Name_____

Period _____ Date _____

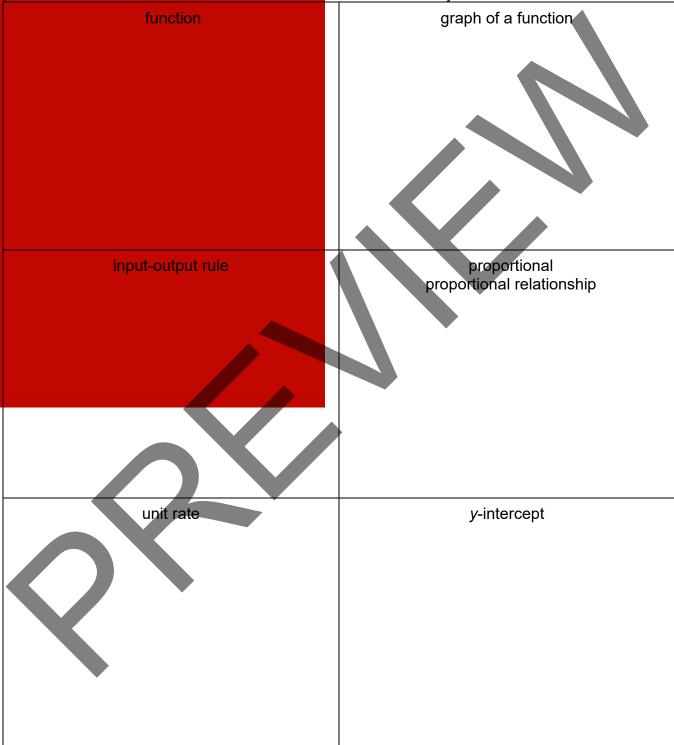
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UNIT 4 STUDENT PACKET	GRADE 8	1			И	ks
INTRODUCTIO	N TO FUNCTIONS					
			Mor Yo 'rog	our		Page
My Word Bank						0
4.0 Opening Problem: Slides and Jump	bs					1
 4.1 Multiple Representations Represent a situation with words, pict equations. 		3	2	•	0	2
Recognize when a graph is linear or in decreasing.		3	2	1	0	
 Understand when a situation describe Explore the meaning of initial values a graphs, and equations. 		3 3	2 2	1	0 0	
 4.2 Function Representations Understand the definition of a function Determine if a representation is a function 		3 3	2 2	1 1	0 0	11
 4.3 Rate Representations Represent and interpret rate situation tables, graphs, and equations. 	s with words, pictures,	3	2	1	0	18
Review						25
Student Resources						33

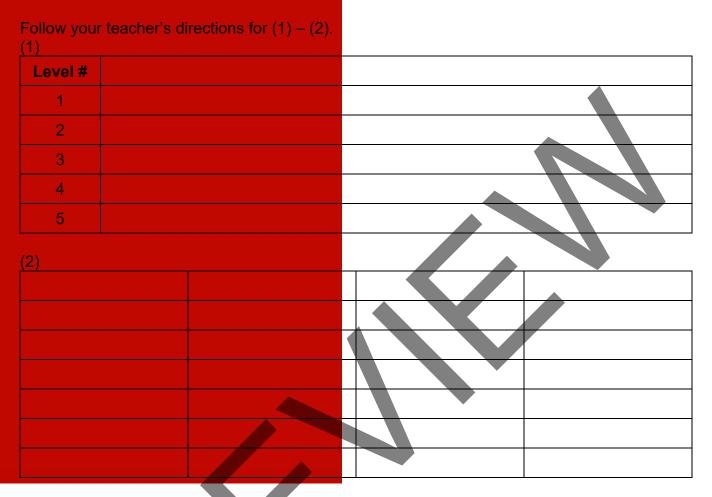
Parent (or Guardian) signature _____

MY WORD BANK

Explain the mathematical meaning of each word or phrase, using pictures and examples when possible. See **Student Resources** for mathematical vocabulary.



SLIDES AND JUMPS



3. Record the missing values in the table below. Show your work on this page as needed.

Level #	# of Slides	# of Jumps	Total # of Moves
10			
	40		
-25			
	100		
		10,000	
1,000			
			n ² + 2n

MULTIPLE REPRESENTATIONS

We will use words, pictures, tables of numbers, and graphs to represent, describe, and analyze situations involving area and money.

[8.EE.5, 8.F.2, 8.F.3, 8.F.4; SMP1, 2, 3, 4, 7, 8]

GETTING STARTED

Fill in missing numbers and blanks based on the suggested numerical patterns. In the tables below, the *x*-value is considered the input value (independent variable) and the *y*-value is the output value (dependent variable).

			Tabl	e I			
1.	x	1	2		4	6	
	У	4	8	12		20	

- a. Rate of change: for every increase of x by 1, y increases by ____.
- b. Input-output rule (words): multiply the x-value by _____ to get the corresponding y-value.
- c. Input-output rule (equation): *y* = _____

. When x = 0, y =___.

- Table II

 2.
 x
 1
 3
 5
 6

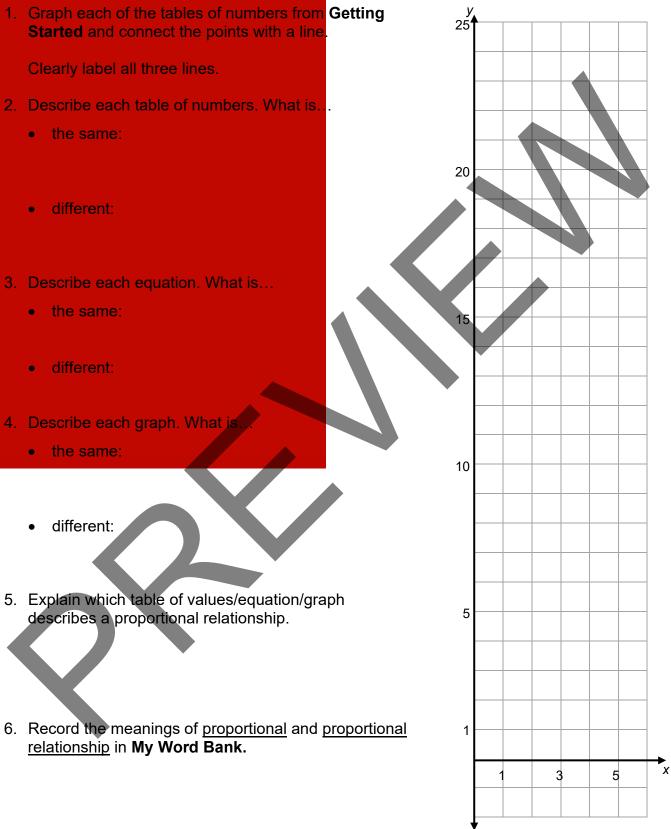
 y
 5
 9
 17
 25
 - a. Rate of change: for every increase of x by 1, y increases by ____.
 - b. Input-output rule (words): multiply the *x*-value by ____, then _____ to get the corresponding *y*-value.
 - c. Input-output rule (equation): y =_____. When x = 0, y =____.

		Table	III			
3. x	1	2		4	5	
У	3		11		19	23

- a. Rate of change: for every increase of x by 1, y increases by ____.
- b. Input-output rule (words): multiply the *x*-value by ____, then _____ to get the corresponding *y*-value.
- c. Input-output rule (equation): y =____. When x = 0, y =___.

