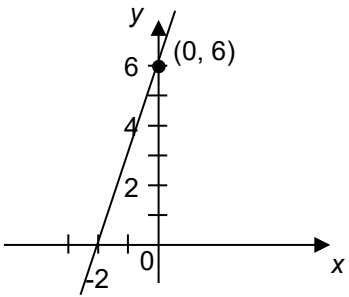


STUDENT RESOURCES

Word or Phrase	Definition														
coefficient	<p>A <u>coefficient</u> is a number or constant factor in a term of an algebraic expression.</p> <p>In the expression $3x + 5$, 3 is the coefficient of the term $3x$, and 5 is the constant term.</p>														
dependent variable	<p>A <u>dependent variable</u> is a variable whose value is determined by the values of the independent variables. See <u>independent variable</u>.</p>														
function	<p>A <u>function</u> is a rule that assigns to each input value exactly one output value.</p> <p style="padding-left: 40px;">For $y = 3x + 6$, any input value, say $x = 10$, has a unique output value, in this case $y = 36$.</p> <p style="padding-left: 40px;">For $y = x^2 + 1$, $x = 2$ has the unique output value $y = 2^2 + 1 = 5$.</p>														
graph of a function	<p>The <u>graph of a function</u> is the set of all ordered pairs (x, y) where y is the output for the input value x. If x and y are real numbers, then we can represent the graph of a function as points in the coordinate plane.</p>														
independent variable	<p>An <u>independent variable</u> is a variable whose value may be specified. Once specified, the values of the independent variables determine the values of the dependent variables.</p> <p style="padding-left: 40px;">For the equation $y = 3x$, y is the dependent variable and x is the independent variable. We may assign a value to x. The value assigned to x determines the value of y.</p>														
input-output rule	<p>An <u>input-output rule</u> for a sequence of values is a rule that establishes explicitly an output value for each given input value.</p> <table border="1" style="margin-left: auto; margin-right: auto;"> <tbody> <tr> <td style="text-align: center;">input value (x)</td> <td style="text-align: center;">1</td> <td style="text-align: center;">2</td> <td style="text-align: center;">3</td> <td style="text-align: center;">4</td> <td style="text-align: center;">5</td> <td style="text-align: center;">x</td> </tr> <tr> <td style="text-align: center;">output value (y)</td> <td style="text-align: center;">1.5</td> <td style="text-align: center;">3</td> <td style="text-align: center;">4.5</td> <td style="text-align: center;">6</td> <td style="text-align: center;">7.5</td> <td style="text-align: center;">$1.5x$</td> </tr> </tbody> </table> <p style="padding-left: 40px;">In the table above, the input-output rule could be $y = 1.5x$. To get the output value, multiply the input value by 1.5. If $x = 100$, then $y = 1.5(100) = 150$.</p>	input value (x)	1	2	3	4	5	x	output value (y)	1.5	3	4.5	6	7.5	$1.5x$
input value (x)	1	2	3	4	5	x									
output value (y)	1.5	3	4.5	6	7.5	$1.5x$									
proportional	<p>Two variables are <u>proportional</u> if the values of one are the same constant multiple of the corresponding values of the other. The variables are said to be in a <u>proportional relationship</u>, and the constant is referred to as the <u>constant of proportionality</u>.</p> <p style="padding-left: 40px;">If Wrigley eats 3 cups of kibble each day, then the number of cups of kibble is proportional to the number of days. If x is the number of days, and y is the number of cups of kibble, then $y = 3x$. The constant of proportionality is 3.</p>														
unit rate	<p>The <u>unit rate</u> associated with a ratio $a : b$ of two quantities a and b, $b \neq 0$, is the number $\frac{a}{b}$, to which units may be attached. This is sometimes referred to as the <u>value of the ratio</u>.</p> <p style="padding-left: 40px;">The ratio of 40 miles for every 5 hours has a unit rate of 8 miles per hour.</p>														

Word or Phrase	Definition
y-intercept	<p>The <u>y-intercept</u> of a line is the y-coordinate of the point at which the line crosses the y-axis. It is the value of y that corresponds to $x = 0$.</p> <p>The y-intercept of the line $y = 3x + 6$ is 6. If $x = 0$, then $y = 6$.</p> 

The Coordinate Plane

A coordinate plane is determined by a horizontal number line (the x-axis) and a vertical number line (the y-axis) intersecting at the zero on each line. The point of intersection $(0, 0)$ of the two lines is called the origin. Points are located using ordered pairs (x, y) .

- The first number (x -coordinate) indicates how far the point is to the right or left of the y -axis.
- The second number (y -coordinate) indicates how far the point is above or below the x -axis.

Point, coordinates, and interpretation

$O(0, 0)$ → This is the intersection of the axes (origin).

