Name_____

Period _____ Date _____

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MY WORD BANK

Explain the mathematical meaning of each word or phrase, using pictures and examples when possible. See **Student Resources** for mathematical vocabulary.



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PAPER SOLIDS

Follow your teacher's directions for (1) - (4) for each solid.



VOLUME OF CYLINDERS

We will develop the formula for the volume of a cylinder and use it to solve problems. [8.G.9; SMP1, 2, 3, 4, 5, 6, 7]

GETTING STARTED

Find the area of each circle with the given radius (r) or diameter (d) measures.

- 1. r = 6 mm (Use $\pi = 3.14$.)
- 2. d = 8 mm (Leave in terms of π .)

Consider the rectangular prism pictured to the right to complete the following.

- 3. How many squares are in the rectangular base (*B*) of this prism (either top or bottom)?
- 4. How many cubes are in the top (or bottom) horizontal "layer" of this rectangular prism?
- 5. How many horizontal layers are there?
- 6. How many cubes are there in all (the total volume)? _____
- 7. Write the length, width, and height of this prism: $\ell =$ ____, w =____, h =____
- 8. Write a formula to find the volume of a rectangular prism using ℓ , *w*, and *h*:
- 9. Write a second version of this formula using *B* as the area of the base:
 V = ______



VOLUME OF A CYLINDER



Find the volume of each cylinder described below.

8. Use $\pi = 3.14$,	9. Use $\pi = \frac{22}{7}$,	10. Leave in terms of π ,
h = 10 cm, $d = 4$ cm	$h = \frac{7}{8}$ in, $r = \frac{1}{2}$ in	$h = 6$ mm, $C = 24 \pi$ mm

11. Record the meaning of cylinder in My Word Bank.

PRACTICE 1

Find the volume of each cylinder described below.



Find the height of each cylinder described below.

6. A cylinder with circumference of 62.8 inches has volume = 628 cubic inches. Use π = 3.14.	 7. A cylinder with diameter = 8 cm has volume = 400 cubic cm. Write in terms of π and use π = 3.14.

PRACTICE 2: EXTEND YOUR THINKING

In the opening problem, you created models for a square prism, triangular prism, and cylinder from an 8.5 × 11-inch piece of paper with a height of 8.5 inches. Then you found the volumes.

- 1. Go back to **Paper Solids** and update or correct your work if needed.
- 2. Suppose you created models for a square prism, triangular prism, and cylinder from an 8.5 × 11-inch piece of paper with a height of 11 inches. Which of the six models do you think would have the greatest volume? Why?
- 3. In the space provided on **Paper Solids**, sketch the following with 11-inch heights:
 - Sketch #4, a square prism,
 - Sketch #5, a triangular prism, and
 - Sketch #6, a cylinder.

Then find the areas of the bases and the volumes.

4. Write conclusions based on your work. Compare volumes based on the height or shape of the base. Include which has the greatest volume and the least volume in your explanation.



5. A soup can is measured and found to have a radius of about 3.7 cm and a height of about 7.3 cm. The label on the can lists the volume as 310.52 mL. Is this a reasonable volume of soup? Explain. (1 cubic cm is equivalent to 1 mL.)

Plane and Solid Figures

A COIN PROBLEM

To the right is some information about coins.

Suppose you had a \$10 stack of dimes and a \$10 stack of quarters.

- 1. Make some predictions:
 - Which stack will have the greatest weight?
 - Which stack will have the greatest height?
 - Which stack will have the greatest volume?