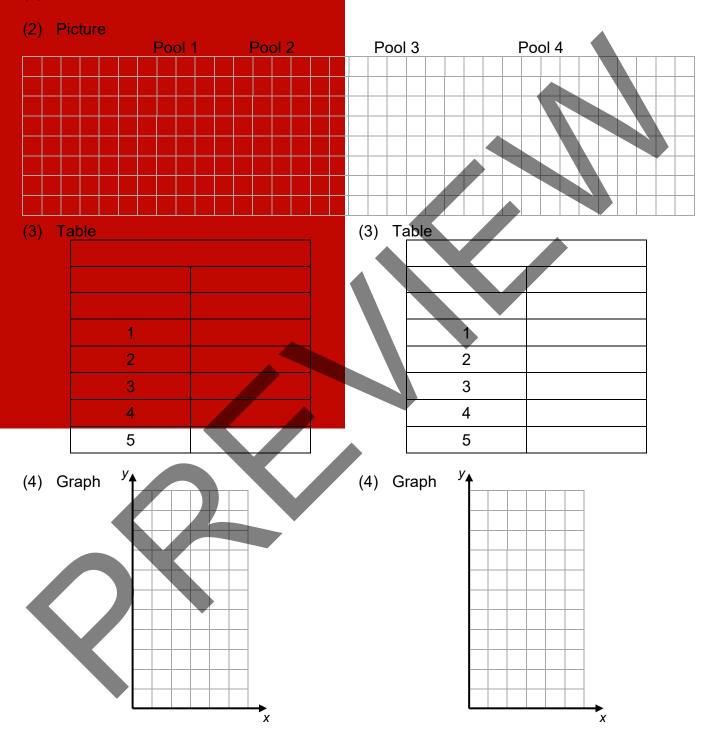
4. Record the meaning of <u>input-output rule</u> in **My Word Bank**.

INTERPRETING TABLES, EQUATIONS AND GRAPHS





Follow your teacher's directions. (1)



ANALYZING THE POOL PROBLEM

Refer to The Pool Problem.

1. Draw and label "Pool 0" in the space to the left of Pool 1. How is it different from the other pools?

Water:

b. Water:

- 2. In the top row of the tables, write the entries for Pool 0. Graph the points for Pool 0.
- 3. When does the Border Pattern have more squares than the Water Pattern?

When does the Water Pattern have more squares?

- 4. Write equations to represent the number of squares for each pool number.
 - a. Border:
- 5. Write the number of squares for each pattern for Pool 20.
 - a. Border:
- 6. Which pool has 48 border squares and 121 water squares?
- 7. Explain what (0, 4) and (0, 0) represent in the context of The Pool Problem.

Where are these points found on the graphs?

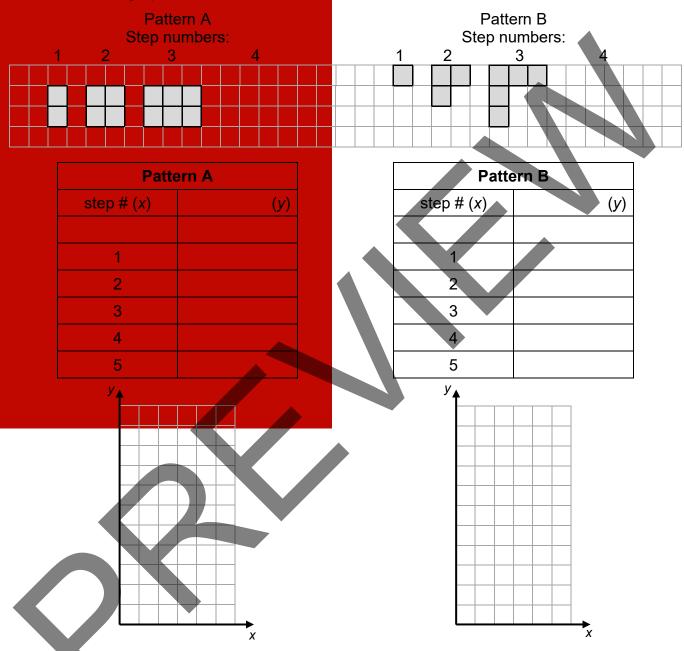
8. Does the Border Pattern grow at a constant rate? Explain.

Does it represent a proportional relationship? Explain.

9. Does the Water Pattern grow at a constant rate? Explain.

Does it represent a proportional reationship? Explain.

1. Below are two different square patterns. Draw the 4th step for each pattern. Fill in the tables. Draw graphs with titles and labels.



- 2. If not already done, write the entries for step 0 in the top row of the tables.
- 3. Given the pictures and numbers, does "step 0" make sense for either pattern?
- 4. Graph a point for step 0 only if it makes sense for the pattern.

b. Pattern B:

- 5. Write equations to represent the number of squares for each pattern.
 - a. Pattern A:
- 6. For Pattern A, find...
 - a. The number of squares in step 80
- 7. For Pattern B, find...
 - a. The number of squares in step 70
- b. The step number for 200 squares:
- b. The step number for 101 squares:
- 8. Consider the tables, graphs, and rules used to represent both patterns.
 - a. List some things that are the same for both
 - b. List some things that are different for both.
- 9. Why does Pattern A represent a proportional relationship, while Pattern B does NOT?
- 10. For both patterns:
 - a. In the tables, as the x-value increases by 1, the y-value increases by _____.
 - b. On the graphs, the *y*-coordinate moves up by _____ as the *x*-coordinate moves right by 1.
 - c. For the equations, the coefficient of *x* is _____.

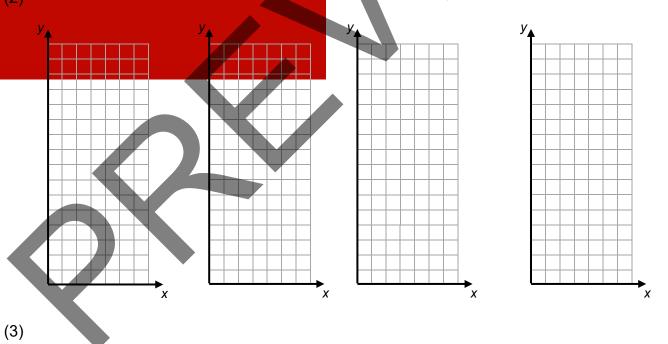
4.1 Multiple Representations

SAVING VS SPENDING

Follow your teacher's directions for (1) - (3).

(1)				
	Mateo	Dion	Talia	Ayla
0	0		140	
1	20	30		130
2	40	50		105
		70	80	80
4			60	
				30
	120	130	20	5
7	140	150		





4. Record the meaning of <u>*y*-intercept</u> in **My Word Bank**.

ANALYZING SAVING VS SPENDING

Refer to **Saving vs Spending** on the previous page. As a convention, we read graphs from left to right.

1. For which students do table values and graphs appear to be increasing?

Decreasing?