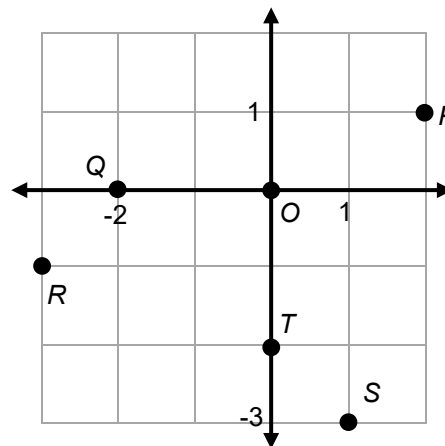
$P(2, 1)$ → start at the origin, move 2 units right, then 1 unit up

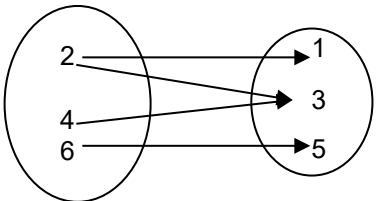
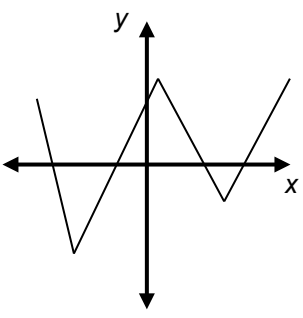
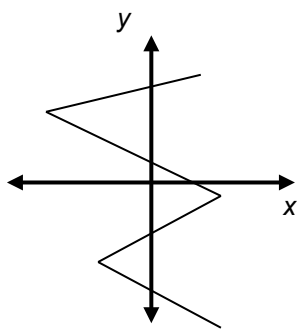
$R(-3, -1)$ → start at the origin, move 3 units left, then 1 unit down

$S(1, -3)$ → start at the origin, 1 unit right, then 3 units down

$Q(-2, 0)$ → start at the origin, move 2 units left, then 0 units up or down

$T(0, -2)$ → start at the origin, 0 units right or left, then 2 units down



Functions													
Some ways to represent rules in mathematics are input-output tables, mapping diagrams, ordered pairs, equations, and graphs.													
Examples that are Functions	Examples that are NOT Functions												
<p style="text-align: center;">Input-Output Table</p> <table border="1" style="margin: auto; border-collapse: collapse; text-align: center;"> <thead> <tr> <th style="padding: 5px;">x input</th> <th style="padding: 5px;">y output</th> </tr> </thead> <tbody> <tr><td style="padding: 5px;">1</td><td style="padding: 5px;">1</td></tr> <tr><td style="padding: 5px;">3</td><td style="padding: 5px;">3</td></tr> <tr><td style="padding: 5px;">5</td><td style="padding: 5px;">5</td></tr> <tr><td style="padding: 5px;">7</td><td style="padding: 5px;">7</td></tr> <tr><td style="padding: 5px;">9</td><td style="padding: 5px;">9</td></tr> </tbody> </table> <p style="margin-top: 10px;">This table lists input values with unique output values.</p>	x input	y output	1	1	3	3	5	5	7	7	9	9	<p style="text-align: center;">Mapping Diagram</p> <div style="text-align: center; margin-bottom: 10px;"> Inputs Outputs </div>  <p style="margin-top: 10px;">This mapping diagram is not a function. It is not permissible for the same input value (in this case 2) to be assigned two different output values. However, all other input-output mappings above are fine.</p>
x input	y output												
1	1												
3	3												
5	5												
7	7												
9	9												
<p style="text-align: center;">Ordered Pairs</p> <p style="text-align: center; margin: 5px 0;">(0, 2), (1, -2), (2, 2), (3, -2)</p> <p style="margin-top: 10px;">In this set of ordered pairs, each input value is assigned to a unique output value. Note that different input values may be assigned the same output value. In this example, both 1 and 3 are assigned the output value -2.</p>	<p style="text-align: center;">Equation (with Ordered Pairs)</p> <p style="margin-top: 10px;">Consider the set of pairs (x, y) that satisfy $x = y^2$, such as $(0, 0)$, $(25, 5)$, and $(25, -5)$. Since the input value, $x = 25$, corresponds to two different output values ($y = 5$ and $y = -5$), the y-values are not a function of the x values.</p>												
<p style="text-align: center;">Graph</p> <p style="margin-top: 10px;">This graph represents a function because every vertical line through it intersects at most one point of the graph. In other words, each possible x-value corresponds to a unique y-value.</p> 	<p style="text-align: center;">Graph</p> <p style="margin-top: 10px;">This graph does not represent a function because some vertical lines (for example, the y-axis) intersect the graph in more than one point. In other words, some x-values correspond to more than one y-value.</p> 												

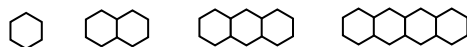
Using Multiple Representations to Describe Linear Functions

Here are four representations commonly used to approach a math problem:

- Numbers (numerical approach, as by making a table)
- Pictures (visual approach, as with a picture or graph)
- Symbols (approaching the problem using algebraic symbols)
- Words (verbalizing a solution, orally or in writing)

Each approach may lead to a valid solution. Collectively they should lead to a complete and comprehensive solution, one that is readily accessible to more people and that provides more insight.