2. Compute the weight, height, and volume for the \$10 stacks of coins.

	weight	height	volume
dime			
quarter			

3. Compare your results to your predictions. Were there any surprises?

	Dime	Quarter
Weight (grams)	2.27	5.67
Thickness (mm)	1.35	1.75
Diameter (mm)	17.9	24.26

VOLUME OF CONES AND SPHERES

We will develop formulas for the volume of a cone and a sphere and apply them to solve problems. [8.G.9; SMP2, 3, 4, 3, 5, 6, 7, 8]



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VOLUME OF A CONE AND A SPHERE





8. Record the meanings of <u>cone</u> and <u>sphere</u> in **My Word Bank**.

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ICE CREAM CONES

An ice cream store has two different kinds of cones. For a single scoop, they fill the cone with ice cream and then put a dome (half sphere) of ice cream on the top. Below are the dimensions and prices for one scoop. *Remember that d = 2r.

	Height	Top Diameter*	Botto Diame	om ter*	Cost	
Sugar Cone	$4\frac{5}{8}$ inches	2 inches	0 incł	ies	\$3.50	
Cake Cone	3 inches	$2\frac{1}{2}$ inches	$1\frac{1}{2}$ ir	ich	\$3.50	•



- 1. Predict which option you think will have the most ice cream:
- 2. Rank the amount of ice cream from least to greatest. Show formulas and substitutions.

Sugar Cone	Cake Cone Assume two cylinders. The bottom has twice the height as the top.

3. Which is the best buy? Which would you choose? Explain your reasoning.

LINES, ANGLES, AND TRIANGLES

We will establish facts about angles in the interior and on the exterior of a triangle. We will introduce vocabulary and facts related to angles formed when two parallel lines are intersected by another line. We will use properties of parallel lines to solve problems.





Measure of $\angle d \rightarrow |\angle d|$

Use a protractor to find angle measures in degrees for the figures above.

6.	∠d	7. ∠P	8. ∠ <i>KMN</i>
9.	∠PQN	10. ∠ <i>PRK</i>	11. ∠ <i>PK</i> R



TWO INVESTIGATIONS ROLLED INTO ONE

Plane and Solid Figures

ANGLES

1. Your teacher will give you some cards. Match vocabulary to descriptions and pictures.

Total total fill give you come called the									1001
Vocabulary	А	В	С		D	Е	F	G	Н
Description									
Picture									

- 2. Which card(s) were difficult to match up? Explain.
- 3. Find the missing angle measures in the figure below.





ANGLE RELATIONSHIPS

10. Record the meanings of <u>parallel</u> and <u>transversal</u> in **My Word Bank**.

PRACTICE 3

- 1. If two lines are cut by a transversal, and the three statements below are true, what do we know about the two lines?
 - corresponding angles have equal measure
 - alternate interior angles have equal measure
 - alternate exterior angles have equal measure
- 2. In the figure to the right, assume lines that appear to be parallel are parallel. Label the parallel lines using arrow notation. Then find the measures of all labeled angles.
 - |∠a| =____ |∠b| =____
 - $|\angle f| = |\angle g| =$
 - [h] =____



Name one pair of each of the following types of angles from the figure above.

3.	Acute, vertical angles	4.	Right, vertical angles	5.	Obtuse, vertical angles
6.	Form a straight angle	7.	Corresponding angles with the same measures	8.	Alternate exterior angles with the same measures
9.	Alternate interior angles with the same measures	10.	Adjacent, supplementary angles	11.	Vertical, supplementary angles

- 12. When do corresponding angles have equal measures?
- 13. For the triangle in the figure above, name two exterior angles whose measures are equal to the sum of $|\angle m| + |\angle d|$.
- 14. Record the meanings of <u>corresponding angles</u>, <u>alternate interior angles</u>, <u>alternate exterior</u> <u>angles</u>, and <u>exterior angle of a triangle</u> in **My Word Bank**.

ANGLE FACTS RELATED TO TRIANGLES



11. Choose any three **unused** cards so that you can draw a figure that incorporates all three of them. Describe your examples.

Cards chosen:	Bold words on cards:
Figure and descriptions:	

PRACTICE 4





11. Corresponding angles in the figure above have the same measure. Under what condition do corresponding angles NOT have the same measure?

