## STUDENT RESOURCES

| Word or Phrase | Definition |
| :---: | :---: |
| area | The area of a two-dimensional figure is a measure of the size of the figure, expressed in square units. <br> The area of a rectangle is the product of its length and width (Area $=$ length $\bullet$ width). or <br> The area of a rectangle is the product of its base and height (Area = base $\bullet$ height). <br> If this rectangle has a length of 12 inches and a width of 5 inches, then: $\begin{array}{ll} A=\ell w & A=b h \\ A=(12)(5) & \text { or } \\ A=(12)(5) \\ A=60 \text { square inches } & A=60 \text { square inches } \end{array}$ <br> length <br> base |
| net | A net for a three-dimensional figure is a two-dimensional pattern for the figure. <br> If cut from a sheet of paper, for example, <br> net of a cube a net forms one connected piece which can be folded with the edges joined to form the given figure. |
| plane | A plane is a flat, two-dimensional surface without holes that extends to infinity in all directions. |
| polygon | A polygon is a special kind of figure in a plane made up of a chain of line segments laid end-to-end to enclose a region. <br> polygons <br> not polygons |
| solid figure | A solid figure refers to a figure in three-dimensional space such as a prism or a cylinder. <br> cube <br> triangular prism <br> rectangular pyramid <br> cylinder |


| Word or Phrase | Definition |
| :---: | :---: |
| prism | A prism is a solid figure in which two faces (the bases) are identical parallel polygons, and the other faces (referred to as the lateral faces) are parallelograms. <br> If the lateral faces are perpendicular to the bases, the prism is a right prism. Otherwise, the prism is an oblique prism. <br> A right rectangular prism is a right prism whose bases are rectangles and whose faces are rectangles. <br> An oblique triangular prism is a prism whose bases are triangles and whose faces are parallelograms. |
| pyramid | A pyramid is a solid figure in which one face (the base) is a polygon, and the other faces (referred to as lateral faces) are triangles with a common vertex (referred to as the apex). <br> The Egyptian pyramids are square pyramids since they have square bases. |
| right rectangular prism | A right rectangular prism is a six-sided solid figure in which all the faces are rectangles. <br> A rectangular box is a right rectangular prism. |
| surface area | The surface area of a three-dimensional figure is a measure of the size of the surface of the figure, expressed in square units. If the surface of the three-dimensional figure consists of two-dimensional polygons, the surface area is the sum of the areas of the polygons. <br> If this rectangular box has a length of 3 inches, a width of 4 inches, and a height of 5 inches, then $\begin{aligned} & S A=2(\ell w)+2(\ell h)+(w h) \\ & S A=2(3 \bullet 4)+2(3 \bullet 5)+2(4 \bullet 5) \\ & S A=94 \text { square inches } \end{aligned}$ |


| Word or Phrase | Definition |
| :--- | :--- |
| vertex | A vertex (plural of vertices) of a polygon or solid figure is a point where two edges meet. <br> See polygon, solid figure. <br> A pentagon has five vertices. |
| volume | The volume of a three-dimensional figure is a measure of the size of the figure, <br> expressed in cubic units. The volume of a right rectangular prism is the product of its <br> length, width, and height. <br> If this cube has a side length of 3 units, then |
|  | $V=\ell w h$ <br> $V=3 \bullet 3 \bullet 3$ <br> $V=27$ cubic inches |
|  |  |

## Base of a Polygon (b) Versus Base of a Solid Figure (B)

The base of a polygon is a predesignated side of the figure. It is typically denoted with a "b."
The base is usually regarded as the "bottom" of the polygon. The top is also a base, if it is parallel to the bottom.


The base of a solid figure is a predesignated face of the figure. It is typically denoted with a "B."
The base is usually regarded as the "bottom" of the figure, on which it is standing. The "top" of a figure is sometimes also referred to as a base if it is identical and parallel to the "bottom."


## Composing and Decomposing Shapes: "Cut-Up Strategies"

Composing shapes refers to joining geometric shapes without overlaps to form other shapes.
Here are two identical triangles ( A and B ). When joining $A$ and $B$ (after rotating $B$ ), the result is a parallelogram with twice the area of each of the given triangles.


Decomposing shapes refers to taking a given geometric shape, and identifying geometric shapes that meet without overlap to form that given shape.

Given parallelogram $C$, we can identify a segment that creates two identical trapezoids $D$ and $E$, each with one-half the area of $C$.


Composing and decomposing shapes are useful strategies for finding area formulas for common polygons derived from ones we already know. We refer to these methods collectively as "cut-up" strategies. For example, first we learn the formula for area of a rectangle. Then we can use a cut-up strategy to find the formula for area of a parallelogram. Then we can use other cut-up strategies to find the formulas for area of a triangle and area of a trapezoid.

| Summary of Area Formulas |  |  |
| :---: | :---: | :---: |
| Shape/Definition | Diagram | Area |
| Rectangle a quadrilateral with 4 right angles |  | $\begin{gathered} A=b h \\ \text { or } \\ A=\ell w \end{gathered}$ |
| Square <br> a rectangle with 4 sides of equal length |  | $\begin{gathered} A=b^{2} \\ \text { or } \\ A=s^{2} \end{gathered}$ |
| Parallelogram a quadrilateral with opposite sides parallel |  | $A=b h$ |
| Triangle <br> a polygon with three sides |  | $A=\frac{1}{2} b h$ |
| Trapezoid a quadrilateral with at least one pair of parallel sides |  | $A=\frac{1}{2}\left(b_{1}+b_{2}\right) h$ |

## Volume and Surface Area of Right Rectangular Prisms

A right rectangular prism is identified by its length, width, and height.

The area of the base is the product of the length and width $(B=\ell w)$.

If the top and bottom rectangular faces are chosen as the bases, then the other rectangles are referred to as the lateral faces.


Area of base ( $B$ )


Right rectangular prism made with 30 cubes


## Volume

The volume of a prism may be computed by counting layers of unit cubes. In the prism above, each layer has 10 cubes $(5 \times 2)$. There are 3 layers.

The volume is $(5 \times 2)(3)=10(3)=30$ cubic units.
In general, multiply the area of the base (B) by the height.

$$
V=\ell w h \quad O R \quad V=B h
$$

Surface Area
The surface area may be computed by creating a net that shows the areas of each face of the prism. In this prism there are two faces with dimensions $2 \times 5$, two faces with dimensions $3 \times 2$, and two faces with dimensions $3 \times 5$.

The surface area is
$2(2 \times 5)+2(3 \times 2)+2(3 \times 5)$
$=20+12+30$
$=62$ square units.
In general, find the area of each rectangular face.

$$
\begin{array}{ll}
S A=\ell w+\ell w+w h+w h+\ell h+\ell h & \text { OR } \\
S A=2 \ell w+2 w h+2 \ell h & \text { OR } \\
S A=2(\ell w+w h+\ell h) &
\end{array}
$$