2. Compare tables and graphs for pairs of students.

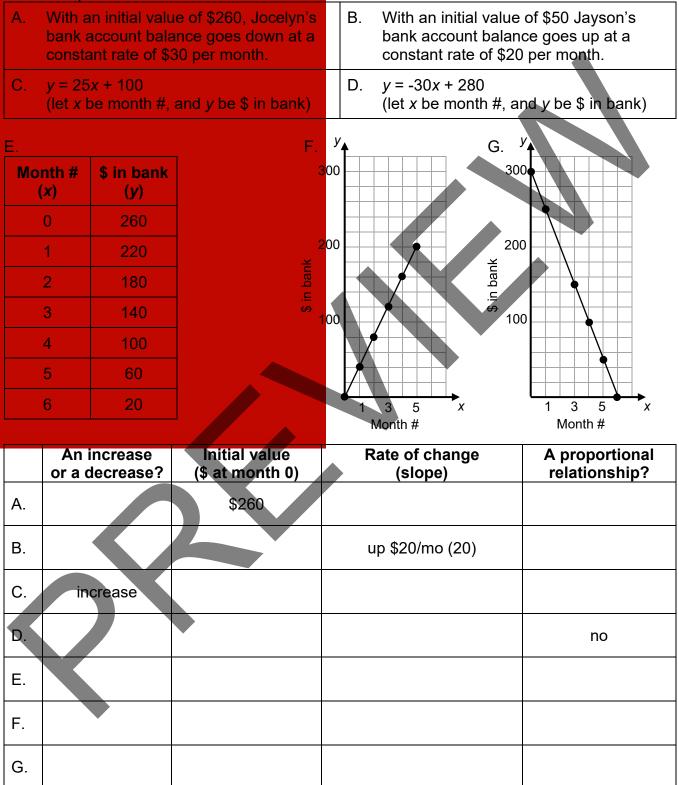
	How are they the same?	How are they different?
Compare: Mateo and Dion	How are they the same?	
Dion and Talia		
		
Talia and Ayla		

3. How do initial amounts (in these cases, this is Month 0) appear to be shown in the equations?

4. How do rates of change (slope) appear in the equations?

5. Do any of these situations represent a proportional relationship? Explain.

Use the representations A – G to fill in the table below.



FUNCTION REPRESENTATIONS

We will explore the concept of a function. We will define function and graph of a function. We will describe examples of functions and examples of non-functions.

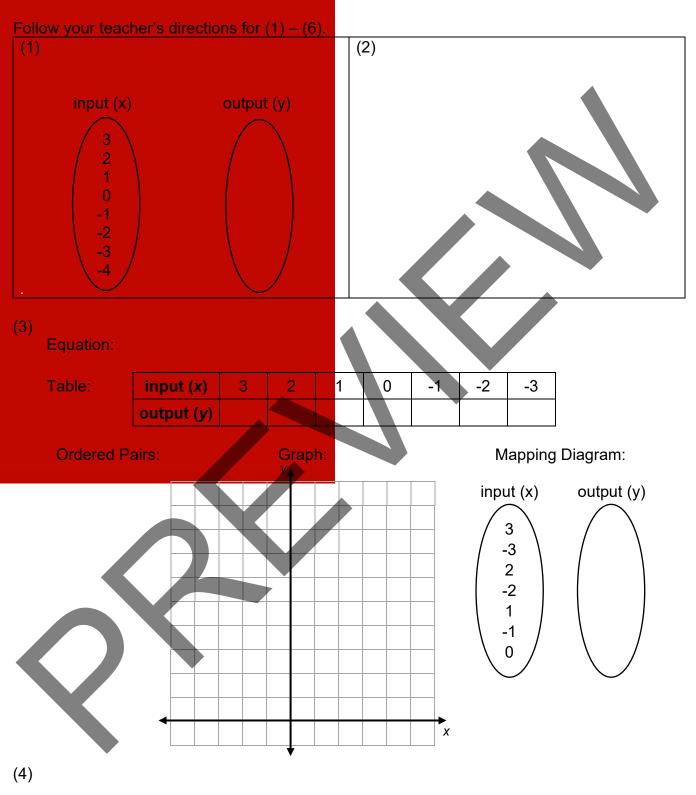
[8.F.1, 8.F.3, 8.F.5; SMP1, 2, 4, 5, 6]

GETTING STARTE	D	
 Refer to the table to the right about Super Bowl champions in the 1970s. 	Year	Super Bowl Champion
a. Which team(s) won exactly once?	1970	Kansas City Chiefs
	1971	Baltimore Colts
b. Which team(s) won exactly twice?	1972	Dallas Cowboys
	1973	Miami Dolphins
c. Which team(s) won exactly three times?	1974	Miami Dolphins
	1975	Pittsburgh Steelers
d. If you are given a specific year (input), can you	1976	Pittsburgh Steelers
always tell which team won (output)?	1977	Oakland Raiders
Give an example.	1978	Dallas Cowboys
	1979	Pittsburgh Steelers
e If you are given a specific team (input) can you alw	ave tell w	hich one year they won

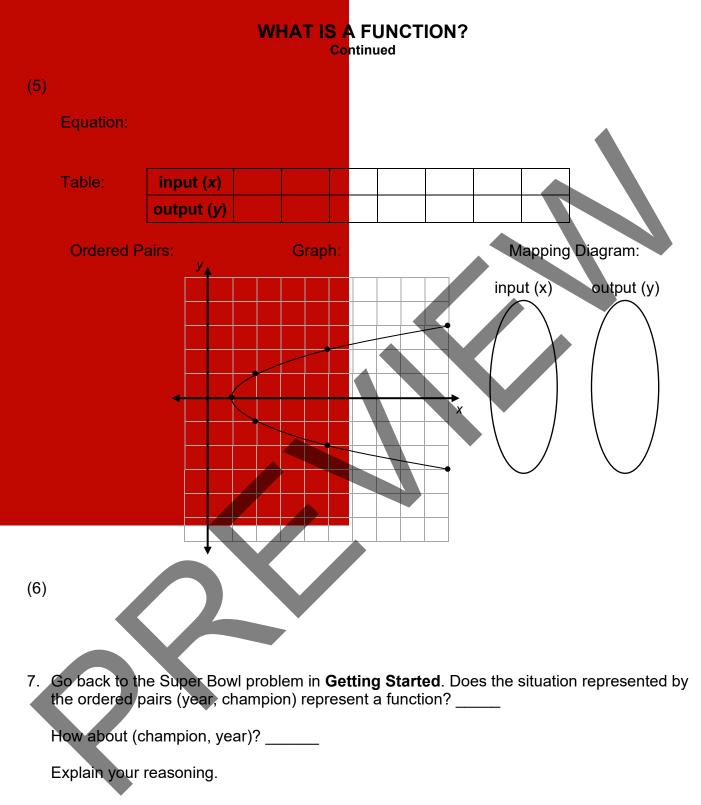
e. If you are given a specific team (input), can you always tell which one year they won (output)? _____ Give an example.

2. For the equation y = x + 1, fill in the table, write ordered pairs to correspond with table entries, and draw a graph.

Table: input (x)	3	2	1	0	-1	-2	-3	
output (y)								
Ordered Pairs:			Graph:			У_		
				•				x



WHAT IS A FUNCTION?



8. Record the meanings of <u>function</u> and <u>graph of a function</u> in **My Word Bank**.

Innut

Mapping diagram

PETS AND APARTMENTS

Mary has three pets, Kerry has one pet, and both Larry and Barry have no pets.

Let friend names be the input values.

Output

Let the number of pets they each own be the output values.