REVIEW

POSTER PROBLEMS: PLANE AND SOLID FIGURES

Part 1: Your teacher will divide you into groups.

- Identify members of your group as A, B, C, or D.
- Each group will start at a numbered poster. Our group start poster is
- Each group will have a different colored marker. Our group marker is

Part 2: Do the problems on the posters by following your teacher's directions.



- Use π = 3.14 and round results to two decimal places as needed.
- A. Write the name of the solid figure and its volume formula. If a second, equivalent formula exists, include it.
- B. Find the volume of the solid.
- C. Find the volume if the height of the solid is doubled.
- D. Find the volume of the solid if ALL given measures on the figure are doubled.

Part 3: Return to your seats. Work with your group, and show all work.

Compare the three volume measures in parts B – D for your "start problem." Record what you notice below. Be ready to share with the class.

MATCH AND COMPARE SORT: PLANE AND SOLID FIGURES

Your teacher will give you some cards. Cut them out.

1. Individually, match words with descriptions. Record results.

	Card set 🛆			Card set 🔿
Card number	word	Card letter	Card number	word Card letter
I			I	
п			п	
ш			ш	
IV			IV	

2. Partners, choose a pair of numbered matched cards and record the attributes that are the same and those that are different.



3. Partners, choose another pair of numbered matched cards and discuss the attributes that are the same and those that are different.

A BIG PUZZLE

Use the figure below for all problems. For problems 1 – 8, name an angle that is:

1. adjacent to $\angle m$.	2. vertical to $\angle r$.	3. supplementary to $\angle m$.	
4. corresponding to $\angle z$.	5. complementary to $\angle e$.	6. alternate interior to $\angle u$.	
7. alternate exterior to $\angle j$.	8. an exterior angle of a trian	or angle of a triangle and equal to $ \angle h + \angle x $.	

Find the angle measures in any order. Notice that $| \angle a |$, $| \ge h |$ and $| \ge z |$ are given.





Review





SPIRAL REVIEW

1. **READY-X.** Solve for the values of R, E, A, D, Y, X. Sums of rows and columns are indicated at the end of each row and column.





- 3. Write an expression for each word description.
 - a. 3 more than 4 times a number
 - b. The difference of twice a number and 20
 - c. 2 less than the sum of a number and 8
 - d. The quotient of a number and the sum of 5 and 7



REFLECTION

1. **Big Ideas**. Shade all circles that describe big ideas in this unit. Draw lines to show connections that you noticed.



Give an example from this unit of one of the connections above.

- 2. Unit Progress. Go back to Monitor Your Progress on the cover and complete or update your responses. Explain something you understand better now than before or something you would still like to work on.
- 3. **Mathematical Practice.** Explain how the structure of a previously learned concept helped you learn a new one [SMP7]. Then circle one more SMP on the back of this packet that you think was addressed in this unit and be prepared to share an example.

4. More Connections. Describe something new that you learned about shapes and space.

STUDENT RESOURCES



Word or Phrase	Definition		
cone	A circular <u>cone</u> is a figure in space consisting of a circle in a plane (called the <u>base</u> of the cone), a point off the plane (called the <u>vertex</u> of the cone), and all the straight line segments joining the vertex to the base. If the line joining the vertex of the cone to the center of its base is perpendicular to the base, the cone is a <u>right circular cone</u> . Otherwise it is an <u>oblique circular cone</u> .		
	right circular cone oblique circular cone		
corresponding angles	When two lines in a plane are out by a transversal, two angles that appear on the same side of the transversal in the same relative location are referred to as <u>corresponding</u> angles. When parallel lines are cut by a transversal, corresponding angles have the same measure.		
	Line <i>m</i> is not parallel to line <i>n</i> . $m = \frac{1}{1}$ Line <i>m</i> is parallel to line <i>n</i> . $m = \frac{1}{1}$ $n = \frac{1}{2}$ Line <i>m</i> is parallel to line <i>n</i> .		
	$\angle 1 \text{ and } \angle 2 \text{ are corresponding angles.} \qquad \qquad \angle 1 \text{ and } \angle 2 \text{ are corresponding angles.} \\ \angle 1 = \angle 2 $		
cylinder	A (right circular) <u>cylinder</u> is a figure in three-dimensional space that has two parallel circular bases. These circles are connected by a curved surface, called the <u>lateral</u> <u>surface</u> , which is a "rolled up" rectangle. Most soup cans have the shape of a right circular cylinder.		
	cylinder		
exterior angle of a triangle	An <u>exterior angle of a triangle</u> is an angle formed by a side of the triangle and an extension of its adjacent side.		
	$\angle 1$ is an exterior angle of $\triangle ABC$.		

