphin is swimming 35 meters below sea level. What is the vertical distance between the bird and the dolphin?

PRACTICE 9: EXTEND YOUR THINKING

1. Some ranchers are digging a well. Ground level has an elevation of zero. First write an expression to describe their actions. Then solve the problem.

From ground level, they dig down 13 feet, and then stop for the day. Overnight wind blew 2 feet of dirt back into the hole. The second day, they dig another 9 feet. The third day, they decide the hole is now too deep, and fill in 6 feet of dirt. What is the elevation at the bottom of the well after their work is complete?

Recall that properties like the commutative and associative properties of addition allow us to add numbers in different orders. Use these properties to make the following calculations easier. Describe your process.



Insert plus (+) and minus (-) signs to make the equations true.



REVIEW

COMPARING ADDITION AND SUBTRACTION

Complete the tables below using patterns.

1.

E	kpressi	Sum	
5	+	()	
5	+	()	
5	+	(1)	
5	+	(0)	5
5	+	(-1)	4
5	+	(-2)	
5	+	()	
5	+	()	
5	+	()	
5	+	()	

2.		Expressi	on	Difference
	5	_	()	
	5	_	()	
	5	-	(-1)	
	5	_	(0)	5
	5	-	(1)	4
	5	-	(2)	•
	5	-	(3)	
	5			
	5	-	()	
	5		()	

Complete the problems below based on the results (sums or differences) in the tables above.

3. Under what circumstances are the results less than 5?

Adding a ______ number or subtracting a ______ number.

4. Under what circumstances are the results greater than 5?

Adding a _____ _____ number or subtracting a ______ number.

- 5. What two expressions have a result of 4? _____ and _____
- 6. What two expressions have a result of 8? _____ and _____
- 7. Subtracting 6 from a number gives the same result as adding _____ to it.
- 8. Subtracting -2 from a number gives the same result as adding _____ to it.
- 9. Write the related addition expression for each subtraction expression below.

	a5 – 1	b.	-5 – (-1)	с.	0 - (-1)	
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INTEGER BATTLE



2. Play the subtraction version of Integer Battle. Record two winning hands:



BIG SQUARE PUZZLES: RATIONAL NUMBER ADDITION AND SUBTRACTION

- 1. Complete the Big Square Puzzle(s) provided by your teacher.
- 2. Describe a strategy you use to complete the puzzle(s).

POSTER PROBLEMS: RATIONAL NUMBER ADDITION AND SUBTRACTION

Part 1: Your teacher will divide you into groups.

- Identify members of your group as A, B, C, or D.
- Each group will start at a numbered poster. Our group start poster is
- Each group will have a different colored marker. Our group marker is

Part 2: Do the problems on the posters by following your teacher's directions. Show all computations neatly on the posters.

	ROW	Poster 1 (or 5)	Poster 2 (or 6)	Poster 3 (or 7)	Poster 4 (or 8)
	Ι	$-3\frac{1}{5}+4\frac{3}{10}$	$-\frac{2}{3}+\frac{5}{6}$	-2.8 + 4.35	-0.064 + 0.54
	II	$-3\frac{1}{2}$	$-\frac{3}{4}$	-5.6	-0.51
	III	$1\frac{9}{10}$	$\frac{1}{2}$	6.1	0.056
	IV	$-4\frac{2}{5}$	$-\frac{1}{3}$	-10.1	-0.29
	A. Copy and compute row I.				
	B. Add the number in row II to the result of row I.				
(C. Subtract the number in row III from the result of row II.				
	D. Subtract the number in row IV from the result of row III.				

Part 3: Return to your original poster. Verify computations and correct errors if needed.

Review



VOCABULARY REVIEW

Review

SPIRAL REVIEW

1. **Math Path Fluency Challenge**: Use what you know about decimal operations to find the correct path from Start to Finish.



SPIRAL REVIEW

3. Compute. (Remember: first simplify expressions in grouping symbols, then calculate exponents, then multiply and divide left to right, and finally add and subtract left to right).

a.	$6^{2} + 2\left(7 - \frac{15}{5}\right)$	b. $25-5\left(\frac{10\cdot 2}{4}\right)$
C.	$(2 + 3)^2 - 24$	d. $48-3^2(5)+10$
Simpli	fy.	
a.	3x + 5y + 2y	b. $3(f+3) - f$
C.	4(w + 3) + 2(4 - w)	d. a+a-a+b+b
Evalua	ate for $x = 3$ and $y = 5$.	
a.	2x + 2y	b. $x + x + x + y$
C.	20x - 2y	d. $\frac{6}{x} + 5y$

6. JM buys \$58.20 worth of schools supplies to donate to the local after school program. JM receives a 35% discount on the purchase.

a. What is the discounted price of the school supplies?	b. JM pays 9.25% tax on the discounted price. What is the total that JM spent?