1. Represent this situation with an input-output table, ordered pairs, and a mapping diagram.

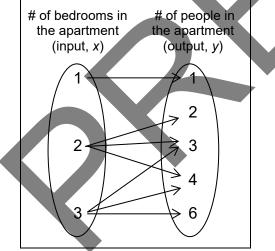
Ordered pairs

	Output
Name	
Mary	
Kerry	
Larry	
Barry	

2. Explain why this situation represents a function.

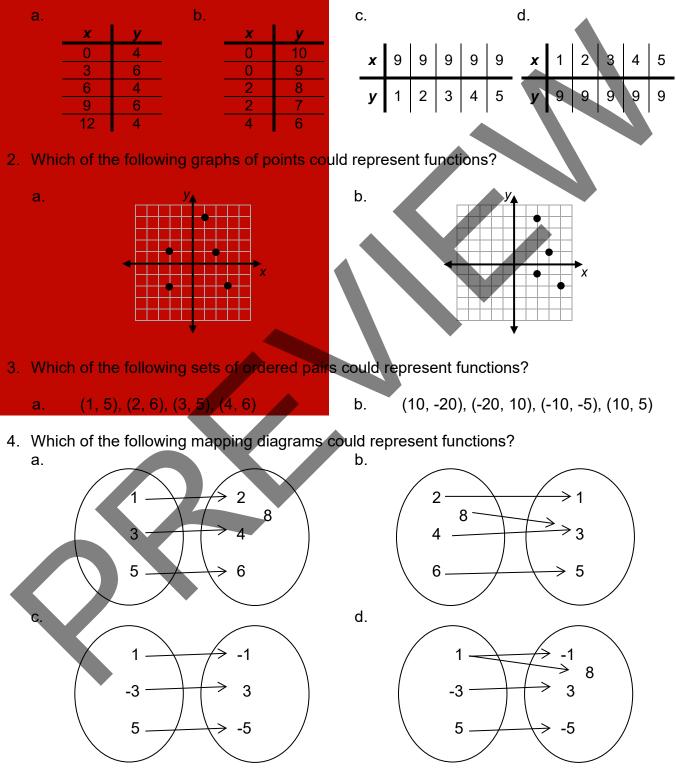
The mapping diagram below shows the number of bedrooms in an apartment building and the number of people who live in the apartment.

3. Create a table, write ordered pairs, and draw a graph for this situation.



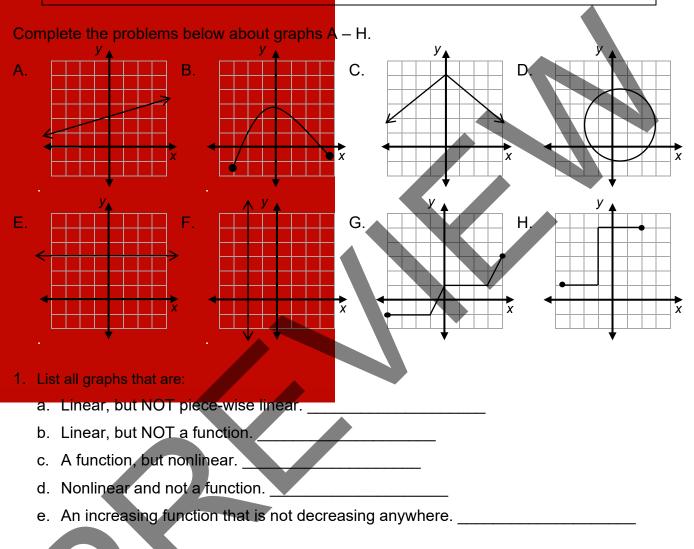
4. Does this situation represent a function? Explain.

1. Which of the following input-output tables could represent functions when x is used for the input value and y for the output value?



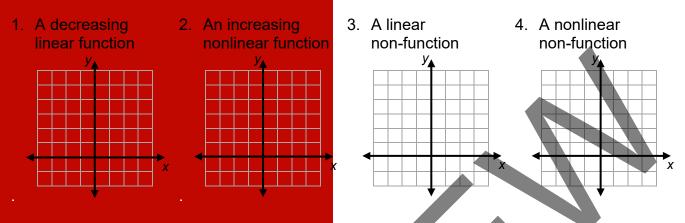
MathLinks: Grade 8 (2nd ed.) ©CMAT Unit 4: Student Packet

We say a function is **increasing** if a graph of the output values increases from left to right, and **decreasing** if a graph of the output values decreases from left to right. **Piece-wise** linear functions are considered to be linear.

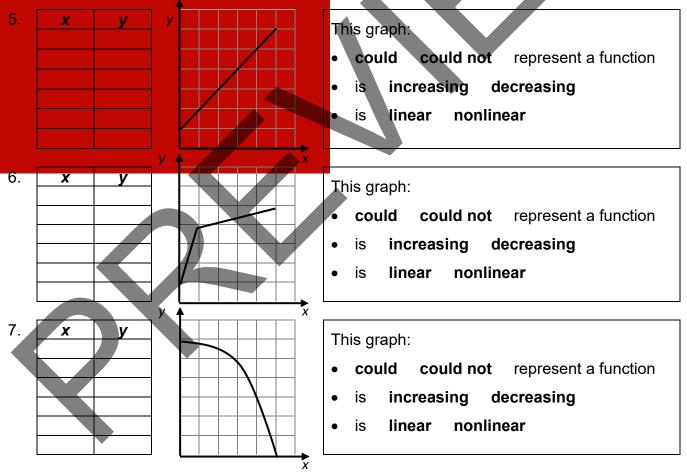


- 2. Describe where the graph of C is increasing and where it is decreasing.
- 3. The graph of G has four line segments. How many of them are increasing? Circle those segments on the graph.

Draw the four graphs as described.



Estimate appropriate ordered pairs for each graph. Circle one **bold** choice for each bulleted statement.



8. Describe the change you observe in the table and graph in problem 7.

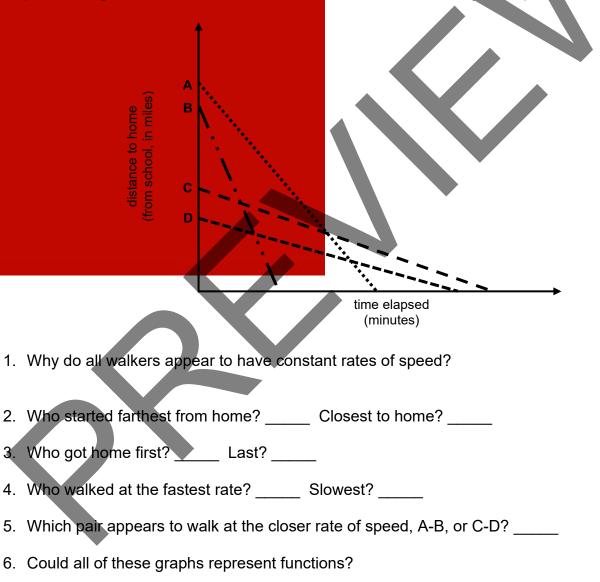
RATE REPRESENTATIONS

We will use words, tables of numbers, equations, and graphs to represent rates. We will compare representations of functions.

[8.EE.5, 8.F.1, 8.F.2, 8.F.3, 8.F.4, 8.F.5; SMP1, 2, 3, 4, 5, 7, 8]

GETTING STARTED

Andre, Bethany, Claudia, and Derek all walked home from school today to each of their respective homes. The graph below shows the distance from school to home, and the time elapsed during their walks. Use the letters A, B, C, and D to identify each person.



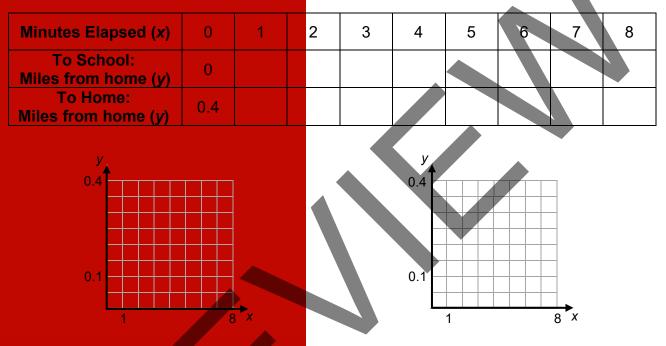
7. Which of these graphs are increasing and which are decreasing?

TO SCHOOL AND BACK HOME

Nellie walks to school each morning at a constant rate of 0.05 miles per minute, and jogs home in the afternoon at a constant rate of 0.08 miles per minute.