Plane and Solid Figures

Word or Phrase	Definition			
parallel	Two lines in a plane are <u>parallel</u> if they do not meet. Two line segments in a plane are parallel if the lines they lie on are parallel.			
perpendicular	Two lines are <u>perpendicular</u> if they intersect at right angles.			
sphere	A <u>sphere</u> is a closed surface in three-dimensional space consisting of all points at a fixed distance (the radius) from a specified point (the center).			
supplementary angles	Two angles are <u>supplementary</u> if the sum of their measures is 180°. Any two right angles are supplementary, because the sum of their measures is $90^\circ + 90^\circ = 180^\circ$. Angles A and B are supplementary because they $AB \to B$			
transversal	A <u>transversal</u> is a line that passes through two or more other lines.			
vertical angles	Two angles are vertical angles if they are the opposite angles formed by a pair of intersecting lines. When two lines intersect at a point, they form two pairs of vertical angles with vertex at the point.			
	$\angle 1$ and $\angle 3$ are vertical angles. $\angle 2$ and $\angle 4$ are vertical angles. 4 3 2			
	Some Properties of Equality			
Properties of equality govern the manipulation of equations (mathematical sentences). For any three numbers <i>a</i> , <i>b</i> , and <i>c</i> :				
 ✓ Addition prop (Subtraction If a = b and ✓ Multiplication (Division prop 	perty of equality property of equality) \checkmark Reflexive property of equality $a = a$ $c = d$, then $a + c = b + d$. \checkmark Symmetric property of equality If $a = b$, then $b = a$			
If $a = b$ and	$c = d$, then $ac = bd$ \checkmark Transitive property of equality (Substitution property) If $a = b$, and $b = c$, then $a = c$			



Circumference:

Area:

d

 $C = \pi d$ or C = 2πr

 $A = \pi r^2$





$$|\angle b| + |\angle e| = |\angle f|$$

COMMON CORE STATE STANDARDS

STANDARDS FOR MATHEMATICAL CONTENT				
8.G.A	Understand congruence and similarity using software.	physical models, transparencies, or geometry		
8.G.5	Use informal arguments to establish facts about the angles created when parallel lines are cut by similarity of triangles. For example, arrange thre three angles appears to form a line, and give ar	the angle sum and exterior angle of triangles, about y a transversal, and the angle angle criterion for e copies of the same triangle so that the sum of the argument in terms of transversals why this is so.		
8.G.C	Solve real-world and mathematical problems spheres.	involving volume of cylinders, cones, and		
8.G.9	Know the formulas for the volumes of cones, cy and mathematical problems.	linders, and spheres and use them to solve real-world		
STANDARDS FOR MATHEMATICAL PRACTICE				
SMP1	Make sense of problems and persevere in sol	ving them.		
SMP2	Reason abstractly and quantitatively.			
SMP3	Construct viable arguments and critique the re	asoning of others.		
SMP4	Model with mathematics.			

- SMP5 Use appropriate tools strategically.
- SMP6 Attend to precision.
- SMP7 Look for and make use of structure.
- SMP8 Look for and express regularity in repeated reasoning.