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4

REFLECTION

1. **Big Ideas**. Shade all circles that describe big ideas in this unit. Draw lines to show connections that you noticed.



Give an example from this unit of one of the connections above.

- 2. Unit Progress. Go back to Monitor Your Progress on the cover and complete or update your responses. Explain something you understand better now than before.
- 3. **Mathematical Practices.** Suppose you were asked to explain how to add integers to a younger student. What model or strategy would you use, and why? Give an example and explain in words [SMP3, 5]. Then circle one more SMP on the back of this packet that you think was addressed in this unit and be prepared to share an example.

4. **Making Connections.** Why do you think that some students may have a misconception that subtraction makes things smaller? Give an example that might correct this misconception.

STUDENT RESOURCES

Word or Phrase	Definition
absolute value	The <u>absolute value</u> $ x $ of a number x is the distance from x to 0 on the number line.
	2 = 2 and $ -2 = 2$, because both 2 and -2 are 2 units from 0 on the number line. 2 units 2 units -1 0 1
addend	See <u>sum</u> .
additive identity property	The <u>additive identity property</u> states that $a + 0 = 0 + a = a$ for any number a . In other words, the sum of a number and 0 is the number.
	We say that 0 is an <u>additive identity</u> . The additive identity property is sometimes called the <u>addition property of zero</u> . 3 + 0 = 3, 0 + 7 = 7, -5 + 0 = -5 = 0 + (+5)
additive inverse	The <u>additive inverse</u> of <i>a</i> is the number <i>b</i> such that $a + b = b + a = 0$. The additive inverse of <i>a</i> is denoted by <i>-a</i> . -4 is the additive inverse of 4.
additive inverse	The additive inverse property states that $a + (-a) = 0$ for any number a. In other words,
property	the sum of a number and its opposite is 0. The number $-a$ is the additive inverse of a . 3 + (-3) = 0, -5 + 5 = 0
difference	In a subtraction problem, the <u>difference</u> is the result of subtraction. The <u>minuend</u> is the number from which another number is being subtracted, and the <u>subtrahend</u> is the number that is being subtracted. 12 - 4 = 8 minuend subtrahend difference
integers	The <u>integers</u> are the whole numbers and their opposites. They are the numbers 0, 1, 2, 3, and -1, -2, -3,
minuend	See <u>difference</u> .
negative numbers	<u>Negative numbers</u> are numbers that are less than zero, written $a < 0$. The negative numbers are the numbers to the left of 0 on a horizontal number line, or below zero on a vertical number line.
	The numbers -2, -4.76, and $-\frac{1}{4}$ are negative.
	The numbers 2 and 5.3, and 0 are NOT negative.

Word or Phrase	Definition		
opposite of a number	The <u>opposite of a number</u> n , written $-n$, is its additive inverse. Algebraically, the sum of a number and its opposite is zero. Geometrically, the opposite of a number is the number on the other side of zero at the same distance from zero.		
	The opposite of 1 is -1, because $1 + (-1) = -1 + 1 = 0$. The opposite of -1 is $-(-1) = 1$. Thus, the opposite of a number does not have to be $-1 0 1$ negative.		
positive numbers	Positive numbers are numbers that are greater than zero, written $a > 0$. The positive numbers are the numbers to the right of 0 on a number line, or above zero on a vertical number line.		
	The numbers 3, 2.6, and $\frac{3}{7}$ are positive.		
	The numbers $-3, -2.6, -\frac{1}{7}$, and 0 are NOT positive.		
rational numbers	Rational number are numbers expressible in the form $\frac{m}{n}$, where <i>m</i> and <i>n</i> are integers, and $n \neq 0$.		
	$\frac{3}{5}$ is rational because it is a quotient of integers.		
	$2\frac{1}{3}$ and 0.7 are rational numbers because they can be expressed as quotients of		
	integers, namely $\frac{7}{3}$ and $\frac{7}{10}$, respectively.		
	$\sqrt{2}\;$ and $\;\pi\;$ are NOT rational numbers. They cannot be expressed as a quotient of integers.		
subtrahend	See <u>difference</u> .		
sum	A <u>sum</u> is the result of addition. In an addition problem, the numbers to be added are <u>addends</u> . 7 + 5 = 12 addend addend sum		
whole numbers	The <u>whole numbers</u> are the natural numbers together with 0. They are the numbers $0, 1, 2, 3,$.		
zero pair	In the counter model, a positive and a negative counter together form a zero pair.		
	Let + represent a positive counter and		
	let - represent a negative counter.		
	Then the figure to the right is an example of a collection of (three) zero pairs.		