School and home are $\frac{4}{10}$ of a mile apart.

1. Fill in both columns in the table below and draw graphs based upon the given data.



- 2. Why does it make sense to draw lines for the graphs with this context?
- 3. Which graph is increasing? _____ Decreasing? _____
- 4. Does either one of these situations represent a proportional relationship? Explain.
- 5. For walking to school, what is the unit rate?
- 6. Write an equation for each situation.
 Walking to school: ______ Jogging home: ______

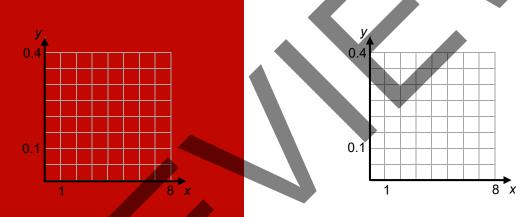
TO SCHOOL AND BACK HOME

Continued

Nellie's brother, Willie, lives in the same house, goes to the same school, and he also walks there and jogs back.

- His "jogging home" data is in the table below
- The equation that represents his walk to school is y = 0.04x
- 7. Fill in the rest of the table below and draw graphs based on the given data.

Minutes Elapsed (<i>x</i>)	0	1	2	3	4	5	6	7	8
To School: Miles from home (<i>y</i>)	0								
To Home: Miles from home (<i>y</i>)	0.4	0.3	0.2	0.1	0	N/A	N/A	N/A	N/A



8. For walking to school, what is the unit rate?

What does an initial value of x = 0 mean?

- 9. Write an equation for jogging home.
- 10. Who walked to school at a faster rate? Explain.
- 11. Who jogged home at a faster rate? Explain.

Below is information for four different cyclists, Tamika, Vinnie, Wanda, and Zach, all of whom ride at constant rates of speed. Use the letters T, V, W and Z to identify each person.

Let *x* be time elapsed in hours (hr) and *y* be distance traveled in miles (mi).

One representation is given for each. Complete the remaining representations in any order

1. W	ord de	scriptions						
т	Tamił	ka rides at	t a constai	nt rate o	f 18 miles	per hour.		
V								
w								
z								
2. E	ntries ir	n the table	e and equa	ations.				
-	X	0	1	2	3	4	5	
	у							
								,
V	X	0	1	2	3	4	5	
	у	0	15	30	<mark>4</mark> 5	60	75	
							I	
W	X	0	1	2	3	4	5	v = 10v
vv	у							y = 12x
						-		·
-	x	0	1	2	3	4	5	
Z	У							
3. G	raphs			4. \	Nhat are t	he initial v	alues (<i>y</i> -i	ntercepts) for each rider?
		Cyclist Rat	8	C		r each rid		per hour (rates of e do you see these rates

6. How are the graphs of the fastest and slowest riders different?

1 hours MathLinks: Grade 8 (2nd ed.) ©CMAT Unit 4: Student Packet

miles

10

Ζ

×

4 min

Monday

2 min

PRACTICE 7

1,200 yd

400 yd

0

Chris went jogging in the park on Monday.

- 1. Could Chris' graph represent a function?
- 2. Does it appear to be linear?
- 3. Is it increasing or decreasing?
- 4. Use the Monday graph to the right to complete the table below.

Time Period	Number of Minutes	Yards Traveled	Average Rate of Speed
From 0 to 2 minutes			
From 2 to 4 minutes			
From 0 to 4 minutes			

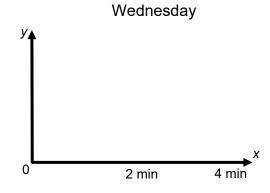
5. In what part of the jog did Chris run faster, the initial two minutes or the last two minutes? Explain by referencing numbers and the shape of the graph.

Chris went jogging in the park again on Wednesday.

6. Complete the table below, and sketch and label a graph.

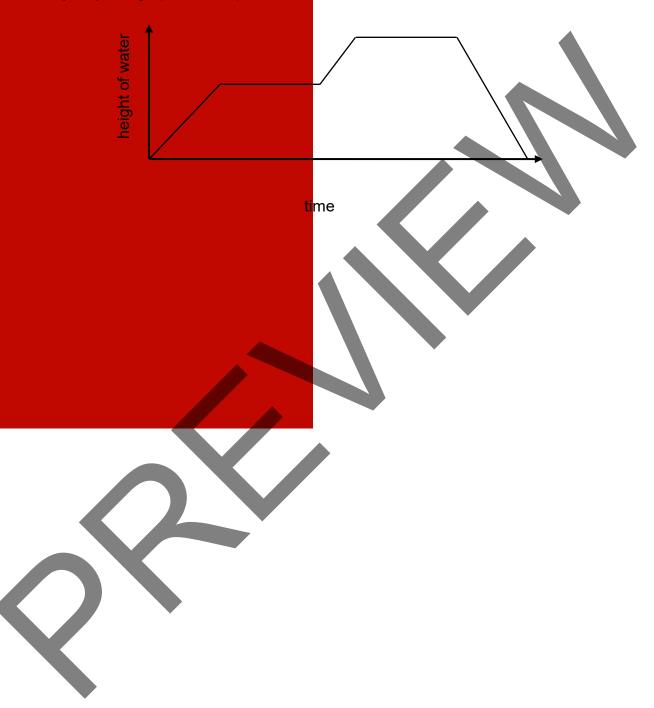
Time Period	Number of Minutes	Yards Traveled	Average Rate of Speed
From 0 to 2 minutes	2	600	
From 2 to 4 minutes	2	200	
From 0 to 4 minutes			

7. In what part of the jog did Chris run faster, the initial two minutes or the last two minutes? Explain by referencing numbers and the shape of the graph to the right.



THE BATH GRAPH

Write several sentences to explain what story this graph could be telling. Explain in the context of the story why this graph must represent a function.

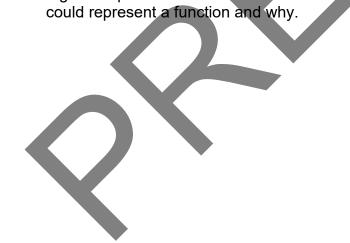


THE ROLLERCOASTER

- Draw a reasonable graph for a typical rollercoaster ride, based on the following information. Label each section by letter (each segment or curved portion of your graph) based upon the descriptions below, A – F. Note that the vertical axis represents speed, NOT HEIGHT.
 - A. The rollercoaster starts slowly and gradually builds speed.
 - B. It comes to a hill and climbs up slowly.
 - C. It races downhill.
 - D. It does a full loop.
 - E. It continues at a constant speed.
 - F. It gradually comes to a stop.

