## Unit 5: Rational Numbers 2

## Dear Parents/Guardians,

Unit 5 continues with the counter model to develop integer multiplication rules. Students investigate patterns and the inverse relationship between multiplication and division to develop integer division rules. In this lesson, a temperature context from the opening lesson connects to the counter model. In Lesson 2 students use number lines as a way to convince themselves that the integer multiplication and division rules hold for other rational numbers (signed fractions and decimals). In Lesson 3 students make sense of the order of operations conventions and use the order of operations to solve problems involving rational numbers.

## The Counter Model

A positive (+) counter represents a value of 1. ط
A negative (-) counter represents a value of -1 . $\square$
A "zero pair" is represented by one positive and one negative counter and has a value of zero (0).


Place two groups of 3 on the mat. positive $\times$ positive $=$ positive
$(-2) \cdot(3)=-6$


Start with two rows of 3 zero pairs (to keep the value 0).
Remove two groups of 3 from the mat.
negative $\times$ positive $=$ negative
(2) $\cdot(-3)=-6$


Place two groups of ( -3 ) on the mat. positive x negative $=$ negative

$$
(-2) \cdot(-3)=-6
$$



Start with two rows of 3 zero pairs (to keep the value 0).
Remove two groups of (-3) from the mat.
negative $\times$ negative $=$ positive

## Relating Multiplication and Division

Students use the relationship between multiplication and division to develop rules for signed division.

| Multiplication <br> Fact | Related Division <br> Facts | Division Rule |
| :---: | :---: | :---: |
| $(5) \times(8)=40$ | $40 \div(5)=8$ |  |
| $40 \div(8)=5$ | positive $\div$ positive = positive |  |
| $(3) \times(-4)=-12$ | $-12 \div(3)=-4$ | negative $\div$ positive $=$ negative |
| $-12 \div(-4)=3$ | negative $\div$ negative $=$ positive |  |
| $(-2) \times(7)=-14$ | $-14 \div(-2)=7$ | negative $\div$ negative $=$ positive |
| $-14 \div(7)=-2$ | negative $\div$ positive $=$ negative |  |
| $(-5) \times(-6)=30$ | $30 \div(-6)=-5$ | positive $\div$ negative $=$ negative |

## Math <br> GRADE 7 Links

By the end of the unit, your student should know...

- How to multiply integers using counters and then rules [Lesson 5.1]
- How to divide integers based upon the inverse relationship between multiplication and division [Lessons 5.1 and 5.2]
- How to represent multiplication of rational numbers on a number line [Lesson 5.2]
- How to multiply and divide rational numbers using any method [Lesson 5.2]
- How to use the conventions of the order of operations to evaluate expressions and solve problems [Lesson 5.3]


## Additional Resources

- For definitions and additional notes please refer to Student Resources at the end of this unit.
- For more on multiplying integers with counters: https://youtu.be/MuZ3Y3PYv2U and https://youtu.be/Yhozlg35alw
- For more on order of operations:
https://tinyurl.com/khan-order-of-operations