Mr. Mortimer's Magic Cubes Mr. Mortimer discovered an amazing way to control the temperature of liquid. He invented magic hot and cold cubes to change the liquid's temperature. These magic cubes never melt or change in any way. For example, ice cubes melt, but magic cold cubes do not. Hot Cubes (the basics): If you add 1 hot cube to a liquid, the liquid heats up by 1 degree. • If you remove 1 hot cube from the liquid, the liquid cools down by 1 degree. • Cold Cubes (the basics): If you add 1 cold cube to the liquid, the liquid cools down by 1 degree. • If you remove 1 cold cube from the liquid, the liquid heats up by 1 degree. • For 1 cube How this temperature change model works Put in Heat add (+1) \rightarrow Hotter +(+1) = +1 \rightarrow Hot Cubes Positive (+) **Remove Heat** \rightarrow Colder subtract $(+1) \rightarrow -(+1) = -1$ Put in Cold Colder add (-1) \rightarrow +(-1) = -1 **Cold Cubes Negative** (–) Remove Cold subtract (-1) \rightarrow -(-1) = +1 Hotter Here are a few examples to show temperature change using magic hot and cold cubes. Simplest ways: **Other Ways:** Put in 6 hot cubes Remove 6 cold cubes Remove 4 cold Put in and and 4 hot cubes cubes put in 2 cold cubes remove 2 hot cubes +4 degrees +(+4) = 4(-4) = 4+(+6) + (-2) = 4-(-6) - (+2) = 4Remove 3 hot cubes Put in 3 cold cubes Remove 2 hot cubes Put in 2 cold cubes and and remove 1 cold cube put in 1 hot cube -2 degrees -(+2) = -2+(-2) = -2-(+3) - (-1) = -2+(-3) + (+1) = -2Put in 4 hot cubes Remove 3 hot cubes Do nothing and and remove 3 cold cubes put in 4 cold cubes 0 degrees 0 +(+4) + (-4) = 0-(+3) - (-3) = 0





Rules for Addition of Integers

Rule 1: When the addends have the same sign, add the absolute values. Use the original sign in the answer.

Rule 2: When the addends have different signs, subtract the absolute values. Use the sign of the addend with the greatest absolute value in the answer.



In words, the result is the same whether subtracting a quantity or adding its opposite.

Examples: 6 - 4 = 6 + (-4) = 2

-3 - (-2) = -2 + 2 = -1



COMMON CORE STATE STANDARDS

	STANDARDS FOR MATHEMATICAL CONTENT				
7.NS.A	Apply and extend previous understandings multiply, and divide rational numbers.	of operations with fractions to add, subtract,			
7.NS.1	Apply and extend previous understandings of a numbers; represent addition and subtraction or	addition and subtraction to add and subtract rational n a horizontal or vertical number line diagram.			
а	Describe situations in which opposite quantities has 0 charge because its two constituents are	s combine to make 0. For example, a hydrogen atom oppositely charged.			
b	Understand $p + q$ as the number located a distance depending upon whether q is positive or negation of 0 (are additive inverses). Interpret sums of rates	ance $ q $ from p , in the positive or negative direction ve. Show that a number and its opposite have a sum ational numbers by describing real-world contexts.			
С	Understand subtraction of rational numbers as that the distance between two rational numbers difference, and apply this principle in real-world	adding the additive inverse, $p - q = p + (-q)$. Show s on the number line is the absolute value of their contexts.			
d	Apply properties of operations as strategies to	add and subtract rational numbers.			
7.SP.C	Investigate chance processes and develop,	use, and evaluate probability models.			
7.SP.7	Develop a probability model and use it to find p	probabilities of events.			
b	Compare probabilities from a model to observe possible sources of the discrepancy: Develop a	ed frequencies; if the agreement is not good, explain a probability model (which may not be uniform) by			
	observing frequencies in data generated from a probability that a spinning penny will land head down. Do the outcomes for the spinning penny frequencies?	a chance process. For example, find the approximate s up or that a tossed paper cup will land open-end appear to be equally likely based on the observed			
7.SP.8	Find probabilities of compound events using or	ganized lists, tables, tree diagrams, and simulation:			
а	Understand that, just as with simple events, the outcomes in the sample space for which the co	e probability of a compound event is the fraction of mpound event occurs.			
STANDARDS FOR MATHEMATICAL PRACTICE					
SMP1	Make sense of problems and persevere in so	blying them.			
SMP2	Reason abstractly and guantitatively.				
SMP3	Construct viable arguments and critique the r	reasoning of others.			

- SMP4 Model with mathematics.
- SMP5 Use appropriate tools strategically.
- SMP6 Attend to precision.
- SMP7 Look for and make use of structure.
- SMP8 Look for and express regularity in repeated reasoning.