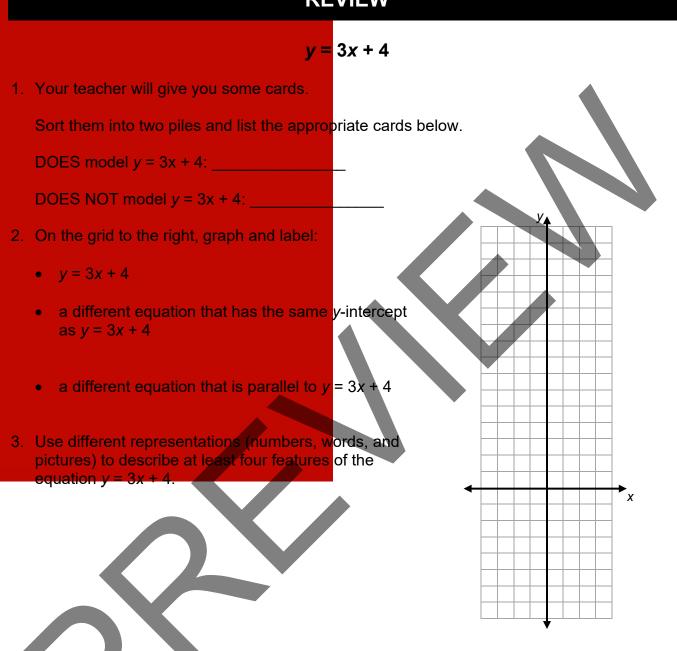






Introduction to Functions

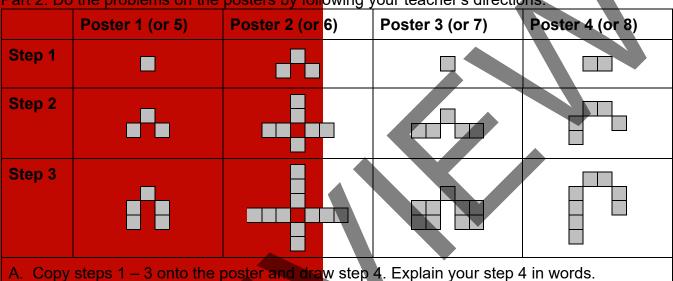
REVIEW



Part 1: Your teacher will divide you into groups.

- Identify members of your group as A, B, C, or D.
- Each group will start at a numbered poster. Our group start poster is _
- Each group will have a different colored marker. Our group marker is _

Part 2: Do the problems on the posters by following your teacher's directions.



B. Make a table, label it appropriately, and record values for steps 0 through 5. Make note of the initial value and the rate of increase.

C. Make a graph and label it appropriately.

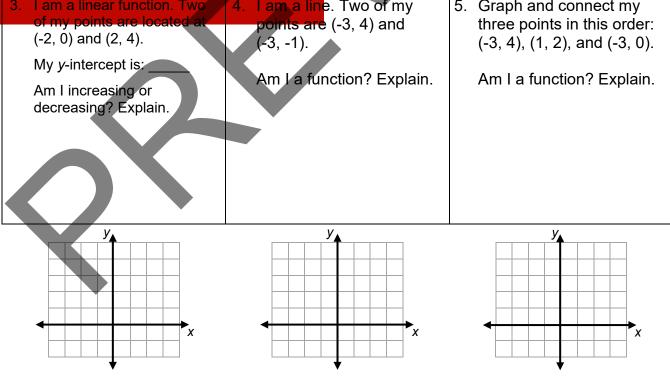
D. Write an input-output rule that relates the total number of tiles to the step number, and then find the number of tiles for step 100.

Part 3: Return to your seats. Work with your group, and show all your work.

- 1. The ordered pair (1, 1) is on both Posters 1 and 3. What does it represent?
- 2. Find the step number that has exactly 155 tiles in poster 2.
- 3. Find the step number that has exactly 185 tiles in poster 4.
- 4. What does the *y*-intercept mean in each poster?

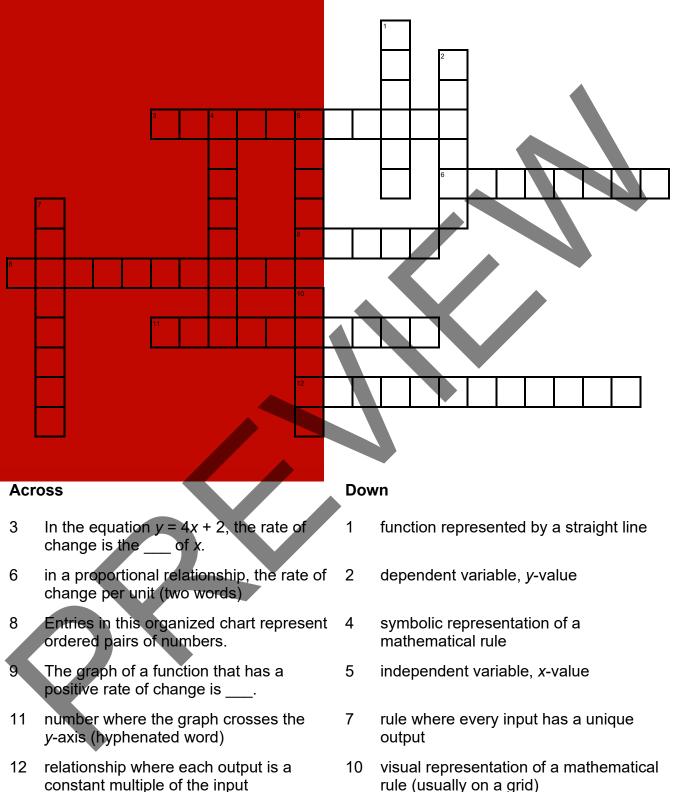
WHY DOESN'T IT BELONG?: INTRODUCTION TO FUNCTIONS

A. Table:		B. Equation:	y = -2x + 1	D. Graph
Input (x)	Output (y)			<i>Y</i>
0	0	C. Context:		
1	1		ds to and from wo	
2	4		rage rate of 6 mile	
3	9		this information to ar he travels after	
4	16	number of ho		
 Avoid the obvious differences, such as "It's a graph." 1. Choose one representation A – D above and explain why it does not belong with the others. 2. Now choose a different representation and explain why it does not belong. 				
Graph each	of the describ	ed situations below	, answer the ques	tions, and explain.
	ear function. T		e. Two of my e (-3, 4) and	5. Graph and connect my three points in this order:
(-2, 0) an		(-3, -1).		(-3, 4), (1, 2), and (-3, 0).
My y-inte	rcept is:			



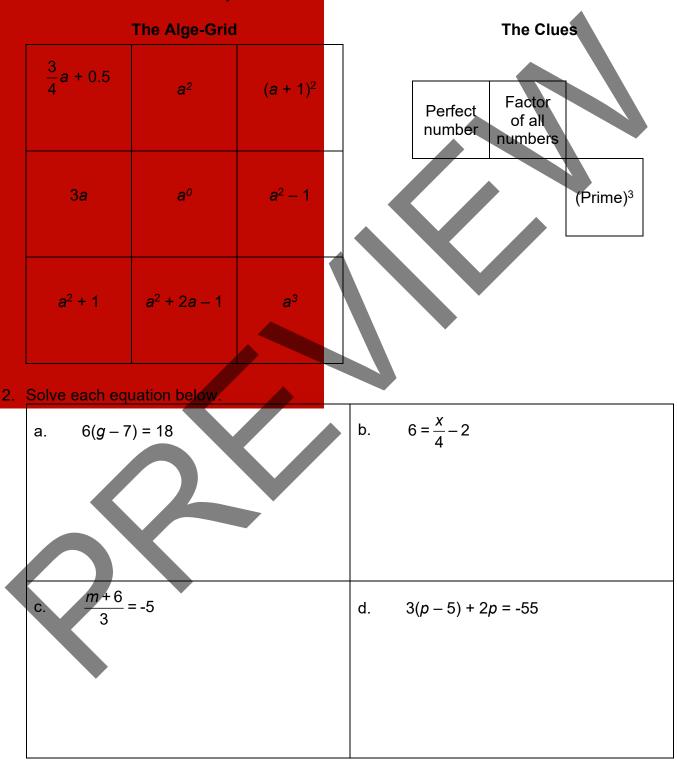
Review





SPIRAL REVIEW

1. Alge-Grid: What's the a? Each clue gives the value of a corresponding cell. Use clues to find *a*, which has the same value in all cells. Once evaluated, the cells will contain the whole numbers 1 – 9, exactly once each.