Example 1: Describe this pattern of hexagons using numbers, pictures, words, and symbols.



Numbers

Step #	number of segments	Breaking apart numbers sometimes helps you see an input-output rule.
1	6	$6 = 6 + (0)5$
2	11	$6 + 5 = 6 + (1)5$
3	16	$6 + 5 + 5 = 6 + (2)5$
4	21	$6 + 5 + 5 + 5 = 6 + (3)5$
5	26	$6 + 5 + 5 + 5 + 5 = 6 + (4)5$
n	$5n + 1$	$5n + 1 = 6 + (n - 1)5$

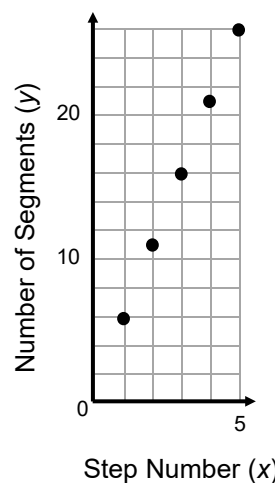
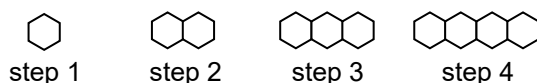
Words

One way to describe the hexagonal pattern is to start with 6 segments and add 5 more segments at each subsequent step. Notice that the number of 5's added at each step is equal to 1 less than the step number.

Symbols

A rule for finding the number of segments at step n is $6 + (n - 1)5$, which can be simplified to $5n + 1$.

Pictures



Note: we consider a graph to be a picture.

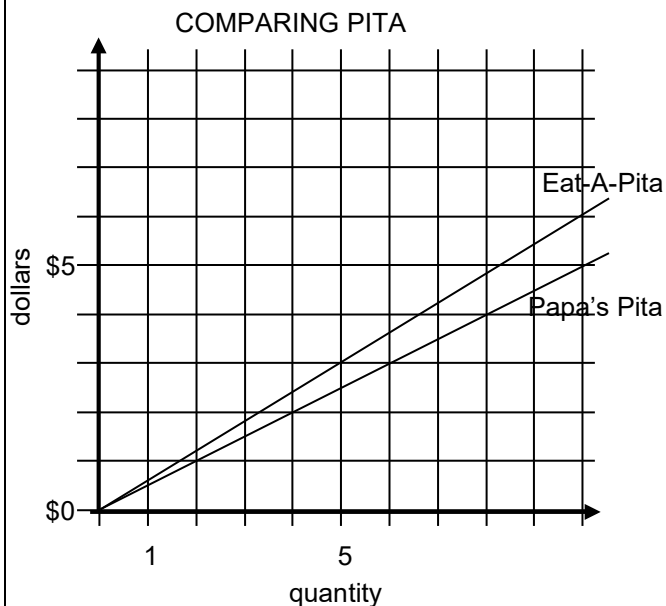
Using Multiple Representations to Describe Linear Functions (Continued)

Example 2: At Papa’s Pitas, 2 pitas cost \$1.00. At Eat-A-Pita, 5 pitas cost \$3.00. Assuming a proportional relationship between the number of pitas and their cost, use multiple representations to explore which store offers the better buy for pitas.

Numbers (make a table)

PAPA’S PITAS		EAT-A-PITA	
# of pitas (x)	cost (y)	# of pitas (x)	cost (y)
2	\$1.00	5	\$3.00
4	\$2.00	10	\$6.00
6	\$3.00	15	\$9.00
8	\$4.00	20	\$12.00
10	\$5.00	25	\$15.00

Pictures (make a graph)



Words (write sentences)

Based on the table, Papa’s Pitas is the better buy.

At Papa’s Pitas, you get 6 pitas for \$3.00. This means the unit price (cost for one pita) is \$0.50.

At Eat-A-Pita you only get 5 pitas for \$3.00. This means the unit price (cost for one pita) is \$0.60.

Symbols (write equations to relate the number of pitas to cost)

PAPA’S PITAS $y = 0.5x$

EAT-A-PITA $y = 0.6x$

Notice that \$0.50 is the cost of one pita at Papa’s Pita. This corresponds to the point (1, 0.5) on the graph.

Notice that \$0.60 is the cost of one pita at Eat-A-Pita. This corresponds to the point (1, 0.6) on the graph.

The equations above are both in the form $y = mx$. This equation form represents a proportional relationship because y is a constant multiple of x . Graphs of equations in this form are always lines going through the origin. They will be explored more in the next unit and contrasted with equations in the form $y = mx + b$.