Introduction to Functions

Review

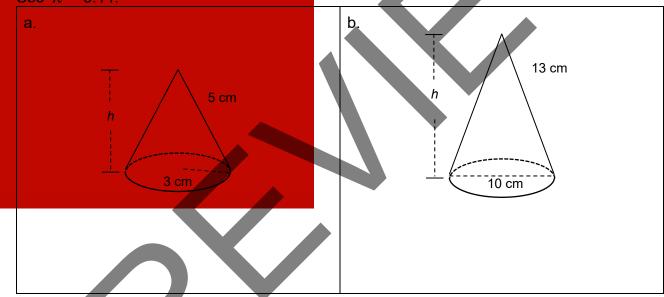
10 cm

12 cm

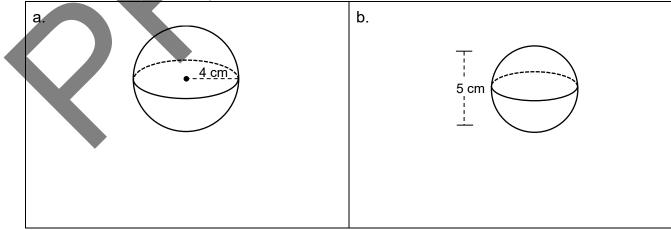
SPIRAL REVIEW

Figures not drawn to scale.

- 3. Find the height and the volume of the cone to the right if the diameter is 12 cm and the slanted edge is 10 cm. Round to the nearest tenth. Use π = 3.14.
- 4. Find the height and the volume of each cone below. Round to the nearest tenth. Use $\pi = 3.14$.



5. Find the volume of each sphere below. Use π = 3.14. Round to the nearest hundredth.



SPIRAL REVIEW

6. Solve and show your work.

A store is having a sale on bikes. The original cost of a bike that Epic wants to buy is \$190.

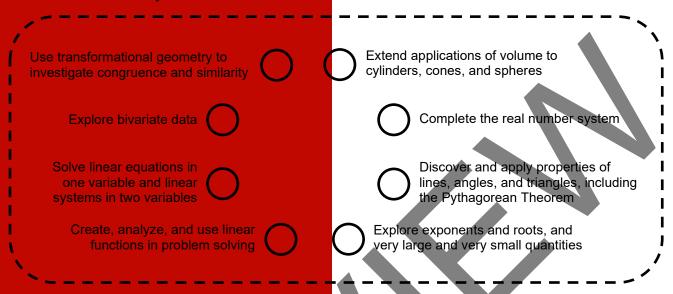
a. If the bike is marked down to \$110, what is the percent discount?
b. Sales tax in this location is 9.6%. What is the sales tax amount for the discounted bike?
c. Epic has \$125 to spend on the bike. Will this be enough money? Explain.

7. Compute

1.	Compute			
	a. 4 ⁻² • 4 ³	b. 5 ⁷ • 5 ⁻⁷	C.	3 ⁻² • 3 ⁻³ • 3 ⁸
	d. $(2^3)^4 \cdot (4^2)^{-3}$	e. $\frac{10^5 \cdot 10^8}{10^{10}}$	f.	∛27
	g. ∛–27	h. $\left(\sqrt{25}\right)\left(\sqrt{4}\right)$	i.	$\left(\frac{\sqrt{36}}{\sqrt{16}}\right)$

REFLECTION

1. **Big Ideas**. Shade all circles that describe big ideas in this unit. Draw lines to show connections that you noticed.



Give an example from this unit of one of the connections above.

- 2. Unit Progress. Go back to Monitor Your Progress on the cover and complete or update your responses. Explain something you understand better now than before.
- 3. **Mathematical Practice.** Explain how you used multiple representations to model and analyze relationships [SMP4]. Then circle one more SMP on the back of this packet that you think was addressed in this unit and be prepared to share an example.

4. **Making Connections.** Give examples of how a function helps us to explore changing quantities and predict what might happen.

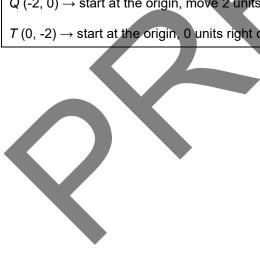
STUDENT RESOURCES

Word or Phrase	Definition
coefficient	A <u>coefficient</u> is a number or constant factor in a term of an algebraic expression.
	In the expression $3x + 5$, 3 is the coefficient of the term $3x$, and 5 is the constant term.
dependent variable	A dependent variable is a variable whose value is determined by the values of the independent variables. See independent variable.
function	A <u>function</u> is a rule that assigns to each input value exactly one output value.
	For $y = 3x + 6$, any input value, say $x = 10$, has a unique output value, in this case $y = 36$.
	For $y = x^2 + 1$, $x = 2$ has the unique output value $y = 2^2 + 1 = 5$.
graph of a function	The graph of a function is the set of all ordered pairs (x, y) where y is the output for the input value x. If x and y are real numbers, then we can represent the graph of a function as points in the coordinate plane.
independent variable	An independent variable is a variable whose value may be specified. Once specified, the values of the independent variables determine the values of the dependent variables.
	For the equation $y = 3x$, y is the dependent variable and x is the independent variable. We may assign a value to x. The value assigned to x determines the value of y.
input-output rule	An <u>input-output rule</u> for a sequence of values is a rule that establishes explicitly an output value for each given input value.
	input value (x) 1 2 3 4 5 x output value (y) 1.5 3 4.5 6 7.5 1.5x
	In the table above, the input-output rule could be $y = 1.5x$. To get the output value, multiply the input value by 1.5. If $x = 100$, then $y = 1.5(100) = 150$.
proportional	Two variables are <u>proportional</u> if the values of one are the same constant multiple of the corresponding values of the other. The variables are said to be in a <u>proportional</u> <u>relationship</u> , and the constant is referred to as the <u>constant of proportionality</u> .
	If Wrigley eats 3 cups of kibble each day, then the number of cups of kibble is proportional to the number of days. If x is the number of days, and y is the number of cups of kibble, then $y = 3x$. The constant of proportionality is 3.
unit rate	The <u>unit rate</u> associated with a ratio $a : b$ of two quantities a and $b, b \neq 0$,
	is the number $\frac{a}{b}$, to which units may be attached. This is sometimes referred to as the
	value of the ratio.
	The ratio of 40 miles for every 5 hours has a unit rate of 8 miles per hour.

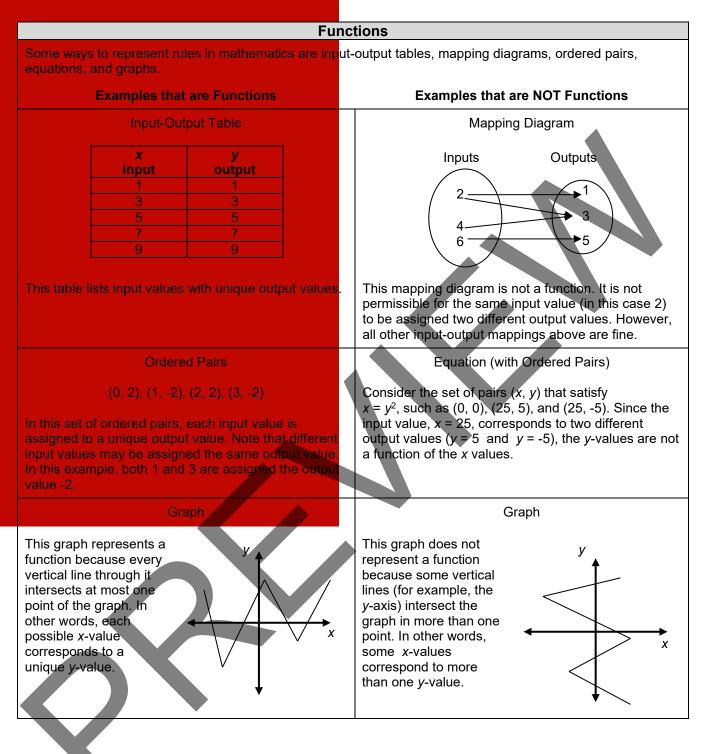
Introduction to Functions

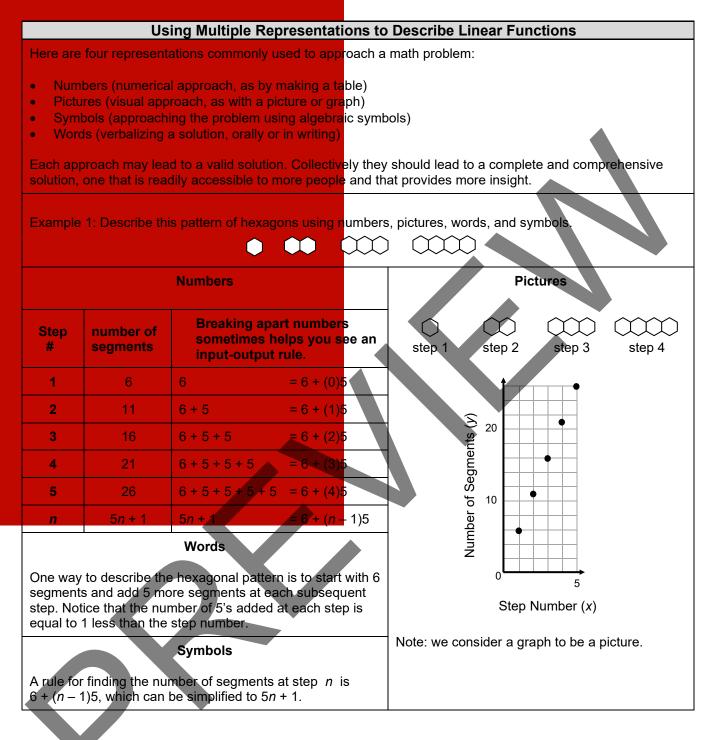
Student Resources

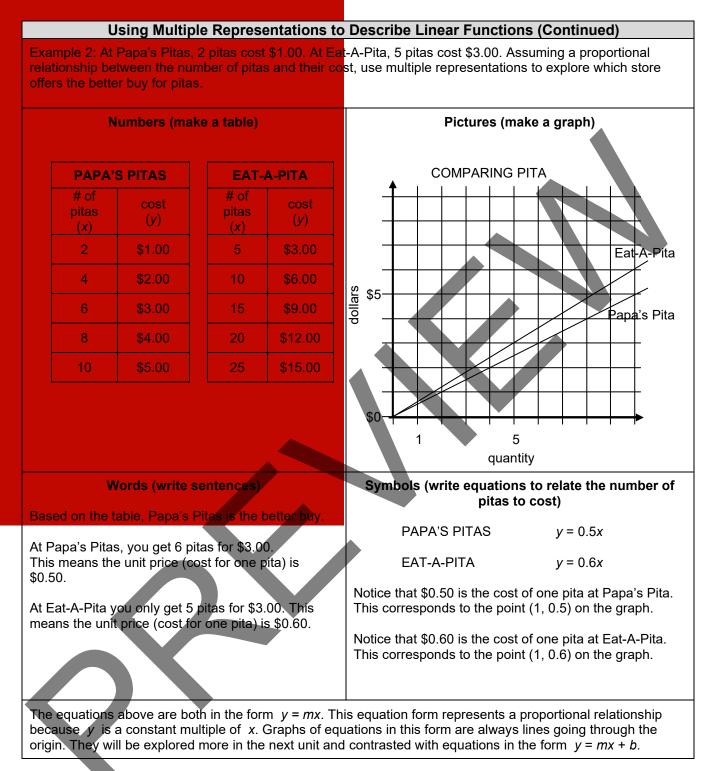
Word or Phrase	Definition		
<i>y</i> -intercept	The <u>y-intercept</u> of a line is the y-coordinate of the point at which the line crosses the y-axis. It is the value of y that corresponds to $x = 0$.		
	The y-intercept of the line $y = 3x + 6$ is 6. If $x = 0$, then $y = 6$.		
	The Coordinate Plane		
	s determined by a horizontal number line (the x-axis) and a vertical number line (the y-axis) ero on each line. The point of intersection $(0, 0)$ of the two lines is called the origin. Points dered pairs (x, y) .		
to the right or le			
	nber (<i>y</i> -coordinate) indicates how far the relation of the re		
	, and interpretation		
$O(0, 0) \rightarrow$ This is the intersection of the axes (origin).			
$P(2, 1) \rightarrow$ start at the origin, move 2 units right, then 1 unit up			
$R(-3, -1) \rightarrow \text{start at}$	the origin, move 3 units left, then 1 unit down		
S (1, -3) \rightarrow start at t	he origin, i unit right, then 3 units down		
Q (-2, 0) \rightarrow start at the origin, move 2 units left, then 0 units up or down			
$T(0, -2) \rightarrow$ start at the origin, 0 units right or left, then 2 units down			



Introduction to Functions







COMMON CORE STATE STANDARDS

STANDARDS FOR MATHEMATICAL CONTENT		
8.EE.B	Understand the connections between proportional relationships, lines, and linear equations.	
8.EE.5	Graph proportional relationships, interpreting the unit rate as the slope of the graph. Compare two different proportional relationships represented in different ways. For example, compare a distance-time graph to a distance-time equation to determine which of two moving objects has greater speed.	
8.F.A	Define, evaluate, and compare functions.	
8.F.1	Understand that a function is a rule that assigns to each input exactly one output. The graph of a function is the set of ordered pairs consisting of an input and the corresponding output.	
8.F.2	Compare properties of two functions each represented in a different way (algebraically, graphically, numerically in tables, or by verbal descriptions). For example, given a linear function represented by a table of values and a linear function represented by an algebraic expression, determine which function has the greater rate of change.	
8.F.3	Interpret the equation $y = mx + b$ as defining a linear function, whose graph is a straight line; give examples of functions that are not linear. For example, the function $A = s^2$ giving the area of a square as a function of its side length is not linear because its graph contains the points (1,1), (2,4) and (3,9), which are not on a straight line.	
8.F.B	Use functions to model relationships between quantities.	
8.F.4	Construct a function to model a linear relationship between two quantities. Determine the rate of change and initial value of the function from a description of a relationship or from two (x, y) values, including reading these from a table or from a graph. Interpret the rate of change and initial value of a linear function in terms of the situation it models, and in terms of its graph or a table of values.	
8.F.5	Describe qualitatively the functional relation ship between two quantities by analyzing a graph (e.g., where the function is increasing or decreasing, linear or nonlinear). Sketch a graph that exhibits the qualitative features of a function that has been described verbally.	

STANDARDS FOR MATHEMATICAL PRACTICE

- SMP1 Make sense of problems and persevere in solving them.
- SMP2 Reason abstractly and quantitatively.
- SMP3 Construct viable arguments and critique the reasoning of others.
- SMP4 Model with mathematics.
- SMP5 Use appropriate tools strategically.
- SMP6 Attend to precision.
- SMP7 Look for and make use of structure.
- SMP8 Look for and express regularity in repeated reasoning.

